

Designation: E2283 - 08 (Reapproved 2019)

Standard Practice for Extreme Value Analysis of Nonmetallic Inclusions in Steel and Other Microstructural Features¹

This standard is issued under the fixed designation E2283; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ε) indicates an editorial change since the last revision or reapproval.

1. Scope

1.1 This practice describes a methodology to statistically characterize the distribution of the largest indigenous nonmetallic inclusions in steel specimens based upon quantitative metallographic measurements. The practice is not suitable for assessing exogenous inclusions.

1.2 Based upon the statistical analysis, the nonmetallic content of different lots of steels can be compared.

1.3 This practice deals only with the recommended test methods and nothing in it should be construed as defining or establishing limits of acceptability.

1.4 The values stated in SI units are to be regarded as standard. No other units of measurement are included in this standard.

1.4.1 For measurements obtained from light microscopy, linear feature parameters shall be reported as micrometers, and feature areas shall be reported as micrometers.

1.5 The methodology can be extended to other materials and to other microstructural features.

1.6 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety, health, and environmental practices and determine the applicability of regulatory limitations prior to use.

1.7 This international standard was developed in accordance with internationally recognized principles on standardization established in the Decision on Principles for the Development of International Standards, Guides and Recommendations issued by the World Trade Organization Technical Barriers to Trade (TBT) Committee.

2. Referenced Documents

- 2.1 ASTM Standards:²
- E3 Guide for Preparation of Metallographic Specimens
- E7 Terminology Relating to Metallography
- E45 Test Methods for Determining the Inclusion Content of Steel
- E178 Practice for Dealing With Outlying Observations
- E456 Terminology Relating to Quality and Statistics
- E691 Practice for Conducting an Interlaboratory Study to Determine the Precision of a Test Method
- E768 Guide for Preparing and Evaluating Specimens for Automatic Inclusion Assessment of Steel
- E1122 Practice for Obtaining JK Inclusion Ratings Using Automatic Image Analysis (Withdrawn 2006)³
- E1245 Practice for Determining the Inclusion or Second-Phase Constituent Content of Metals by Automatic Image Analysis

3. Terminology

3.1 *Definitions*—For definitions of metallographic terms used in this practice, refer to Terminology, E7; for statistical terms, refer to Terminology E456.

3.2 Definitions of Terms Specific to This Standard:

3.2.1 A_f —the area of each field of view used by the Image Analysis system in performing the measurements.

3.2.2 A_o —control area; total area observed on one specimen per polishing plane for the analysis. A_o is assumed to be 150 mm² unless otherwise noted.

3.2.3 N_s —number of specimens used for the evaluation. N_s is generally six.

3.2.4 N_p —number of planes of polish used for the evaluation, generally four.

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¹ This practice is under the jurisdiction of ASTM Committee E04 on Metallography and is the direct responsibility of Subcommittee E04.09 on Inclusions.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

³ The last approved version of this historical standard is referenced on www.astm.org.

3.2.5 N_f —number of fields observed per specimen plane of polish.

$$N_f = \frac{A_o}{A_f} \tag{1}$$

3.2.6 *N*—total number of inclusion lengths used for the analysis, generally 24.

$$N = N_s \cdot N_p \tag{2}$$

3.2.7 *extreme value distribution*—The statistical distribution that is created based upon only measuring the largest feature in a given control area or volume (1,2).⁴ The continuous random variable x has a two parameter (Gumbel) Extreme Value Distribution if the probability density function is given by the following equation:

$$f(x) = \frac{1}{\delta} \left[\exp\left(-\frac{x-\lambda}{\delta}\right) \right] \times \exp\left[-\exp\left(-\frac{x-\lambda}{\delta}\right) \right]$$
(3)

and the cumulative distribution is given by the following equation:

$$F(x) = \exp(-\exp(-(x-\lambda)/\delta))$$
(4)

As applied to this practice, x, represents the maximum feret diameter, Length, of the largest inclusion in each control area, A_o , letting:

$$y = \frac{x - \lambda}{\delta}$$
 (5)

it follows that:

 $F(y) = \exp(-\exp(-y))$

and

$$x = \delta y + \lambda$$
 Document(7)

3.2.8 λ —the location parameter of the extreme value distribution function.

3.2.9 δ —the scale parameter of the extreme value distribution function.

3.2.10 *reduced variate*—The variable *y* is called the reduced variate. As indicated in Eq 6, *y* is related to the probability density function. That is y = F(P), then from Eq 6, it follows that:

$$y = -\ln(-\ln(F(y))) = -\ln(-\ln(P))$$
(8)

3.2.11 *plotting position*—Each of the *N* measured inclusion lengths can be represented as x_i , where $1 \le i \le N$. The data points are arranged in increasing order such that:

 $x_1 \le x_2 \le x_3 \le x_4 \le x_5 \dots \le x_N$ Then the cumulative probability plotting position for data point x_i is given by the relationship:

$$P_i = \frac{i}{N+1} \tag{9}$$

The fraction (i / (N + 1)) is the cumulative probability. $F(y_i)$ in Eq.8 corresponds to data point x_i .

3.2.12 mean longest inclusion length— \overline{L} is the arithmetic average of the set of N maximum feret diameters of the measured longest inclusions.

$$\overline{L} = \frac{1}{N} \sum_{i=1}^{i=N} L_i \tag{10}$$

3.2.13 *standard deviation of longest inclusion lengths*— Sdev is the standard deviation of the set of *N* maximum feret diameters of the measured longest inclusions.

Sdev =
$$\left[\sum_{i=1}^{N} (L_i - \overline{L})^2 / (N - 1)\right]^{0.5}$$
 (11)

3.2.14 *return period*—the number of areas that must be observed in order to find an inclusion equal to or larger than a specified maximum inclusion length. Statistically, the return period is defined as:

$$T = \frac{1}{1 - P} \tag{12}$$

3.2.15 reference area, A_{ref} —the arbitrarily selected area of 150 000 mm². A_{ref} in conjunction with the parameters of the extreme value distribution is used to calculate the size of the largest inclusion reported by this standard. As applied to this analysis, the largest inclusion in each control area A_o is measured. The Return Period, *T*, is used to predict how large an inclusion could be expected to be found if an area A_{ref} larger than A_o were to be evaluated. For this standard, A_{ref} is 1000 times larger than A_o . Thus, *T* is equal to 1000. By use of Eq 12 it would be found that this corresponds to a probability value of 0.999, (99.9 %). Similarly by using Eq 6 and 7, the length of an inclusion corresponding to the 99.99 % probability value could be calculated. Mathematically, another expression for the return period is:

$$T = \frac{A_{ref}}{A_o} \tag{13}$$

3.2.16 predicted maximum inclusion length, L_{max} —the longest inclusion expected to be found in area A_{ref} based upon the extreme value distribution analysis.

4. Summary of Practice

4.1 This practice enables the experimenter to estimate the extreme value distribution of inclusions in steels.

4.2 Generally, the largest oxide inclusions within the specimens are measured. However, the practice can be used to measure other microstructural features such as graphite nodules in ductile iron, or carbides in tool steels and bearing steels. The practice is based upon using the specimens described in Test Method E45. Six specimens will be required for the analysis. For inclusion analysis, an area of 150 mm² should be evaluated for each specimen.

4.3 After obtaining the specimens, it is recommended that they be prepared by following the procedures described in Methods E3 and Practice E768.

4.4 The polished specimens are then evaluated by using the guidelines for completing image analysis described in Practices E1122 and E1245. For this analysis, feature specific measurements are required. The measured inclusion lengths shall be based on a minimum of eight feret diameter measurements.

4.5 For each specimen, the maximum feret diameter of each inclusion is measured. After performing the analysis for each specimen, the largest maximum feret diameter of the measured

⁴ The boldface numbers in parentheses refer to the list of references at the end of this standard.

inclusions is recorded. This will result in six lengths. The procedure is repeated three more times. This will result in a total of 24 inclusion lengths.

4.6 The 24 measurements are used to estimate the values of δ and λ for the extreme value distribution for the particular material being evaluated. The largest inclusion L_{max} expected to be in the reference area A_{ref} is calculated, and a graphical representation of the data and test report are then prepared.

4.7 The reference area used for this standard is $150\ 000\ \text{mm}^2$. Based upon specific producer, purchaser requirements, other reference areas may be used in conjunction with this standard.

4.8 When required, the procedure can be repeated to evaluate more than one type of inclusion population in a given set of specimens. For example, oxides and sulfides or titaniumcarbonitrides could be evaluated from the same set of specimens.

5. Significance and Use

5.1 This practice is used to assess the indigenous inclusions or second-phase constituents in metals using extreme value statistics.

5.2 It is well known that failures of mechanical components, such as gears and bearings, are often caused by the presence of large nonmetallic oxide inclusions. Failure of a component can often be traced to the presence of a large inclusion. Predictions related to component fatigue life are not possible with the evaluations provided by standards such as Test Methods E45, Practice E1122, or Practice E1245. The use of extreme value statistics has been related to component life and inclusion size distributions by several different investigators (3-8). The purpose of this practice is to create a standardized method of performing this analysis.

5.3 This practice is not suitable for assessing the exogenous inclusions in steels and other metals because of the unpredictable nature of the distribution of exogenous inclusions. Other methods involving complete inspection such as ultrasonics must be used to locate their presence.

6. Procedure

6.1 Test specimens are obtained and prepared in accordance with E3, E45 and E768.

6.2 The microstructural analysis is to be performed using the types of equipment and image analysis procedures described in E1122 and E1245.

6.3 Determine the appropriate magnification to use for the analysis. For accurate measurements, the largest inclusion measured should be a minimum of 20 pixels in length. For specimens containing relatively large inclusions, objective lens having magnifications ranging from 10 to $20 \times$ will be adequate. Generally, for specimens with small inclusions, an objective lens of 32 to $80 \times$ will be required. The same magnification shall be used for all the specimens to be analyzed.

6.4 Using the appropriate calibration factors, calculate the area of the field of view observed by the image analysis

system, A_f . For each specimen, an area of 150 mm² shall be evaluated. Using Eq 1, the number of fields of view required to perform the analysis is $N_f = A_o / A_f = 150 / A_f$. N_f should be rounded up to the next highest integer value; that is, if N_f is calculated to be 632.31, then 633 fields of view shall be examined.

6.5 Image Analysis Measurements:

6.5.1 In this practice, feature specific parameters are measured for each individual inclusion. The measured inclusion lengths shall be based on a minimum of eight feret diameters.

6.5.2 For each field of view, focus the image either manually or automatically, and measure the maximum feret diameter of each detected oxide inclusion. The measured feret diameters are stored in the computer's memory for further analysis. This procedure is repeated until an area of 150 mm² is analyzed.

6.5.3 In situations where only a very few inclusions are contained within the inspected area, the specimen can first be observed at low magnification, and the location of the inclusions noted. The observed inclusions can then be remeasured at high magnification.

6.5.4 After the specimen is analyzed, using the accumulated data, the maximum feret diameter of the largest measured inclusion in the 150 mm^2 area is recorded. This procedure is repeated for each of the other five specimens.

6.5.5 The specimens are then repolished and the procedure is repeated until each specimen has been evaluated four times. This will result in a set of 24 maximum feret diameters. For each repolishing step, it is recommended that at least 0.3 mm of material be removed in order to create a new plane of observation.

6.5.6 The mean length, \overline{L} , is then calculated using Eq 10.

6.5.7 The standard deviation, Sdev, is calculated using Eq 11.

6.6 The 24 measured inclusion lengths are sorted in ascending order. An example of the calculations is contained in Appendix X1. The inclusions are then given a ranking. The smallest inclusion is ranked number 1, the second smallest is ranked number 2 etc.

6.7 The probability plotting position for each inclusion is based upon the rank. The probabilities are determined using Eq 9: $P_i = i / (N + 1)$. Where $1 \le i \le 24$, and N = 24.

6.8 A graph is created to represent the data. Plotting positions for the ordinate are calculated from Eq 8: $y_i = -\ln(-\ln(P_i))$. The variable y in this analysis is referred to as the Reduced Variate (Red. Var.). Typically the ordinate scale ranges from -2 through +7. This corresponds to a probability range of inclusion lengths from 0.87 through 99.9 %. The ordinate axis is labeled as Red. Var. It is also possible to include the Probability values on the ordinate. In this case, the ordinate can be labeled Probability (%). The abscissa is labeled as Inclusion Length (mm); the units of inclusion length shall be micrometers.

6.9 Estimation of the Extreme Value Distribution Parameters:

6.9.1 Several methods can be used to estimate the parameters of the extreme value distribution. Using linear regression to fit a straight line to the plot of the Reduced Variate as a 🕼 E2283 – 08 (2019)

function of inclusion length is the easiest method; however, it is the least precise. This is because the larger values of the inclusion lengths are more heavily weighted than the smaller inclusion lengths. Two other methods for estimating the parameters are the method of moments (mom), and the method of maximum likelihood (ML). The method of moments is very easy to calculate, but the method of maximum likelihood gives estimates that are more precise. While both methods will be described, the maximum likelihood method shall be used to calculate the reported values of δ and λ for this standard. (Since the ML solution is obtained by numerical analysis, the values of δ and λ obtained by the method of moments are good guesses for starting the ML analysis.)

6.9.2 *Moments Method*—It has been shown that the parameters for the Gumbel distribution, can be represented by:

$$\delta_{\rm mom} = \frac{\rm Sdev\,\sqrt{6}}{\pi} \tag{14}$$

and

$$\lambda_{\rm mom} = L - 0.5772 \cdot \delta_{\rm mom} \tag{15}$$

where the subscript mom indicates the estimates are based on the moment method.

6.9.3 Maximum Likelihood Method—This method is based on the approach that the best values for the parameters δ and λ are those estimates that maximize the likelihood of obtaining the measured set of inclusion lengths. Since the extreme value distribution is based on a double exponential function, the maximization process is easiest to perform on the log of the distribution function. That is for the given set if measurements:

$$LL = \sum_{i=1}^{n} \ln(f(x_i, \lambda, \delta))$$
(16)

 $=\sum_{i=1}^{n}\ln\left(\frac{1}{\delta}\right) - \left(\frac{x_i - \lambda}{1+\delta}\right) - \exp\left(-\frac{x_i - \lambda}{1+\delta}\right) + \exp\left($

The maximization of LL is best performed by numerical analysis. This can be done via a spreadsheet or an appropriate computer analysis program. The values of δ and λ that are determined from Eq 17 are referred to as δ_{ML} and λ_{ML} . An example of the maximization process is described in Appendix X1. Having determined the best estimates for δ_{ML} and λ_{ML} , it follows that:

$$x = \delta_{\rm ML} ({\rm Red. \, Var.}) + \lambda_{\rm ML}$$
(18)

or

$$x = \delta_{\rm ML} \ln(-\ln(P)) + \lambda_{\rm ML}$$
(19)

In terms of the return period:

$$x = -\delta_{\rm ML} \ln \left(-\ln \left(\frac{T-1}{T} \right) \right) + \lambda_{\rm ML}$$
(20)

6.9.4 *Outlying Observations*—Practice E178 shall be used to deal with outlying observations. As applied to this standard, an upper significance of 1 % shall be the governing criterion. The recommended criteria for single sample rejections is described in Section 4 of Practice E178. If a data point is concluded to be an outlier, then in accordance with Practice E178, section 2.3, it shall be rejected. The specimen containing

the outlier shall then be repolished, and the analysis repeated. Examples of outlier calculations are described in Appendix X1.

6.9.5 The standard error, SE, for any inclusion of length x based upon the ML method is:

$$SE(x) = \delta_{\rm ML} \cdot \sqrt{(1.109 + 0.514 \cdot y + 0.608 \cdot y^2)/n}$$
(21)

6.9.6 95 % *Confidence Intervals*—In practice, very large return periods are used in predicting how large an inclusion will be present is a particular area of steel. Thus the results of the extreme value analysis shall be presented with confidence limits. The approximate 95 % confidence intervals are:

$$95\% CI = \pm 2 \cdot SE(x) \tag{22}$$

6.10 Predicted Longest Inclusion, L_{max} —The return period is used to predict how large an inclusion would be expected to be found if an area much greater than A_o were to be examined. As previously defined, 3.2.15, this area is referred to as $A_{ref} =$ 150 000 mm². Thus using the calculated values of δ_{ML} and λ_{ML} from the maximum likelihood method, Eq 17, and P = 0.999, L_{max} is calculated.

6.11 *Comparison of Different Lots of Steel*—Using the methodology described herein, the following procedure can be used to compare the differences in sizes of large nonmetallic inclusions in two steels designated A and B.

6.11.1 For steel A, δ_A , λ_A , are calculated from Eq 17. The SE for steel A is calculated based upon the value of L_{max} for steel A by using Eq 21. The same parameters are calculated for steel B.

6.11.2 The approximate 95 % confidence interval for L_{max} (A) – L_{max} (B) is:

$$CI = L_{max}(A) - L_{max}(B) \pm 2 \cdot \sqrt{SE_{ref}(A)^2 + SE_{ref}(B)^2}$$
(23)

6.11.3 If the lower to upper bounds of the 95 % CI include 0, then conclude that there is no difference in the characteristic sizes of the largest inclusions in heat A and B. 082010

6.11.4 If the value 0 is less than the bounds of the confidence interval, then conclude that characteristic size of the largest inclusion in heat A is greater than that in heat B.

6.11.5 If the value 0 is greater than the bounds of the confidence interval, then conclude that characteristic size of the largest inclusion in heat B is greater than that in heat A.

7. Report

7.1 The report shall consist of a graphical representation of the data, information discussing how the data was measured and the results of the statistical analysis.

7.2 The graphical analysis shall contain the data points used for the analysis, the best-fit line as determined by the maximum likelihood method, and the 95 % confidence intervals for the data. The ordinate of the graph may be the Reduced Variate or the probability values. The abscissa will be Inclusion Length in micrometers. The control area, A_0 shall be included on the graph.

7.3 For this practice, the accompanying report shall contain the following:

7.3.1 Name of the person performing the analysis.

- 7.3.2 Date the analysis was completed.
- 7.3.3 Material Type.

7.3.4 Specimen location and size of material.

7.3.5 Microscope objective magnification.

- 7.3.6 Image Analysis Calibration Constant.
- 7.3.7 A_f [µm²].
- 7.3.8 A_o [µm²].
- 7.3.9 N_f
- 7.3.10 Ľ.
- 7.3.11 Sdev.
- 7.3.12 δ_{ML} (to 3 decimal places).
- 7.3.13 λ_{ML} (to 3 decimal places).
- 7.3.14 L_{max}.

7.4 The length of any outlier measurements that were rejected shall be reported.

7.5 When possible, the report should contain the steel Oxygen, Silicon, Aluminum and Calcium contents.

7.6 Any other information deemed necessary shall be based upon purchaser-producer agreements.

8. Precision and Bias

8.1 *Interlaboratory Test Program*—Interlaboratory Test study was conducted using heat treated 4140 calcium treated steel. This material, having a low sulfur content, was selected so that all of the large inclusions contained in the steel would be oxides or oxisulfides. The chemical analysis of the alloy in weight percent is listed in Table 1.

8.1.1 Complete instructions for completing the testing program and a detailed analysis of the test results have been previously reported (9). A total of 19 laboratories participated in the program. Each laboratory prepared the specimens in accordance with the instructions provided as well as in accordance with the procedures listed in this practice and Guides E3, and E768 and Test Method E45. The largest inclusion on each of 24 polishing planes of 150 mm² was measured and recorded. Inclusion measurements were made by either Image analysis or manual methods in accordance with the standard. The inclusions were ranked from the smallest to the largest. The mean and standard deviations of the measured inclusions was calculated. In addition, the parameters associated with the extreme value distribution of the inclusions were calculated.

8.2 *Precision*—The test results were analyzed in accordance with Practice E691. By using this practice, statistical information regarding the test method can be obtained. In particular to evaluate the consistency of the data obtained in the interlaboratory study, two statistics are used. The "*k*-value" is used to examine the consistency of the within-laboratory precision - *Repeatability*. The "*h*-value" is used to examine the consistency of the test results from laboratory to laboratory - *Reproducibility*.

TABL	E 1	4140	Ca4	Steel	Composition
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		•	
С	0.40	S	0.001
Mn	0.85	AI	0.031
Si	0.30	Ti	0.004
Cr	1.06	Ca	16 ppm
Ni	0.11	0	5 ppm
Мо	0.23	Ν	76 ppm

8.2.1 Data from one laboratory was immediately rejected because the investigator was not able to properly prepare the specimens, and was not sure the Image Analysis system was properly calibrated when performing the test. A preliminary analysis of the results indicated that another laboratory seemed to have mean values of inclusion lengths that were significantly greater than the critical values of both the h and k statistics. It was later determined that this laboratory did not perform the test in accordance with the furnished instructions. Since this laboratory did not wish to repeat the tests, their results were discarded. Thus the testing program was based on the results obtained from 17 laboratories. For the h-statistic, the results from all the laboratories were below the critical value, Fig. 1. With regard to the k-statistic, two laboratories were slightly above the critical level, dotted line, Fig. 2.

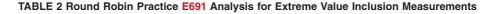
8.2.2 While two labs slightly exceeded the critical value for the repeatability statistic, k, the overall test results for this portion of the analysis are considered to be successful. There are several reasons for this conclusion. Unlike most round robin testing programs, more than one procedure or operation was required to perform the test. First the specimens that were provided to the participants had to be sectioned and mounted. Second, the specimens had to be metallographically prepared by each participant four times. For steel specimens containing calcium-rich inclusions, sample preparation can be challenging; particularly, if the laboratories are not experienced in preparing these types of specimens. Third, the inclusions had to be measured by either manual means or by using an Image Analysis system. Fourth, the standard requires that a measurement magnification of 200X or higher be used for the measurements. Some bias could possibly be introduced when comparing measurements made at 200X to those made at 500X. There are more possible sources of variation of the test results in this round robin since multiple operations are required to create the final test result.

8.3 *Extreme Value Distribution Parameters*—After performing the 24 inclusion measurements as required by the standard, the values of the location parameter, λ , and the scaling parameter, δ , are calculated using Eq 17 for the maximum likelihood method. The values of λ and δ are used to construct the best-fit line through the data points using Eq 18. Similarly the 95 % confidence bands for the data set are calculated using Eq 21 and Eq 22.

8.4 Comparing Predicted Results:

8.4.1 One of the main reasons for developing this standard is to be able to use the results of the analysis to compare different heats of steel. The method of performing this comparison is to use a specific probability position to predict how large an inclusion can be expected to be found in the steel. For this standard, the predicted probability value is 99.9%. The comparison between two different heats is based on the predicted size of the L_{max}. (P = 99.9%) inclusion in each heat and the 95% confidence interval associated with each of the extreme value distributions, equation 23. For the round robin test, each disk used to create the six metallographic specimens came from the same bar of steel. Thus, within statistical error, the results obtained by each laboratory should be the same. The smallest predicted L_{max}. inclusion was 58.93 µm from Lab E,

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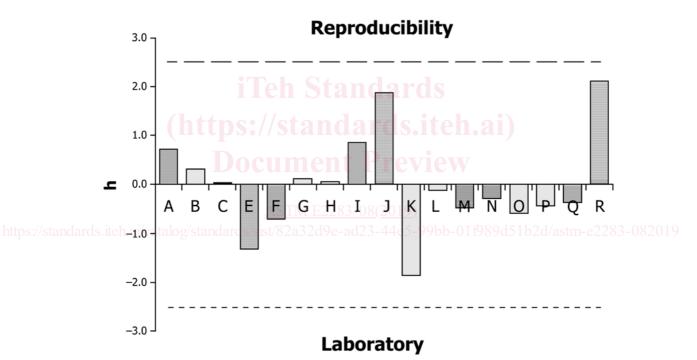


Lab	n	Mean	Stdev.	Dev. avg	h	K
A	24	37.50	11.31	4.69	0.72	1.04
В	24	34.85	15.14	2.04	0.31	1.39
С	24	32.99	9.25	0.18	0.03	0.85
E	24	24.29	6.39	-8.52	-1.31	0.59
F	24	28.25	6.99	-4.56	-0.70	0.64
G	24	33.57	10.68	0.76	0.12	0.98
Н	24	33.20	15.15	0.38	0.06	1.39
I	24	38.37	14.52	5.56	0.85	1.34
J	24	45.07	14.31	12.26	1.88	1.32
К	24	20.74	11.77	-12.08	-1.86	1.08
L	24	32.07	5.99	-0.74	-0.11	0.55
Μ	24	29.71	9.50	-3.11	-0.48	0.87
N	24	31.08	9.59	-1.73	-0.27	0.88
0	24	29.09	9.83	-3.72	-0.57	0.90
Р	24	30.03	8.00	-2.79	-0.43	0.74
Q	24	30.45	9.97	-2.37	-0.36	0.92
R	24	46.57	9.97	13.76	2.11	0.92
Number of Laboratories =17			Number o	of tests = 24		
Lab Avg	. = 32.81					
Sr =	10.87	r =	30.42			
SR =	12.47	R =	34.91			

h crit = 2.51

34.91





The dotted lines are the critical values

FIG. 1 Practice E691 Analysis, h Statistic for Inclusion Extreme Value Analysis

Table 3. The longest predicted L max. inclusion was 114.7 µm from Lab J, Table 3. The corresponding standard errors were 6.43 and 13.01 respectively.

8.4.2 95% Confidence Interval-Using the test criteria described by Eq 23, a 95 % Confidence Interval, it is found that the value of the confidence interval ranges from -85 to -25. Since this interval does not contain zero, statistically the results suggest the steels were from different heats.

8.4.3 Based on the round robin test results, a confidence interval of 99.98% is required for the analysis to predict the steel specimens are from the same lot. This means that the coefficient appearing in Eq 23 should be 3.8 and not 2.0, that is;

$$CI = L_{max}(A) - L_{max} \pm 3.8 \cdot \sqrt{SE_{ref}(A)^2 + SE_{ref}(B)^2}$$
(24)