Designation: E2555 – $21^{\epsilon 1}$

An American National Standard

Standard Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection¹

This standard is issued under the fixed designation E2555; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ε) indicates an editorial change since the last revision or reapproval.

ε¹ NOTE—Editorial corrections were made to the Terminology section in January 2022.

1. Scope

1.1 This practice presents a procedure and related tables of factors for adapting Practice E2234 (equivalent to MIL-STD-105) sampling plans to acceptance sampling inspection when the item quality of interest is life length or reliability. Factors are provided for three alternative criteria for lot evaluation: mean life, hazard rate, and reliable life. Inspection of the sample is by attributes with testing truncated at the end of some prearranged period of time. The Weibull distribution, together with the exponential distribution as a special case, is used as the underlying statistical model.

- 1.2 A system of units is not specified by this practice.
- 1.3 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety, health, and environmental practices and determine the applicability of regulatory limitations prior to use.
- 1.4 This international standard was developed in accordance with internationally recognized principles on standardization established in the Decision on Principles for the Development of International Standards, Guides and Recommendations issued by the World Trade Organization Technical Barriers to Trade (TBT) Committee.

2. Referenced Documents

2.1 ASTM Standards:²

E456 Terminology Relating to Quality and Statistics

E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

E2586 Practice for Calculating and Using Basic Statistics

2.2 Other Documents:

MIL-STD-105E Sampling Procedures and Tables for Inspection by Attributes³

3. Terminology

- 3.1 Definitions:
- 3.1.1 The terminology defined in Terminology E456 applies to this practice unless modified herein.
- 3.1.2 acceptance quality limit (AQL), n—quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling.
- 3.1.2.1 *Discussion*—This definition supersedes that given in MIL-STD-105E.
- 3.1.2.2 Discussion—A sampling plan and an AQL are chosen in accordance with the risk assumed. Use of a value of AQL for a certain defect or group of defects indicates that the sampling plan will accept the great majority of the lots or batches provided the process average level of percent defective (or defects per hundred units) in these lots or batches are no greater than the designated value of AQL. Thus, the AQL is a designated value of percent defective (or defects per hundred units) for which lots will be accepted most of the time by the sampling procedure being used. The sampling plans provided herein are so arranged that the probability of acceptance at the designated AQL value depends upon the sample size, being generally higher for large samples than for small ones, for a given AQL. The AQL alone does not identify the chances of accepting or rejecting individual lots or batches but more directly relates to what might be expected from a series of lots or batches, provided the steps indicated in this refer to the operating characteristic curve of the plan to determine the relative risks.
- 3.1.3 *consumer's risk*, *n*—probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan.

¹ This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.40 on Reliability.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

³ MIL-STD-105E is also commonly referred to as "MIL-STD-105." It is virtually identical in content to its predecessor, MIL-STD-105D. These documents are out of print.

- 3.1.4 *double sampling plan, n*—a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot.

 E2234
- 3.1.5 *hazard rate*, n—differential fraction of items failing at time t among those surviving up to time t, symbolized by h(t).
- 3.1.5.1 *Discussion*—h(t) is also referred to as the instantaneous failure rate at time t. It is related to the probability density and cumulative distribution functions by h(t) = f(t) / (1 F(t)).
- 3.1.6 *limiting quality level (LQL)*, *n*—quality level having a specified consumer's risk for a given sampling plan.
- 3.1.7 *lot*, *n*—a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes.
- 3.1.7.1 *Discussion*—The lot for sampling may differ from a collection of units designated as a batch for other purposes, for example, production, shipment, and so forth.
- 3.1.8 multiple sampling plan, n—a sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples.

 E2234
- 3.1.8.1 *Discussion*—When the quality is much less or much more than the AQL, the decision can be made on the first sample, which is smaller than that of a single sampling plan with equivalent acceptance quality level. For samples that are close to the AQL in quality, additional samples are required and the total sample size will be larger than the corresponding single sampling plan.
- 3.1.9 *sample*, *n*—group of items, observations, test results, or portions of material taken from a large collection of items, observations, test results, or quantities of material that serves to

- provide information that may be used as a basis for making a decision concerning the larger collection. **E2586**
 - 3.2 Definitions of Terms Specific to This Standard:
- 3.2.1 acceptance number, n—the maximum number of failed items allowed in the sample for the lot to be accepted using a single or multiple sampling plan.
- 3.2.2 *mean life*, *n*—average time that items in the lot or population are expected to operate before failure.
- 3.2.2.1 *Discussion*—This metric is often referred to as mean time to failure (MTTF).
- 3.2.3 *rejection number, n*—the minimum number of failed items in the sample that will cause the lot to be rejected under a given sampling plan.
- 3.2.4 *reliable life* (ρ_r), n—life beyond which some specified proportion, r, of the items in the lot or population will survive.
- 3.2.5 *test truncation time* (*t*), *n*—amount of time sampled items are allowed to be tested.
- 3.2.6 *Weibull distribution, n*—probability distribution having cumulative distribution:

function
$$F(t) = 1 - \exp\left(-\left(\frac{t - \gamma}{\eta}\right)^{\beta}\right)$$
, $t > \gamma$ and probability density
$$function f(t) = \frac{\beta}{\eta} \left(\frac{t - \gamma}{\eta}\right)^{\beta - 1} \exp\left(-\left(\frac{t - \gamma}{\eta}\right)^{\beta}\right)$$

3.2.6.1 *Discussion*—The Weibull distribution is widely used for modeling product life. It can take a wide variety of shapes and also the characteristics of other types of distributions based on the value of its parameters. γ is called the location, minimum life, or threshold parameter and defines the lower limit of the distribution (Fig. 1). η is called the scale or characteristic life parameter and is equal to the 63.2 percentile

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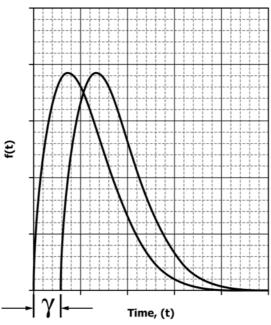


FIG. 1 Effect of the Parameter γ on the Weibull Probability Density Function, f(t)

of the distribution, minus γ (Fig. 2). β is the shape parameter (Fig. 3). The exponential distribution is the special case where $\gamma = 0$ and $\beta = 1$.

4. Significance and Use

- 4.1 The procedure and tables presented in this practice are based on the use of the Weibull distribution in acceptance sampling inspection. Details of this work, together with tables of sampling plans of other forms, have been published previously. See Refs (1-3).⁴ Since the basic computations required have already been made, it has been quite easy to provide these new factors. No changes in method or details of application have been made over those described in the publications referenced above. For this reason, the text portion of this report has been briefly written. Readers interested in further details are referred to these previous publications. Other sources of material on the underlying theory and approach are also available (4-7).
- 4.2 The procedure to be used is essentially the same as the one normally used for attribute sampling inspection. The only difference is that sample items are tested for life or survival instead of for some other property. For single sampling, the following are the required steps:
- 4.2.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234.
- 4.2.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.
- 4.2.3 Place the sample of items on life test for the specified period of time, *t*.
- 4.2.4 Determine the number of sample items that failed during the test period.
- ⁴ The boldface numbers in parentheses refer to the list of references at the end of this standard.

- 4.2.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.
- 4.2.6 If the number that failed is equal to or less than the acceptable number, accept the lot; if the number failing exceeds the acceptable number, reject the lot.
- 4.3 Both the sample sizes and the acceptance numbers used are those specified by Practice E2234 plans. It will be assumed in the section on examples that single sampling plans will be used. However, the matching double sampling and multiple sampling plans provided in MIL-STD-105 can be used if desired. The corresponding sample sizes and acceptance and rejection numbers are used in the usual way. The specified test truncation time, t, must be used for all samples.
- 4.4 The probability of acceptance for a lot under this procedure depends only on the probability of a sample item failing before the end of the test truncation time, *t*. For this reason, the actual life at failure need not be determined; only the number of items failing is of interest. Life requirements and test time specifications need not necessarily be measured in chronological terms such as minutes or hours. For example, the life measure may be cycles of operation, revolutions, or miles of travel.
- 4.5 The underlying life distribution assumed in this standard is the Weibull distribution (note that the exponential distribution is a special case of the Weibull). The Weibull model has three parameters. One parameter is a scale or characteristic life parameter. For these plans and procedures, the value for this parameter need not be known; the techniques used are independent of its magnitude. A second parameter is a location or "guaranteed life" parameter. In these plans and procedures, it is assumed that this parameter has a value of zero and that there is some risk of item failure right from the start of life. If this is not the case for some applications, a simple modification in procedure is available. The third parameter, and the one of

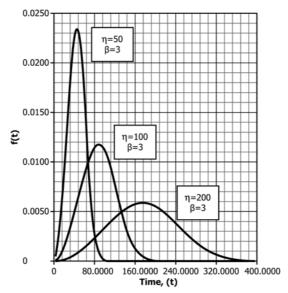


FIG. 2 Effect of the Parameter η on the Weibull Probability Density Function, f(t)



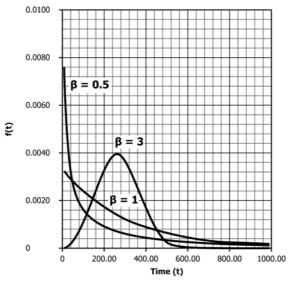


FIG. 3 Effect of the Parameter β on the Weibull Probability Density Function, f(t)

importance, is the shape parameter, β .⁵ The magnitude of the conversion factors used in the procedures described in this report depends directly on the value for this parameter. For this reason, the magnitude of the parameter shall be known through experience with the product or shall be estimated from past research, engineering, or inspection data. Estimation procedures are available and are outlined in Ref (1).

4.6 For the common case of random chance failures with the failure rate constant over time, rather than failures as a result of "infant mortality" or wearout, a value of 1 for the shape parameter shall be assumed. With this parameter value, the Weibull distribution reduces to the exponential. Tables of conversion factors are provided in Annex A1 for 15 selected shape parameter values ranging from ½ to 10, the range commonly encountered in industrial and technical practice. The value 1, used for the exponential case, is included. Factors for other required shape parameter values within this range may be obtained approximately by interpolation. A more complete discussion of the relationship between failure patterns and the Weibull parameters can be found in Refs (1-3).

4.7 One possible acceptance criterion is the mean life for items making up the lot (μ) . Mean life conversion factors or values for the dimensionless ratio $100t/\mu$ have been determined to correspond to or replace all the p' or percent defective values associated with Practice E2234 plans. In this factor, t represents the specified test truncation time and μ the mean item life for the lot. For reliability or life-length applications, these factors are used in place of the corresponding p' values normally used in the use of Practice E2234 plans for attribute inspection of other item qualities. The use of these factors will be demonstrated by several examples (see Sections 5, 7, and 9).

4.8 Annex Table 1A lists, for each selected shape parameter value, $100t/\mu$ ratios for each of the Practice E2234 AQL [p'(%)] values. With acceptance inspection plans selected in terms of these ratios, the probability of acceptance will be high for lots whose mean life meets the specified requirement. The actual probability of acceptance will vary from plan to plan and may be read from the associated operating characteristic curves supplied in MIL-STD-105. The curves are entered by using the corresponding p'(%) value. Annex Table 1B lists $100t/\mu$ ratios at the LQL for the quality level at which the consumer's risk is 0.10. Annex Table 1C lists corresponding $100t/\mu$ ratios for a consumer's risk of 0.05.

4.8.1 These ratios are to be used directly for the usual case for which the value for the Weibull location or threshold parameter (γ) can be assumed as zero. If γ is not zero but has some other known value, all that shall be done is to subtract the value for γ from t to get t_0 and from m to get m_0 . These transformed values, t_0 and m_0 , are then employed in the use of the tables and for all other computations. A solution in terms of m_0 and t_0 can then be converted back to actual or absolute values by adding the value for γ to each.

5. Examples, Mean Life Ratio

5.1 A Practice E2234 acceptance sampling inspection plan is to be applied to incoming lots of product for which the mean item life is the property of interest. An acceptable mean life of 2000 h has been specified, and under the plan, used lots with a mean life of this value or greater shall have a high probability of acceptance. A testing truncation time of t = 250 h has been specified. From past experience it has been determined that the Weibull distribution can be used as a life-length model and a shape parameter value of 2.5 and a location or threshold parameter value of 0 can be assumed. Single sampling is to be used. A sample of as many as 300 items or so can be tested at one time. An appropriate sampling inspection plan shall be

 $^{^{5}}$ In some disciplines, the Weibull shape β parameter is referred to as the "Weibull slope."



selected. Also, the consumer's risk under use of the selected plan shall be determined.

- 5.1.1 Computation of the $100t/\mu$ ratio at the AQL gives $100t/\mu = 100 \times 250/2000 = 12.5$. Examination of the ratios in the column for a shape parameter of 2.5 in Annex Table 1A discloses a value of 12.4 for an AQL of 0.40 in p'(%) terms. A plan with this AQL is accordingly to be used. Reference now to Practice E2234 indicates for Sample Size Code Letter M the sample size is 315; this value will accordingly be used. Examination of the Master Table for Normal Inspection (Single Sampling) in Practice E2234 shows for Sample Size Code Letter M and an AQL of 0.40, the acceptance number must be 3 and the rejection number 4.
- 5.1.2 The acceptance procedure will thus be to draw at random a sample of 315 items and submit them to life test for 250 h. At the end of that time, the number that has failed will be determined. If three items or less have failed, the lot will be accepted; if four or more have failed, it will be rejected.
- 5.1.3 The consumer's risk at a probability level of 0.10 can be determined by use of Annex Table 1B which gives $100t/\mu$ ratios at the LQL for the 0.10 risk value. For a shape parameter value of 2.5, a Sample Size Code Letter M, and an AQL of 0.40, the $100t/\mu$ ratio value is found to be 24. With t = 250, $100t/\mu = 24$ or $100 \times 250/\mu = 24$ which gives a value for μ of 1040. Thus, if the mean life for the items in the lot is 1040 h or less, the probability of acceptance will be 0.10 or less. If the lot quality for which the consumer's risk was 0.05 was desired instead, Annex Table 1C might be used which gives ratios at the LQL for this risk value.
- 5.2 A Practice E2234 plan with Sample Size Code Letter F and an AQL of 4.0 has been specified for a product for which life length in terms of cycles of operation is the quality of interest. Acceptance is to be in terms of a mean life evaluation. The Weibull distribution can be assumed to apply with a shape parameter value and a location parameter value of 0. Testing of sample items is to be truncated at 5000 cycles. The operating characteristics in terms of mean life for this plan are required.
- 5.2.1 Annex Table 1A lists ratios of $100t/\mu$ at selected AQLs and gives a $100t/\mu$ value of 0.62 for an AQL of 4.0 and a shape parameter value of 2/3. With t=5000, $100t/\mu=0.62$ or $100\times5000/\mu=0.62$ which gives $\mu=810\,000$. Therefore, if the mean item life for the lot is 810 000 or more, the probability of acceptance will be high. Annex Table 1C gives ratios $100t/\mu$ at the LQL for a consumer's risk of 0.05 and provides a $100t/\mu$ value of 14 for Code Letter F, an AQL of 4.0, and a shape parameter value of 2/3. Thus, $100\times5000/\mu=14$ or $\mu=36\,000$. If the mean item life for the lot is $36\,000$ cycles or less, the probability of acceptance will be 0.05 or less.
- 5.2.2 The sample size and acceptance number will be those specified by Practice E2234 for Code Letter F and an AQL of 4.0. For single sampling, the sample size will be 20 items and the acceptance number 2. For this example, as in all cases, the matched Practice E2234 double sampling and multiple sampling plans may be used instead. No additional changes in procedure are required. The specified test time, which in this case is 5000 cycles, shall be used for all samples.
- 5.3 Assume the Weibull distribution applies with a shape parameter value of β = 3.33 and a location or threshold

parameter value, γ , of 3000 h. A Practice E2234 acceptance-inspection plan shall be selected under which the probability of acceptance will be low (0.05 or less) if mean item life is 8000 h or less. The sample size will be kept large to reduce the testing period time but it cannot exceed 250 items. To reduce further testing time, an acceptance number of 0 will be used. The required test truncation time must be determined; also, the AQL.

- 5.3.1 Reference to Practice E2234 indicates the Code Letter L with a sample size of 200 items shall be used. With this code letter and an acceptance number of 0, the AQL in Practice E2234 terms must be 0.065. Subtraction of the threshold parameter value, γ , of 3000 h from the required mean value, μ , of 8000 h gives as a converted value for the mean $\mu_0 = 8000 3000 = 5000$ h. This converted value must now be used in working with the tables of factors. Use of Annex Table 1C for $\beta = 3\frac{1}{3}$ Code Letter L, and an AQL of 0.065 gives a $100t/\mu$ value of 31 at the LQL (for P(A) = 0.05). With $\mu_0 = 5000$, $100t_0/\mu_0 = 100 t_0/5000 = 31$ or $t_0 = 1550$ h. Conversion of this to absolute terms gives $t = t_0 + \gamma = 1550 + 3000 = 4550$ h as the required test truncation time.
- 5.3.2 From Annex Table 1A, the corresponding ratio at the AQL may be found. For an AQL of 0.065 and $b = 3\frac{1}{3}$ it is 12.3. Thus, $100 \ t_0/\mu_0 = 12.3$ or $100 \times 1550/\mu_0 = 12.3$ or $\mu_0 = 12$ 600. Converting this to absolute terms gives $\mu = \mu_0 + \gamma = 12$ 600 + 3000 = 15 600. Thus, the mean item life for a lot shall be 15 600 h or more for its probability of acceptance to be high.

6. Hazard Rate Conversion Factors

- 6.1 Another measure of lot quality is the hazard rate or instantaneous failure rate, h(t), at some specified period of time, t. Hazard rate conversion factors or values for the dimensionless product $100t\{h(t)\}$ have been determined for all of the p' values that characterize the collection of Practice E2234 plans. As for the mean life plans, these products may be used in place of the corresponding p' values when using the Practice E2234 plans for life-length and reliability applications.
- 6.2 Annex Table 2A lists for each selected value for the shape parameter $100t\{h(t)\}$ products for each Practice E2234 AQL value. Annex Table 2B lists corresponding $100t\{h(t)\}$ products at the LQL for a consumer's risk of 0.10. Annex Table 2C lists products at the LQL for a consumer's risk of 0.05. Use of these tables of factors is similar to the method of use for the mean life ratios including the variation in method required when some nonzero value for the location or threshold parameter shall be assumed.
- 6.2.1 Note one point of difference. The products are for direct application only in cases in which the time t at which the hazard rate is specified or is to be evaluated is the same as the time t at which the life testing of sample items is to be truncated. However, a table of hazard rate ratios has been prepared, Annex Table 2D, to use in a simple modification of method that allows the test truncation time to differ from the time at which the hazard rate is specified. All that shall be done is to determine the hazard rate at the test truncation time which corresponds to the hazard rate at the specification time. Annex



Table 2D provides ratios for making this conversion. It gives for various values of t_2/t_1 the corresponding values for the ratio $h(t_2)/h(t_1)$ for all the shape parameter values for which conversion values have been provided. If the test truncation time is shorter than the time for hazard rate specification, t_1 is used to represent the test truncation time and $h(t_1)$ the corresponding hazard rate at that time. In this case, t_2 represents the time of hazard rate specification and $h(t_2)$ the specified hazard rate. If the test truncation is longer instead, the meanings given Subscripts 1 and 2 are simply reversed.

7. Examples, Hazard Rate

7.1 An acceptance-inspection plan shall be selected from the Practice E2234 collection for an application for which the Weibull distribution applies and for which it may be assumed the shape parameter value is 1.67 and the location parameter value is 0. A hazard rate of no more than 0.0005/h at 1000 h of life can be tolerated so a plan under which the probability of acceptance will be low (0.10) if this rate will be exceeded at this life is required. The test truncation time is likewise to be 1000 h.

7.1.1 Computation of the $100t\{h(t)\}$ product gives $100 \times 1000 \times 0.0005 = 50$. Thus, apian shall be used for which this product is found at the LQL for which the consumer's risk is 0.10. Examination of the column for $\beta = 1.67$ in Annex Table 2B discloses several close possibilities. One is for a plan with Code Letter D and an AQL of 1.5 for which the product is 48; another is Code Letter F and an AQL of 4.0 for which the product is likewise 48; still another is Code Letter G and an AQL of 6.5 for which the product is 53. Any of these will provide fairly closely the required consumer's protection.

7.1.2 The last plan mentioned with its relatively large sample size and acceptance number will discriminate most sharply between good and bad lots and hence provide the most reasonable AQL. This will be achieved at the expense of a relatively large number of item hours of inspection, of course. With this choice (Code Letter G and an AQL of 6.5) the AQL can be easily determined. Reference to Annex Table 2A gives a value for $100t\{h(t)\}$ of 11.2 for an AQL of 6.5. Thus, $100 \times 1000 \ h(t) = 11.2$ or $h(t) = 0.000 \ 112$ at t = 1000; the "acceptable" hazard rate is therefore $0.000 \ 112$ (per hour). If, alternatively, Code Letter D and an AQL of 1.5 had been used, the "acceptable" hazard rate would be $0.000 \ 025 \ 2$ (per hour) instead.

7.2 Suppose the selected sampling plan must have an acceptable hazard rate (a rate for which the probability of acceptance is high) of 0.0001 per hour at 500 h of life. However, the testing of sample items shall be truncated at 200 h. A value of $\beta = 0.67$ and a location parameter of 0 can be assumed. A Practice E2234 plan shall be selected.

7.2.1 In this case, use Annex Table 2D. Letting $t_2 = 500$ and $t_1 = 200$, $t_2/t_1 = 500/200 = 2.5$. Referencing Annex Table 2D with this ratio using the value $\beta = 0.67$ column shows $h(t_2)/h(t_1)$ to be 0.734. With $h(t_2) = 0.0001$, $0.0001/h(t_1) = 0.734$, or $h(t_1) = 0.000136$. This failure rate number shall be used in selecting the plan. Thus, $100t\{h(t)\} = 100 \times 200 \times 0.000136 = 2.72$ (note that the testing truncation time of 200 h is used as t at this point). Referencing Annex Table 2A examining the

column for $\beta = 0.67$ shows that a Practice E2234 plan with an AQL of 4.0 % precisely meets this need.

8. Reliable Life Conversion Factors

8.1 A third possible reliability and life-length measure for the items in a lot or population is reliable life (ρ). Reliable life can be defined as the life beyond which some specified proportion of the items in the lot or population will survive. The letter r represents this specified proportion.

8.1.1 Tables of conversion factors have been prepared for two different proportions, r = 0.90 and r = 0.99. As for the mean life case, these reliable life conversion factors have been prepared in the form of values for the dimensionless ratio $100t/\rho$. Ratio values have been determined for all the p'(%)values associated with Practice E2234 plans. Annex Table 3A gives $100t/\rho$ values at each of the AQLs for r = 0.90; Annex Table 4A gives corresponding values for r = 0.99. Annex Table 3B gives ratio values at the LQL for a consumer's risk of 0.10 for r = 0.90; Annex Table 4B gives corresponding values for a consumer's risk of 0.10 and r = 0.99. Annex Table 3C gives ratio values at the LQL for a consumer's risk of 0.05 and r = 0.90; Annex Table 4C gives similar ratio values at a consumer's risk of 0.05 and r = 0.99. These conversion ratios are used in the same manner in which mean life ratios are used, including the manner for application when the location parameter is not zero. See Section 9 for an example.

9. Examples, Reliable Life

9.1 A sampling inspection plan shall be selected for a product for which item life in terms of feet of travel is the quality of interest. Experience indicates the Weibull distribution will serve well as a statistical model with a shape parameter value of approximately $1\frac{1}{3}$ and a location parameter of 0. A lot will be considered "acceptable" if the reliable life is 40 000 ft and the probability of acceptance for such lots shall be high. For lots in which reliable life is 10 000 ft or less, the probability of acceptance shall be low, namely 0.05 or less. Reliable life is defined as the life beyond which 90 % of the items will survive; that is, r is to be 0.90. Testing of sample items is to be truncated at 5000 ft.

9.1.1 At the AQL, the 100t/p factor is $100 \times 5000/40~000 = 12.5$. Examination of Annex Table 3A shows that for $\beta = 1\frac{1}{3}$ the 100t/p ratio for an AQL of 0.65 is 12.4 which is quite close to the desired ratio. Accordingly, a plan with this AQL is to be adopted. At the unacceptable or LQL, the $100t/p_r$ factor is $100 \times 5000/10~000 = 50$. Referencing Annex Table 3C, which gives ratios at the LQL for P(A) = 0.05, shows that, for Code Letter L, an AQL of 0.65 (which is required for this application, as indicated above) and $\beta = 1\frac{1}{3}$ the corresponding ratio is 48, which is close to the desired value of 50. Thus, a Practice E2234 plan with Code Letter L and an AQL of 0.65 will meet the specified operating requirements. For single sampling, Practice E2234 shows the sample size to be 200 items and the acceptance number 3.

10. Summary

10.1 This practice preserves the structure of TR-7 for use in applications in which that standard is prescribed or its use is desirable.

- 10.2 This practice provides tables and procedures for applying three different measures of reliability in which testing is performed without replacement.
 - 10.2.1 *Mean Life*, µ—The expected life of the product.
- 10.2.2 *Hazard Rate,* h(t)—The instantaneous failure rate at some specified time, t.
- 10.2.3 *Reliable Life*, ρ_r —The life ρ beyond which some specified proportion r of the items in the population will survive.
 - 10.3 Procedure for Application:
- 10.3.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234 for normal inspection.
- 10.3.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.
- 10.3.3 Place the sample of items on life test for the specified period of time, t.
- 10.3.4 Determine the number of sample items that failed during the test period.
- 10.3.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.
- 10.3.6 If the number that failed is equal to or less than the acceptance number, accept the lot; if the number failing exceeds the acceptance number, reject the lot.
 - 10.4 Selection—Mean Life:
 - 10.4.1 Specify:
 - 10.4.1.1 Acceptable mean life, μ_0 .
 - 10.4.1.2 Unacceptable mean life, μ_1 .
 - 10.4.1.3 Test truncation time, t.
 - 10.4.1.4 Weibull shape parameter, β.

- 10.4.2 Compute the dimensionless ratio $100t/\mu_0$ from the specified μ_0 and t and enter Annex Table 1A under β . Locate the nearest value of $100t/\mu_0$ to that calculated and read the corresponding AQL.
- 10.4.3 Compute the dimensionless ratio $100t/\mu_1$ from the specified μ_1 and t and enter Annex Table 1B under β . Locate the nearest value of $100t/\mu_1$ corresponding to the AQL obtained in 10.4.2 and read the sample size code letter (use Annex Table 1C if a limiting quality with 5 % probability of acceptance is desired).
- 10.4.4 Obtain the sample size and acceptance number for the test from the Practice E2234 normal inspection plan.
 - 10.4.5 Mean Life Example:
- 10.4.5.1 Suppose $\mu_0 = 50$, $\mu_1 = 10$, t = 5, $\beta = 1$, then $100t/\mu_0 = 10$ giving an AQL of 10 from Annex Table 1A and $100t/\mu_1 = 50$ giving Code F from Table 1B.
- 10.4.5.2 Practice E2234 gives sample size 20. Accept on 5 for Code F, AQL = 10.
 - 10.5 Selection—Hazard Rate or Reliable Life:
- 10.5.1 The selection of plans for a specified hazard rate or reliable life follows the procedure for mean life described in 10.4 using appropriate dimensionless ratios and the associated tables from Annex A1.
- 10.5.2 Hazard rate uses the product $100t\{h(t)\}$ with the Annex A1 tables of Section B.
- 10.5.3 Reliable life uses the dimensionless ratio 100t/ρ with the Annex A1 tables of Section C.

11. Keywords

11.1 exponential distribution; hazard rate; mean life; MIL-STD-105; reliability; reliable life; Weibull distribution

ASTM E2555-21e1

https://standards.iteh.ai/catalog/standards/sist/7e3edc ANNEX1-4e3f-a31c-b6f98962edb2/astm-e2555-21e1

(Mandatory Information)

A1. TABLES OF CONVERSION FACTORS

TABLE 1A

100t/μ Ratios at the Acceptable Quality Level (normal inspection) for the ASTM E2234 Plans

Note—These plans assume the characteristic being measured has a Weibull distribution.

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL							Shap	e Parame	ter, β						
p'(%)	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.010	1.67E-11	5.00E-07	7.52E-05	1.00E-02	0.109	0.239	0.446	1.128	2.831	5.198	7.031	7.999	11.033	17.262	41.847
0.015	5.63E-11	1.13E-06	1.38E-04	1.50E-02	0.147	0.313	0.568	1.382	3.330	5.950	7.940	8.981	12.210	18.720	43.578
0.025	2.61E-10	3.13E-06	2.97E-04	2.50E-02	0.216	0.440	0.772	1.784	4.085	7.055	9.255	10.393	13.873	20.734	45.863
0.040	1.07E-09	8.00E-06	6.02E-04	4.00E-02	0.308	0.601	1.024	2.257	4.930	8.252	10.657	11.887	15.603	22.778	48.070
0.065	4.58E-09	2.11E-05	1.25E-03	6.50E-02	0.443	0.831	1.370	2.877	5.986	9.702	12.328	13.656	17.617	25.101	50.462
0.100	1.67E-08	5.01E-05	2.38E-03	0.100	0.612	1.108	1.774	3.569	7.113	11.200	14.030	15.445	19.622	27.360	52.684
0.150	5.64E-08	1.13E-04	4.38E-03	0.150	0.830	1.452	2.263	4.372	8.366	12.822	15.845	17.344	21.716	29.673	54.866
0.250	2.61E-07	3.13E-04	9.42E-03	0.250	1.218	2.042	3.076	5.645	10.265	15.205	18.472	20.072	24.677	32.868	57.744
0.400	1.07E-06	8.03E-04	1.91E-02	0.401	1.733	2.795	4.080	7.144	12.391	17.788	21.274	22.962	27.759	36.113	60.527



TABLE 1A

100t/µ Ratios at the Acceptable Quality Level (normal inspection) for the ASTM E2234 Plans

 $\label{thm:note-thm$

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL		Shape Parameter, β													
p'(%)	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.650	4.62E-06	2.13E-03	3.96E-02	0.652	2.497	3.867	5.464	9.112	15.055	20.922	24.619	26.388	31.352	39.806	63.547
1.000	1.69E-05	5.05E-03	7.58E-02	1.005	3.454	5.159	7.083	11.312	17.899	24.167	28.031	29.859	34.932	43.402	66.356
1.500	5.75E-05	1.14E-02	0.140	1.511	4.690	6.771	9.047	13.872	21.071	27.687	31.680	33.551	38.683	47.092	69.119
2.500	2.70E-04	3.20E-02	0.303	2.532	6.906	9.551	12.330	17.954	25.901	32.883	36.983	38.879	44.008	52.211	72.778
4.000	1.13E-03	8.33E-02	0.620	4.082	9.882	13.133	16.422	22.798	31.355	38.559	42.682	44.565	49.591	57.446	76.339
6.500	5.06E-03	0.226	1.311	6.721	14.362	18.311	22.149	29.253	38.275	45.530	49.569	51.388	56.174	63.469	80.242
10.000	1.95E-02	0.555	2.573	10.536	20.122	24.711	29.007	36.626	45.816	52.891	56.726	58.431	62.856	69.441	83.932

TABLE 1B

100t/ μ Ratios at the Limiting Quality Level for the ASTM E2234 Plans, Consumer's Risk = 0.10

Note—These plans assume the characteristic being measured has a Weibull distribution.

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL							:	Shape Par	ameter, β						
Letter	(p%)	0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
Α	6.500	25.433	66.274	92.927	115.129	120.933	121.682	121.789	121.073	119.240	117.369	116.235	115.707	114.281	112.025	106.605
В	4.000	7.536	29.455	50.583	76.753	89.223	92.861	95.489	98.856	101.388	102.531	102.922	103.050	103.265	103.299	102.369
С	2.500	1.628	10.604	23.509	46.052	60.826	66.059	70.282	76.573	82.650	86.478	88.298	89.056	90.885	93.267	97.271
С	10.000	11.235	38.440	61.762	87.681	98.590	101.478	103.429	105.659	106.932	107.183	107.115	107.045	106.759	106.086	103.741
D	1.500	0.397	4.142	11.616	28.782	42.756	48.289	53.012	60.537	68.485	73.938	76.686	77.865	80.809	84.899	92.805
D	6.500	2.361	13.587	28.313	52.129	66.752	71.750	75.709	81.469	86.852	90.126	91.644	92.267	93.745	95.608	98.484
D	10.000	7.688	29.850	51.091	77.265	89.669	93.274	95.871	99.185	101.658	102.759	103.128	103.247	103.437	103.437	102.437
Е	1.000	9.26E-02	1.569	5.608	17.712	29.707	34.937	39.615	47.489	56.397	62.890	66.292	67.780	71.573	77.043	88.407
Е	4.000	0.505	4.859	13.094	31.175	45.395	50.930	55.614	63.003	70.708	75.933	78.546	79.662	82.439	86.266	93.549
E	6.500	1.478	9.943	22.401		59.376		68.939	75.352	81.594	85.556	87.450	88.241	90.157	92.669	96.959
Е	10.000	3.379	17.255	33.871		73.011		81.336	86.486	91.104	93.789	94.989	95.471	96.588	97.920	99.668
F	0.650	2.54E-02		2.939		21.505		30.592	38.287	47.470	54.478	58.255	59.930	64.265	70.683	84.679
F	2.500	0.133	1.992	6.709		32.495		42.562	50.415	59.160	65.448	68.714	70.136	73.745	78.908	89.471
httEs://	4.000	0.369	3.940	11.189		41.963		52.224	59.786	67.805	73.325	76.114	77.312	80.306	84.476	92.574
F	6.500	0.795	6.577	16.430		50.850		60.899	67.954	75.120	79.860	82.193	83.182	85.617	88.916	94.975
F	10.000	2.566	14.362	29.516		68.156		76.980	82.608	87.821	90.964	92.410	93.001	94.398	96.140	98.758
G	0.400	6.21E-03		1.452	7.196	15.117		23.075	30.268	39.334	46.578	50.594	52.399	57.141	64.341	80.792
G	1.500	3.14E-02		3.266		22.670		31.911	39.657	48.825	55.770	59.498	61.147	65.405	71.684	85.277
G		8.46E-02		5.358		29.038		38.900	46.773	55.716	62.257	65.691	67.194	71.032	76.576	88.139
G	4.000	0.176	2.407	7.730		34.879		45.043	52.852	61.437	67.540	70.688	72.053	75.506	80.412	90.319
G	6.500	0.524	4.981	13.339		45.818		56.028	63.393	71.059	76.246	78.837	79.944	82.694	86.479	93.665
G	10.000	1.201	8.658	20.194	41.613	56.374		66.136	72.790	79.367	83.606	85.654	86.514	88.611	91.395	96.290
Н	0.250	1.63E-03		0.743	4.605	10.817		17.654	24.215	32.904	40.140	44.254	46.126	51.108	58.847	77.265
Н	1.000	8.09E-03		1.657	7.859	16.150		24.329	31.633	40.747	47.967	51.950	53.737	58.414	65.486	81.507
Н	1.500	2.14E-02		2.694	10.865	20.592		29.548	37.194	46.384	53.437	57.252	58.947	63.342	69.869	84.191
H	2.500	4.36E-02		3.849		24.613		34.081	41.892	51.014	57.846	61.487	63.093	67.223	73.274	86.217
H	4.000	0.125	1.912	6.505		31.996		42.039	49.898	58.675	65.000	68.290	69.724	73.366	78.583	89.286
H	6.500	0.273	3.222	9.621		38.912		49.164	56.852	65.130	70.906	73.850	75.121	78.311	82.793	91.647
H	10.000	0.680	5.928	15.199		48.908		59.030	66.212	73.575	78.490	80.922	81.956	84.512	87.997	94.483
J	0.150	3.97E-04			2.878		10.404	13.316	19.143	27.264	34.319	38.434	40.330	45.442	53.568	73.718
J	0.650	1.95E-03		0.814	4.893	11.320		18.308	24.960	33.711	40.959	45.066	46.932	51.889	59.565	77.735
J	1.000	5.10E-03		1.316	6.738	14.390		22.183	29.290	38.314	45.569	49.606	51.425	56.210	63.501	80.262
J		1.03E-02		1.868	8.513	17.147		25.523 31.322	32.922	42.070	49.262	53.211	54.977	59.593	66.541	82.161
J	2.500 4.000	2.86E-02 6.09E-02		3.117 4.547	11.974	22.148 26.752		36.430	39.046 44.285	48.222 53.332	55.196 60.029	58.946 63.571	60.607 65.128	64.899 69.116	71.240 74.920	85.013 87.180
J	6.500	0.145	2.119	7.025	20.584			43.353			66.120		70.753	74.312	79.393	89.745
J	10.000	0.143	3.832	10.956		41.525		51.787	51.194 59.369	59.891 67.426	72.984	69.349 75.795	70.753	80.026	84.240	92.444
J V	0.100	1.04E-04			1.842	5.440	7.726	10.188	15.315	22.807	29.575	33.618	35.502	40.645	48.994	70.500
K K	0.100	5.08E-04			3.124	8.086	10.989	13.988	19.945		35.270	39.392	41.287	46.384		74.325
K	0.400	1.32E-039			4.292	10.261		16.925	23.378	28.174 31.991	39.210	43.330	45.209	50.217	54.454 58.025	74.325 76.724
K		2.64E-03		0.669	5.410	12.206		19.445	26.246	35.094	42.354	46.445	48.299	53.208	60.774	78.520
K		7.24E-03		1.568	7.573	15.707		23.793	31.052	40.147	47.378	51.376	53.170	57.875	65.002	81.205
K		1.52E-02		2.270	9.692	18.900		27.590	35.129	44.311	51.439	55.323	57.054	61.558	68.290	83.234
K	4.000	3.54E-02		3.465	12.849	23.351		32.675	40.447	49.602	56.509	60.206	61.840	66.054	72.252	85.614
K		8.31E-02		5.312		28.913		38.765	46.638	55.588	62.137	65.577	67.084	70.929	76.488	88.088
	0.500	0.01L-02	1.700	0.012	17.004	20.313	04.100	50.705	70.000	33.300	02.107	00.011	07.004	10.323	, 0.400	00.000



TABLE 1B

 $100t\!/\!\mu$ Ratios at the Limiting Quality Level for the ASTM E2234 Plans, Consumer's Risk = 0.10

Note—These plans assume the characteristic being measured has a Weibull distribution.

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL							Shape Par	rameter, β						
Letter	(p%)	0.333 0.5	50 0.66	7 1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
K	10.000	2.51E-01 3.0	9.23	4 24.700	38.122	43.608	48.363	56.079	64.420	70.262	73.247	74.535	11.111	82.341	91.396
L	0.065	2.54E-056.63I			3.824	5.648	7.684	12.107	18.898	25.286	29.197	31.041	36.139	44.598	67.263
L	0.250	1.24E-041.90I			5.677	8.025	10.541	15.756	23.331	30.141	34.196	36.083	41.226	49.553	70.902
L	0.400	3.19E-043.58I			7.196	9.907	12.742	18.454	26.476	33.490	37.597	39.493	44.616	52.787	73.179
L	0.650	6.35E-045.66I			8.550	11.548	14.627	20.701	29.026	36.156	40.281	42.174	47.255	55.271	74.880
L	1.000	1.73E-03 0.1				14.419	17.863	24.453	33.163	40.403	44.515	46.386	51.360	59.079	77.417
L	1.500	3.58E-03 0.1			13.176	16.961	20.673	27.619	36.556	43.819	47.889	49.728	54.583	62.027	79.325
L	2.500	8.23E-03 0.3				20.400	24.411	31.722	40.838	48.057	52.038	53.823	58.497	65.560	81.553
L	4.000	1.89E-02 0.5				24.552	28.840	36.450	45.640	52.722	56.562	58.270	62.705	69.307	83.851
L	6.500	5.50E-02 1.1			26.083	31.122	35.699	43.544	52.617	59.357	62.931	64.503	68.535	74.416	86.887
M M	0.040 0.150	6.51E-062.67			2.720	4.172 5.924	5.851	9.647	15.758	21.733	25.477	27.263	32.259	40.725 45.242	64.276
M	0.150	3.15E-057.65I 8.12E-051.44I			4.035 5.111	7.309	8.022 9.692	12.549 14.691	19.448 22.061	25.897 28.766	29.831 32.789	31.683 34.668	36.792 39.808	48.185	67.747 69.916
M	0.400	1.61E-042.27			6.069	8.515	11.119	16.472	24.176	31.047	35.120	37.011	42.153	50.443	71.535
M	0.400	4.36E-044.40I			7.780	10.619	13.564	19.440	27.601	34.672	38.790	40.686	45.793	53.898	73.944
M	1.000	8.99E-047.14			9.326	12.474	15.679	21.935	30.402	37.580	41.706	43.593	48.643	56.566	75.753
M	1.500	2.05E-03 0.1			11.454	14.975	18.481	25.157	33.924	41.174	45.279	47.143	52.093	59.753	77.857
M	2.500	4.65E-03 0.2			14.066	17.975	21.782	28.849	37.852	45.110	49.157	50.981	55.785	63.117	80.019
M	4.000	1.32E-02 0.4			18.265	22.674	26.846	34.338	43.511	50.664	54.572	56.316	60.861	67.671	82.856
N	0.025	1.63E-061.06I			1.923	3.066	4.435	7.657	13.099	18.631	22.180	23.891	28.740	37.130	61.374
N	0.100	7.87E-063.03I			2.852	4.352	6.078	9.957	16.162	22.197	25.965	27.760	32.774	41.243	64.684
N	0.150	2.02E-055.69I			3.611	5.367	7.340	11.654	18.329	24.651	28.535	30.370	35.455	43.922	66.751
N	0.250	4.01E-058.98I			4.286	6.250	8.418	13.063	20.082	26.600	30.558	32.418	37.538	45.974	68.293
N	0.400	1.08E-041.74I			5.490	7.788	10.261	15.407	22.917	29.694	33.739	35.624	40.767	49.111	70.585
N	0.650	2.22E-042.81I			6.574	9.142	11.853	17.374	25.229	32.171	36.262	38.156	43.292	51.530	72.302
N	1.000	5.03E-044.84I	E-02 0.41	3 3.113	8.063	10.961	13.956	19.908	28.132	35.226	39.347	41.242	46.340	54.413	74.297
N	1.500	1.13E-038.34I	E-02 0.62	1 4.083	9.883	13.135	16.425	22.801	31.358	38.562	42.685	44.568	49.594	57.448	76.341
N	2.500	3.18E-03 0.1	66 1.04	0 5.759	12.791	16.519	20.188	27.078	35.982	43.245	47.324	49.169	54.046	61.538	79.012
Р	0.015	3.97E-074.14I	E-041.16E	02 0.288	1.352	2.241	3.345	6.054	10.854	15.929	19.263	20.889	25.554	33.799	58.556
Р	0.065	1.92E-061.18I	E-032.55E	02 0.487	2.004	3.181	4.583	7.871	13.390	18.975	22.548	24.269	29.138	37.540	61.712
Р	0.100	4.93E-062.22I	E-034.09E	02 0.666	2.537	3.922	5.534	9.209	15.183	21.071	24.777	26.548	31.519	39.975	63.682
Р	0.150	9.76E-063.50I	E-035.76E	02 0.837	3.010	4.565	6.345	10.321	16.633	22.734	26.530	28.335	33.367	41.840	65.150
Р	0.250	2.62E-056.76			3.853	5.686	7.731	12.169	18.975	25.372	29.285	31.130	36.230	44.688	67.331
Р	0.400	5.38E-051.09I	E-02 0.13		4.612	6.671	8.926	13.717	20.883	27.481	31.468	33.336	38.467	46.882	68.964
https:/	0.650	1.21E-041.88I			5.652	7.992	10.503	15.708	23.275	30.080	34.134	36.021	41.164	49.493	70.859
Р	1.000	2.73E-043.22I			6.919	9.567	12.349	17.977	25.928	32.911	37.012	38.908	44.037	52.238	72.797
Р	1.500	7.58E-046.37I			8.937	12.010	15.153	21.321	29.718	36.874	41.000	42.891	47.957	55.926	75.323
Q	0.010	1.04E-071.70l			0.967	1.665	2.559	4.843	9.080	13.728	16.849	18.388	22.856	30.913	56.000
Q	0.040	5.03E-074.85I			1.434	2.362	3.506	6.296	11.200	16.351	19.721	21.362	26.060	34.333	59.017
Q	0.065	1.29E-069.08I			1.815	2.912	4.233	7.366	12.699	18.155	21.669	23.367	28.188	36.558	60.899
Q	0.100	2.55E-061.43I			2.153	3.389	4.852	8.254	13.910	19.587	23.201	24.938	29.839	38.262	62.302
Q	0.150	6.85E-062.76I			2.755	4.220	5.911	9.729	15.865	21.856	25.607	27.395	32.396	40.863	64.385
Q	0.250	1.40E-054.46l			3.296	4.949	6.823	10.965	17.458	23.670	27.512	29.332	34.392	42.865	65.943
Q	0.400	3.16E-057.66			4.037	5.926	8.025	12.552	19.452	25.902	29.836	31.688	36.797	45.247	67.751
Q	0.650	7.08E-051.31			4.939	7.090	9.430	14.359	21.661	28.332	32.343	34.219	39.356	47.747	69.597
Q R	1.000 0.025	1.96E-042.59l 1.23E-071.89l			6.371 1.008	8.891 1.726	11.560 2.644	17.015 4.977	24.812 9.280	31.726 13.979	35.811 17.127	37.704 18.677	42.842 23.170	51.101 31.252	72.001 56.307
R	0.025	3.15E-073.54l			1.275	2.128	3.192	4.977 5.822	9.280 10.521	15.521	18.818	20.429	25.061	33.276	58.102
R	0.040	6.23E-075.59l			1.513	2.126	3.659	6.524	11.524	16.744	20.147	21.801	26.528	34.826	59.439
R	0.100	1.67E-061.08l			1.935	3.083	4.456	7.689	13.142	18.682	22.234	23.947	28.799	37.191	61.424
R	0.150	3.42E-061.74			2.315	3.615	5.143	8.664	14.460	20.230	23.886	25.638	30.571	39.011	62.909
R	0.150	7.68E-062.98I			2.835	4.328	6.047	9.916	16.108	22.135	25.901	27.694	32.705	41.175	64.630
R	0.400	1.72E-055.10l			3.466	5.176	7.104	11.340	17.934	24.206	28.072	29.901	34.975	43.445	66.388
R	0.650	4.74E-051.00I			4.468	6.486	8.703	13.430	20.533	27.097	31.071	32.936	38.062	46.487	68.673
	0.000	001.001	_ 02 0.12	, 1.41/	7100	0.700	0.700	10.400	20.000	21.001	01.071	02.300	00.002	70.707	00.070



TABLE 1C

 $100t\!/\!\mu$ Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, Consumer's Risk = 0.05

Note—These plans assume the characteristic being measured has a Weibull distribution.

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL							Shape Para	meter, β						
Letter	(p%)	0.333	0.50	0.667	1.000 1.3	33 1.5	00 1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
Α	6.500	56.010			149.787147				132.476	128.130	125.783	124.743	122.053	118.079	109.448
В	4.000	16.596	49.858		99.858 108				112.642	111.932	111.377	111.097	110.287	108.881	105.099
С	2.500	3.585	17.949	34.887	59.915 74.				91.825	94.407	95.552	96.010	97.065	98.307	99.865
C D	10.000 1.500	20.487 0.875	57.375 7.011	17.238	107.122114 37.447 52.				115.851 76.087	114.582 80.717	113.748 82.986	113.349 83.946	112.240 86.304	110.421 89.487	105.839 95.280
D	6.500	4.291	20.235	38.169	63.616 77.			89.999	94.053	96.312	97.286	97.669	98.530	99.493	100.465
D	10.000	12.789	41.908	65.896	91.551 101				108.796	108.738	108.512	108.374	107.918	107.007	104.190
Ē	1.000	0.204	2.655	8.322	23.044 36.			54.167	62.657	68.656	71.738	73.072	76.440	81.206	90.764
E	4.000	0.917	7.231	17.642	38.029 52.			69.585	76.559	81.133	83.371	84.317	86.638	89.764	95.427
E	6.500	2.450	13.929	28.845	52.780 67.			81.976	87.284	90.500	91.986	92.594	94.036	95.845	98.607
E	10.000	5.299	23.290	42.415	68.250 81.	702 85.8	69 88.994	93.220	96.736	98.596	99.360	99.651	100.278	100.902	101.174
F	0.650	5.60E-02	1.122	4.361	14.979 26.				52.740	59.472	63.041	64.610	68.635	74.503	86.937
F	2.500	0.241	2.964	9.038	24.348 37.			55.679	64.052	69.927	72.932	74.231	77.499	82.105	91.265
F	4.000	0.611	5.516	14.400	33.215 47.			65.031	72.524	77.554	80.053	81.118	83.755	87.366	94.144
F	6.500	1.244	8.866	20.555	42.108 56.			73.221	79.743	83.936	85.959	86.807	88.873	91.612	96.404
F G	10.000 0.400	3.747 1.37E-02	18.486 0.438	35.667 2.155	60.804 74. 9.362 18.			87.987 34.525	92.368 43.701	94.871 50.848	95.975 54.750	96.415 56.491	97.423	98.597 67.818	100.012 82.946
G	1.500	5.70E-02	1.135	4.399	15.065 26.			43.796	52.861	59.586	63.149	64.716	61.026 68.734	74.588	86.987
G	2.500	0.140	2.066	6.894	20.327 32.			50.874	59.591	65.844	69.088	70.500	74.079	79.194	89.633
G	4.000	0.140	3.242	9.667	25.466 39.			56.942	65.212	70.981	73.921	75.189	78.373	82.845	91.676
G	6.500	0.764	6.404	16.105	35.788 50.			67.503	74.721	79.507	81.865	82.866	85.332	88.680	94.849
G	10.000	1.676	10.814	23.857	46.505 61.			76.950	82.975	86.761	88.559	89.306	91.108	93.450	97.367
Н	0.250	3.58E-03	0.179	1.103	5.991 13.	177 16.9	61 20.674	27.620	36.556	43.820	47.889	49.728	54.584	62.027	79.325
Н	1.000	1.47E-02	0.459	2.232	9.585 18.				44.114	51.249	55.138	56.873	61.387	68.139	83.141
Н	1.500	3.54E-02	0.826	3.466	12.853 23.				49.608	56.515	60.212	61.846	66.059	72.257	85.617
H	2.500	6.82E-02	1.280	4.813	15.998 27.				54.147	60.792	64.298	65.837	69.774	75.490	87.512
H	4.000	0.182	2.457	7.852	22.169 35.			53.128	61.694	67.775	70.909	72.268	75.703	80.580	90.413
H H	6.500 10.000	0.380 0.909	4.022 7.190	11.361 17.566	28.360 42. 37.921 52.			60.091 69.485	68.082 76.471	73.575 81.056	76.347 83.300	77.537 84.248	80.511 86.576	84.649 89.712	92.668 95.400
.1	0.150	8.75E-04			3.745 9.2			21.835	30.291	37.465	41.591	43.479	48.532	56.462	75.683
J	0.650	3.54E-03	0.178	1.097	5.967 13.			27.564	36.497	43.761	47.832	49.671	54.529	61.978	79.294
Ĵ	1.000	8.44E-03	0.318	1.693	7.970 16.			31.856	40.977	48.193	52.170	53.953	58.621	65.671	81.622
J	1.500	1.61E-02		2.336	9.880 19.				44.653	51.770	55.642	57.367	61.854	68.553	83.394
J	2.500	4.17E-02	0.921	3.762	13.573 24.	332 29.2	57 33.769	41.572	50.702	57.551	61.205	62.817	66.966	73.049	86.085
https:/	4.000	8.49E-02	1.480	5.369	17.206 29.				55.747	62.285	65.718	67.221	71.056	76.597	88.151
J	6.500	0.194	2.569	8.117	22.665 35.				62.243	68.277	71.382	72.727	76.123	80.937	90.614
J	10.000	0.455	4.532	12.427	30.107 44.				69.729	75.055	77.728	78.873	81.723	85.666	93.224
K	0.100	2.29E-04			2.397 6.6			17.468	25.339	32.287	36.380	38.274	43.409	51.641	72.380
K	0.400 0.650	9.22E-04			3.810 9.3			22.026	30.503	37.683	41.809	43.696	48.744	56.659	75.815
K K	1.000	2.18E-03 4.13E-03	0.129	0.861 1.184	5.078 11.4 6.279 13.			25.426 28.275	34.214 37.248	41.468 44.510	45.570 48.567	47.431 50.399	52.371 55.227	60.008 62.612	78.023 79.698
K	1.500	1.05E-02		1.892	8.584 17.				42.211	49.400	53.344	55.109	59.718	66.653	82.230
K	2.500	2.11E-02	0.586	2.680	10.826 20.			37.127	46.317	53.373	57.190	58.887	63.285	69.819	84.160
K	4.000	4.72E-02	1.001	4.003	14.147 25.			42.441	51.548	58.351	61.970	63.564	67.662	73.656	86.442
K	6.500	1.07E-01	1.726	6.023	18.577 30.				57.483	63.898	67.247	68.710	72.431	77.781	88.830
K	10.000	3.10E-01	3.513	10.265	26.505 40.	193 45.7	08 50.454	58.093	66.264	71.934	74.813	76.053	79.161	83.511	92.043
L	0.065	5.60E-05			1.498 4.6			13.810	20.996	27.605	31.595	33.465	38.596	47.008	69.057
L	0.250	2.24E-04			2.378 6.5			17.400	25.259	32.203	36.294	38.189	43.324	51.560	72.323
L	0.400	5.28E-04			3.164 8.1				28.316	35.418	39.540	41.435	46.530	54.591	74.418
L	0.650	9.93E-04			3.906 9.5				30.807	37.997	42.122	44.007	49.048	56.942	76.004
L	1.000	2.51E-03		0.924	5.324 12.				34.868	42.127	46.221	48.077	52.994	60.578	78.393
L L	1.500 2.500	5.00E-03 1.10E-02		1.302 1.931	6.692 14. 8.701 17.			29.191 33.285	38.210 42.441	45.466 49.623	49.505 53.562	51.325 55.323	56.114 59.920	63.415 66.834	80.208 82.341
L	4.000	2.43E-02		2.875	11.347 21.				47.195	54.215	58.002	59.682	64.032	70.478	84.556
Ĺ	6.500	6.80E-02		4.805	15.979 27.			45.105	54.121	60.768	64.275	65.814	69.753	75.472	87.501
М	0.040	1.43E-05						11.004	17.508	23.726	27.570	29.391	34.453	42.926	65.990
М	0.150	5.72E-05			1.508 4.6			13.858	21.055	27.669	31.662	33.532	38.664	47.074	69.105
М	0.250	1.34E-04			2.005 5.7				23.594	30.423	34.484	36.372	41.515	49.831	71.100
M	0.400	2.52E-04			2.473 6.7				25.660	32.628	36.725	38.620	43.752	51.968	72.608
M	0.650	6.35E-04			3.364 8.5				29.021	36.151	40.276	42.169	47.250	55.266	74.877
M	1.000	1.25E-03			4.221 10.				31.778	38.991	43.113	44.993	50.008	57.831	76.595
М	1.500	2.73E-03		0.963	5.472 12.				35.255	42.516	46.605	48.457	53.361	60.913	78.610
M	2.500	5.98E-03		1.425	7.108 14.				39.142	46.387	50.408	52.216	56.965	64.183	80.692
M	4.000	1.63E-02		2.356	9.936 19.				44.754	51.868	55.737	57.461	61.942	68.631	83.441
N	0.025	3.58E-06	1./9⊏-03	ა.49E-02	0.599 2.3	43 3.6	54 5.193	8.734	14.553	20.339	24.002	25.757	30.695	39.137	63.010



TABLE 1C

 $100t/\mu$ Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, Consumer's Risk = 0.05

 $\label{thm:note-thm$

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL	Shape Parameter, β													
Letter	(p%)	0.333 0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.100	1.43E-054.51E-	036.96E-02	0.950	3.310	4.968	6.846	10.996	17.498	23.715	27.559	29.380	34.441	42.914	65.981
N	0.150	3.35E-057.96E-	0.107	1.262	4.096	6.003	8.118	12.674	19.603	26.070	30.010	31.864	36.976	45.422	67.882
N	0.250	6.27E-05 1.21E-	02 0.146	1.555	4.792	6.902	9.205	14.073	21.315	27.954	31.955	33.827	38.962	47.364	69.318
N	0.400	1.57E-042.23E-	0.231	2.113	6.031	8.467	11.063	16.403	24.095	30.960	35.032	36.923	42.064	50.358	71.475
N	0.650	3.10E-043.51E-	0.324	2.648	7.143	9.842	12.667	18.363	26.371	33.379	37.486	39.382	44.506	52.683	73.106
N	1.000	6.71E-045.87E-	02 0.477	3.427	8.666	11.687	14.786	20.888	29.235	36.374	40.499	42.392	47.468	55.470	75.015
N	1.500	1.46E-039.86E-	02 0.704	4.440	10.524	13.889	17.271	23.776	32.426	39.653	43.771	45.647	50.643	58.419	76.983
N	2.500	3.93E-03 0.19	1.155	6.179	13.485	17.313	21.060	28.049	37.010	44.272	48.334	50.168	55.006	62.411	79.570
Р	0.015	8.75E-077.01E-	041.72E-02	0.374	1.647	2.671	3.917	6.905	12.059	17.390	20.845	22.520	27.292	35.625	60.117
Р	0.065	3.48E-06 1.76E-	033.44E-02	0.593	2.326	3.631	5.163	8.692	14.497	20.274	23.932	25.685	30.620	39.061	62.949
Р	0.100	8.15E-063.10E-			2.878	4.386	6.121	10.016	16.239	22.284	26.057	27.854	32.870	41.341	64.760
Р	0.150	1.53E-054.71E-			3.366	5.042	6.938	11.119	17.654	23.891	27.743	29.567	34.633	43.105	66.128
Р	0.250	3.82E-058.69E-		1.318	4.233	6.182	8.335	12.956	19.950	26.454	30.407	32.265	37.383	45.822	68.180
Р	0.400	7.50E-05 1.36E-		1.651	5.011	7.182	9.539	14.498	21.828	28.514	32.530	34.407	39.546	47.931	69.731
Р	0.650	1.62E-042.28E-		2.134	6.074	8.522	11.127	16.482	24.188	31.060	35.133	37.024	42.166	50.455	71.544
Р	1.000	3.50E-043.81E-		2.760	7.368	10.117	12.985	18.746	26.811	33.843	37.954	39.850	44.968	53.120	73.409
Р	1.500	9.37E-047.34E-		3.831	9.421	12.588	15.807	22.085	30.567	37.750	41.876	43.762	48.809	56.719	75.855
Q	0.010	2.29E-072.87E-			1.179	1.984	2.997	5.524	10.088	14.986	18.233	19.824	24.411	32.583	57.493
Q	0.040	9.12E-077.21E-			1.664	2.696	3.949	6.953	12.126	17.470	20.931	22.609	27.386	35.724	60.200
Q	0.065	2.13E-06 1.27E-			2.058	3.257	4.682	8.011	13.581	19.201	22.789	24.516	29.397	37.807	61.931
Q	0.100	3.99E-06 1.93E-			2.407	3.743	5.306	8.892	14.764	20.584	24.261	26.022	30.971	39.419	63.237
Q	0.150	9.98E-063.55E-			3.026	4.587	6.373	10.359	16.681	22.789	26.588	28.394	33.427	41.900	65.197
Q	0.250	1.96E-055.56E-			3.581	5.328	7.291	11.589	18.248	24.559	28.440	30.274	35.357	43.824	66.677
Q	0.400	4.22E-059.28E-		1.362	4.339	6.319	8.501	13.171	20.215	26.746	30.710	32.571	37.693	46.125	68.406
Q	0.650	9.10E-051.55E-		1.761	5.259	7.497	9.916	14.973	22.399	29.134	33.166	35.047	40.189	48.553	70.183
Q	1.000	2.42E-042.98E-		2.440	6.717	9.318	12.059	17.625	25.520	32.480	36.575	38.470	43.603	51.826	72.509
R	0.025	2.23E-072.81E-			1.170	1.970	2.979	5.496	10.047	14.936	18.178	19.767	24.349	32.518	57.435
R	0.040	5.21E-074.96E-			1.447	2.380	3.531	6.332	11.252	16.415	19.790	21.433	26.136	34.413	59.086
R	0.065	9.73E-077.53E-			1.691	2.735	4.001	7.028	12.231	17.596	21.068	22.749	27.535	35.879	60.331
R	0.100	2.43E-06 1.39E-			2.126	3.352	4.804	8.186	13.818	19.479	23.086	24.820	29.716	38.135	62.199
R	0.150	4.76E-062.17E-			2.515	3.892	5.496	9.157	15.114	20.991	24.692	26.462	31.429	39.884	63.609
R	0.250	1.02E-053.61E-			3.047	4.615	6.407	10.405	16.740	22.856	26.659	28.466	33.502	41.975	65.255
R	0.400	2.21E-056.03E-			3.691	5.473	7.470	11.825	18.545	24.891	28.786	30.625	35.715	44.179	66.946
R	0.650	5.85E-05 1.16E-	02 0.141	1.520	4.710	6.797	9.078	13.912	21.120	27.740	31.735	33.605	38.738	47.146	69.158

TABLE 2A

100h/(t) Products at the Acceptable Quality Level (normal inspection) for the MIL-STD-105D Plans

Note—These plans assume the characteristic being measured has a Weibull distribution.

Note—Where scientific notation is used (that is, E-x), the decimal point is moved to the left x places (for example, if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL							Shar	e Parame	ter, β						
p'(%)	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.010	3.33E-03	5.00E-03	6.67E-03	1.00E-02	1.33E-02	1.50E-02	1.67E-02	2.00E-02	2.50E-02	3.00E-02	3.33E-02	3.50E-02	4.00E-02	5.00E-02	0.100
0.015	5.00E-03	7.50E-03	1.00E-02	1.50E-02	2.00E-02	2.25E-02	2.50E-02	3.00E-02	3.75E-02	4.50E-02	5.00E-02	5.25E-02	6.00E-02	7.50E-02	0.150
0.025	8.33E-03	1.25E-02	1.67E-02	2.50E-02	3.33E-02	3.75E-02	4.17E-02	5.00E-02	6.25E-02	7.50E-02	8.33E-02	8.75E-02	0.100	0.125	0.250
0.040	1.33E-02	2.00E-02	2.67E-02	4.00E-02	5.33E-02	6.00E-02	6.67E-02	8.00E-02	0.100	0.120	0.133	0.140	0.160	0.200	0.400
0.065	2.17E-02	3.25E-02	4.33E-02	6.50E-02	0.087	9.75E-02	0.108	0.130	0.163	0.195	0.217	0.228	0.260	0.325	0.650
0.100	3.34E-02	5.00E-02	6.67E-02	0.100	0.133	0.150	0.167	0.200	0.250	0.300	0.334	0.350	0.400	0.500	1.001
0.150	5.00E-02	7.51E-02	0.100	0.150	0.200	0.225	0.250	0.300	0.375	0.450	0.500	0.525	0.600	0.751	1.501
0.250	8.34E-02	0.125	0.167	0.250	0.334	0.375	0.417	0.501	0.626	0.751	0.834	0.876	1.001	1.252	2.503
0.400	0.134	0.200	0.267	0.401	0.534	0.601	0.668	0.802	1.002	1.202	1.336	1.403	1.603	2.004	4.008
0.650	0.217	0.326	0.435	0.652	0.869	0.978	1.087	1.304	1.630	1.956	2.174	2.282	2.608	3.261	6.521
1.000	0.335	0.503	0.670	1.005	1.340	1.508	1.675	2.010	2.513	3.015	3.350	3.518	4.020	5.025	10.050
1.500	0.504	0.756	1.008	1.511	2.015	2.267	2.519	3.023	3.778	4.534	5.038	5.290	6.045	7.557	15.114
2.500	0.844	1.266	1.688	2.532	3.376	3.798	4.220	5.064	6.329	7.595	8.439	8.861	10.127	12.659	25.318
4.000	1.361	2.041	2.721	4.082	5.443	6.123	6.804	8.164	10.205	12.247	13.607	14.288	16.329	20.411	40.822
6.500	2.240	3.360	4.481	6.721	8.961	10.081	11.201	13.442	16.802	20.163	22.403	23.523	26.883	33.604	67.209
10.000	3.512	5.268	7.024	10.536	14.048	15.804	17.560	21.072	26.340	31.608	35.120	36.876	42.144	52.680	105.361