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An American National Standard

Standard Terminology Relating to Quality and Statistics¹

This standard is issued under the fixed designation E456; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ε) indicates an editorial change since the last revision or reapproval.

This standard has been approved for use by agencies of the U.S. Department of Defense.

 ϵ^1 NOTE—New terms were added in April 2024.

1. Scope

- 1.1 This standard is the general terminology standard for terms defined in the standards of Committee E11 on Quality and Statistics.
- 1.2 A term in this standard which lists an attribution to an E11 technical standard indicates that the standard is normative for that term. Any changes in the term definition in the normative standard will be editorially changed in this standard. Any terms added to an E11 standard will be editorially added to this standard with an attribution to that standard.
- 1.3 Term definitions that are similar to ISO 3534 will be noted in this standard, but ISO 3534 will not be considered normative for any E11 terms.
- 1.4 This international standard was developed in accordance with internationally recognized principles on standardization established in the Decision on Principles for the Development of International Standards, Guides and Recommendations issued by the World Trade Organization Technical Barriers to Trade (TBT) Committee.

2. Referenced Documents

- 2.1 ASTM E11 Standards with Terms in This Standard:²
- E29 Practice for Using Significant Digits in Test Data to Determine Conformance with Specifications
- E105 Guide for Probability Sampling of Materials
- E122 Practice for Calculating Sample Size to Estimate, With Specified Precision, the Average for a Characteristic of a Lot or Process
- E141 Practice for Acceptance of Evidence Based on the Results of Probability Sampling

- E177 Practice for Use of the Terms Precision and Bias in ASTM Test Methods
- E178 Practice for Dealing With Outlying Observations
- E691 Practice for Conducting an Interlaboratory Study to Determine the Precision of a Test Method
- E1169 Practice for Conducting Ruggedness Tests
- E1325 Terminology Relating to Design of Experiments
- E1402 Guide for Sampling Design
- E1488 Guide for Statistical Procedures to Use in Developing and Applying Test Methods
- E1994 Practice for Use of Process Oriented AOQL and LTPD Sampling Plans
- E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL
- E2281 Practice for Process Capability and Performance Measurement
- E2282 Guide for Defining the Test Result of a Test Method E2334 Practice for Setting an Upper Confidence Bound for a Fraction or Number of Non-Conforming items, or a Rate of Occurrence for Non-Conformities, Using Attribute Data, When There is a Zero Response in the Sample
- E2489 Practice for Statistical Analysis of One-Sample and Two-Sample Interlaboratory Proficiency Testing Programs
- E2554 Practice for Estimating and Monitoring the Uncertainty of Test Results of a Test Method Using Control Chart Techniques
- E2555 Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection
- E2586 Practice for Calculating and Using Basic Statistics
- E2587 Practice for Use of Control Charts in Statistical Process Control
- E2655 Guide for Reporting Uncertainty of Test Results and Use of the Term Measurement Uncertainty in ASTM Test Methods
- E2696 Practice for Life and Reliability Testing Based on the Exponential Distribution
- E2709 Practice for Demonstrating Capability to Comply with an Acceptance Procedure
- E2762 Practice for Sampling a Stream of Product by Variables Indexed by AQL
- E2782 Guide for Measurement Systems Analysis (MSA)

¹ This terminology is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.70 on Editorial/Terminology.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

- E2819 Practice for Single- and Multi-Level Continuous Sampling of a Stream of Product by Attributes Indexed by AOL
- E2935 Practice for Evaluating Equivalence of Two Testing Processes
- E3080 Practice for Regression Analysis with a Single Predictor Variable
- E3159 Guide for General Reliability
- E3264 Guide for Homogeneity of Samples and Reference Materials Used for Inter- and Intra-Laboratory Studies 2.2 *ISO Standards*:³
- ISO 3534 Statistics—Vocabulary and Symbols
- Part 2 Applied Statistics

3. Terminology

- **acceptance quality limit (AQL),** *n*—quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling. **E2234**
- **accepted reference value,** n—a value that serves as an agreed-upon reference for comparison, and which is derived as: (I) a theoretical or established value, based on scientific principles, (2) an assigned or certified value, based on experimental work of some national or international organization, or (3) a consensus or certified value, based on collaborative experimental work under the auspices of a scientific or engineering group.
- accuracy, *n*—the closeness of agreement between a test result and an accepted reference value.
- aliases, n—in a fractional factorial design, two or more effects which are estimated by the same contrast and which, therefore, cannot be estimated separately.E1325
- alternative hypothesis, H_a , n—a probability distribution or type of probability distribution distinguished from the null hypothesis.
- analysis of variance (ANOVA), n—statistical models and associated procedures, in which the observed variance is partitioned into components due to different explanatory variables.
- analysis of variance table, *n*—a tabular summary of results from a regression model or an experimental design for the purpose of evaluating effects of factors.

 E1325
- area sampling, n—probability sampling in which a map, rather than a tabulation of sampling units, serves as the sampling frame.
- assignable cause, n—factor that contributes to variation in a process or product output that is feasible to detect and identify (see special cause).
- attributes data, n—observed values or test results that indicate the presence or absence of specific characteristics or counts of occurrences of events in time or space.

 E2587
- ³ Available from International Organization for Standardization (ISO), ISO Central Secretariat, BIBC II, Chemin de Blandonnet 8, CP 401, 1214 Vernier, Geneva, Switzerland, http://www.iso.org.

- **attributes, method of,** *n*—measurement of quality by the method of attributes consists of noting the presence (or absence) of some characteristic or attribute in each of the units in the group under consideration, and counting how many units do (or do not) possess the quality attribute, or how many such events occur in the unit, group, or area.
- **audit subsample,** *n*—a small subsample of a sample selected for review of all sample selection and data collection procedures. **E141**
- average outgoing quality (AOQ), *n*—the average percent defective of outgoing product including all accepted lots or batches, after any defective units found in them are replaced by acceptable units, plus all lots or batches which are not accepted after such lots or batches have been effectively 100 % inspected and all defective units replaced by acceptable units.

 E1994
- **average outgoing quality limit (AOQL),** *n*—the maximum of the AOQs for all possible incoming percentages defective for the process, for a given acceptance sampling plan. **E1994**
- average quality protection, *n*—a type of protection in which there is prescribed some chosen value of average percent defective in the product after inspection (average outgoing quality limit (AOQL), that shall not be exceeded in the long run no matter what may be the level of percent defective in the product submitted to the inspector.
- average run length (ARL), *n*—the average number of times that a process will have been sampled and evaluated before a shift in process level is signaled.

 E2587
- **B**_p life, *n*—for continuous variables, the life at which there is a probability (expressed as a percentage) of failure at or less than this value.
- balanced incomplete block design (BIB), n—an incomplete block design in which each block contains the same number k of different versions from the t versions of a single principal factor arranged so that every pair of versions occurs together in the same number, λ , of blocks from the b blocks.
- **bias,** *n*—the difference between the expectation of the test results and an accepted reference value. **E177**
- **binary scale,** *n*—nominal scale with only two possible categories.
- **binary test result,** n—a test result for which the final value is one of two possible categories. **E2282**
- **block factor**, *n*—a factor that indexes division of experimental units into disjoint subsets. **E1325**
- **bulk sampling,** *n*—sampling to prepare a portion of a mass of material that is representative of the whole. **E1402**
- **c chart,** *n*—control chart that monitors the count of occurrences of an event in a defined increment of time or space.

E2587



calibration, *n*—process of establishing a relationship between a measurement device and a known standard value(s).

E278

center line, *n*—line on a control chart depicting the average level of the statistic being monitored. **E2587**

chance cause, n—source of inherent random variation in a process which is predictable within statistical limits (see common cause).

characteristic, n—a property of items in a sample or population which, when measured, counted or otherwise observed, helps to distinguish among the items.

check sample, *n*—see control sample. **E2554**

classification of defects, n—the enumeration of possible defects of the unit of product arranged according to their seriousness, that is, critical, major, or minor defect. E2234

cluster sampling, *n*—sampling in which the sampling unit consists of a group of subunits, all of which are measured for sampled clusters. **E1402**

coefficient of variation (CV), *n*—for a nonnegative characteristic, the ratio of the standard deviation to the mean for a population or sample.

collaborative study, *n*—interlaboratory study in which each laboratory uses the defined method of analysis to analyze identical portions of homogeneous materials to assess the performance characteristics obtained for that method of analysis. **E2489**

collaborative trial, *n*—see collaborative study. **E2489**

common cause, *n*—see chance cause. E2587

completely randomized design, *n*—a design in which the treatments are assigned at random to the full set of experimental units. **E1325**

completely randomized factorial design, n—a factorial experiment (including all replications) run in a completely randomized design.
E1325

component of variance, *n*—a part of a total variance identified with a specified source of variability. **E1488**

composite design, *n*—a design developed specifically for fitting second order response surfaces to study curvature, constructed by adding further selected treatments to those obtained from a 2ⁿ factorial (or its fraction). **E1325**

confidence bound, *n*—see confidence limit. **E2586**

confidence coefficient, *n*—see confidence level. **E2586**

confidence interval, n—an interval estimate [L, U] with the statistics L and U as limits for the parameter θ and with confidence level 1- α , where $Pr(L \le \theta \le U) \ge 1-\alpha$. **E2586**

confidence level, *n*—the value, 1-α, of the probability associated with a confidence interval, often expressed as a percentage. **E2586**

confidence limit, *n*—each of the limits, L and U, of a confidence interval, or the limit of a one-sided confidence interval.

confounded factorial design, n—a factorial experiment in which only a fraction of the treatment combinations are run in each block and where the selection of the treatment combinations assigned to each block is arranged so that one or more prescribed effects is (are) confounded with the block effect(s), while the other effects remain free from confounding.

confounding, *n*—combining indistinguishably the main effect of a factor or a differential effect between factors (interactions) with the effect of other factor(s), block factor(s) or interactions(s). **E1325**

consumer's risk, *n*—probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan.

E2555

continuous sampling inspection, *n*—a method of sampling a stream of product in order of production where the sampling frequency is adjusted based on ongoing inspection results.

F2810

contrast, *n*—a linear function of the observations for which the sum of the coefficients is zero. **E1325**

contrast analysis, *n*—a technique for estimating the parameters of a model and making hypothesis tests on preselected linear combinations of the treatments (contrasts). **E1325**

control chart, *n*—chart on which are plotted a statistical measure of a subgroup versus time of sampling along with limits based on the statistical distribution of that measure so as to indicate how much common, or chance, cause variation is inherent in the process or product.

control chart factor, *n*—a tabulated constant, depending on sample size, used to convert specified statistics or parameters into a central line value or control limit appropriate to the control chart.

control limits, n—limits on a control chart that are used as criteria for signaling the need for action or judging whether a set of data does or does not indicate a state of statistical control based on a prescribed degree of risk.
E2587

control sample, *n*—sample taken from a stable, homogeneous material for the purposes of monitoring the performance of a test method in a laboratory. **E2554**

critical defect, *n*—a defect that judgment and experience indicate would result in hazardous or unsafe conditions for individuals using, maintaining, or depending upon the product, or a defect that judgment and experience indicate is likely to prevent performance of the function of a major end item. **E2234**

critical value, *n*—*in hypothesis testing*, the boundary (number) of the rejection region for a test statistic in a hypothesis test.

E2586

- **defect,** *n*—any nonconformance of the unit of product with specified requirements. **E2234**
- **degrees of freedom, df,** *n*—the number of independent data points minus the number of parameters that have to be estimated before calculating the variance. **E2586**
- **design of experiments,** *n*—the arrangement in which an experimental program is to be conducted, and the selection of the levels (versions) of one or more factors or factor combinations to be included in the experiment. Synonyms include *experiment design* and **experimental design. E1325**
- **double sampling plan,** *n*—a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot.

 E2234
- **equal complete coverage result,** *n*—the numerical characteristic of interest calculated from observations made by drawing randomly from the frame, all of the sampling units covered by the frame. **E141**
- **equivalence,** *n*—condition that two population parameters differ by no more than predetermined limits. **E2935**
- **error of result,** *n*—a test result minus the accepted reference value of the characteristic. **E2655**
- **estimate**, *n*—sample statistic used to approximate a population parameter. **E2586**
- **evolutionary operation** (**EVOP**), *n*—a sequential form of experimentation conducted in production facilities during regular production. **E1325**
- **EWMA chart,** *n*—control chart that monitors the exponentially weighted moving averages of consecutive subgroups. **E2587**
- **EWMV chart,** *n*—control chart that monitors the exponentially weighted moving variance. **E2587**
 - **expanded uncertainty, U,** *n*—uncertainty reported as a multiple of the standard uncertainty. **E2655**
 - **experimental design,** *n*—see **design of experiments. E1325 experimental unit,** *n*—a portion of the experiment space to which a treatment is applied or assigned in the experiment. **E1325**
 - **experiment space,** *n*—the materials, equipment, environmental conditions and so forth that are available for conducting an experiment.

 E1325
 - **exponentially weighted moving average** (EWMA), *n*—weighted average of time-ordered data where the weights of past observations decrease geometrically with age. **E2587**
 - exponentially weighted moving variance (EWMV), n—weighted average of squared deviations of observations from their current estimate of the process average for time ordered observations, where the weights of past squared deviations decrease geometrically with age.
 - **factor,** *n*—independent variable in an experimental design. **E1325**

- factorial experiment (general), n—in general, an experiment in which all possible treatments formed from two or more factors, each being studied at two or more levels (versions) are examined so that interactions (differential effects) as well as main effects can be estimated.

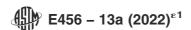
 E1325
- 2^n factorial experiment, n—a factorial experiment in which n factors are studied, each of them in two levels (versions).
- **failure mode,** *n*—the way in which a device, process or system has failed. **E3159**
- **fractional factorial design,** *n*—a factorial experiment in which only an adequately chosen fraction of the treatments required for the complete factorial experiment is selected to be run. **E1325**
- **frame,** *n*—a list, compiled for sampling purposes, which designates all of the sampling units (items or groups) of a population or universe to be considered in a specific study.
- **fully nested experiment,** *n*—a nested experiment in which the second factor is nested within levels (versions) of the first factor and each succeeding factor is nested within versions of the previous factor. **E1325**
- **gage**, *n*—device used as part of the measurement process to obtain a measurement result.

 E2782
- hazard rate, n—differential fraction of items failing at time t among those surviving up to time t, symbolized by h(t).

 E2555
- heterogeneity, n—the condition of a population under which items of the population are not of uniform structure or composition with respect to the characteristic of interest.
- **hierarchical experiment,** *n*—see **nested experiment. E1325 histogram,** *n*—graphical representation of the frequency distribution of a characteristic consisting of a set of rectangles with area proportional to the frequency. **ISO 3534-1, E2586**
- I chart, *n*—control chart that monitors the individual subgroup observations.
- incomplete block design, n—a design in which the experiment space is subdivided into blocks in which there are insufficient experimental units available to run a complete set of treatments or replicate of the experiment.

 E1325
- inspection, *n*—the process of measuring, examining, testing, or otherwise comparing the unit of product with the requirements. **E2234**
- inspection by attributes, *n*—inspection whereby either the unit of product is classified simply as defective or non-defective, or the number of defects in the unit of product is counted, with respect to a given requirement or set of requirements.
- inspection by variables, *n*—inspection wherein the unit of product is measured on a continuous scale with respect to a given requirement or set of requirements.

 E2762



- inspection lot, n—a collection of units of product produced under conditions that are considered uniform and from which a sample is drawn and inspected.E2234
- **interaction,** n—differences in responses to a factor among levels (versions) of other factors in the experiment. **E1325**
- interlaboratory comparison, n—organization, performance, and evaluation of tests on the same or similar test items by two or more laboratories in accordance with predetermined conditions.
 E2489
- interlaboratory study (ILS), *n*—a designed procedure for obtaining a precision statement for a test method, involving multiple laboratories, each generating replicate test results on one or more materials.
- intermediate precision, n—precision of test results from tests conducted on identical material by the same test method in a single laboratory at the same or various times with one or more known sources of variability controlled at multiple levels.
- intermediate precision conditions, *n*—conditions under which test results are obtained with the same test method using test units or test specimens taken at random from a single quantity of material that is as nearly homogeneous as possible, and with changing conditions such as operator, measuring equipment, location within the laboratory, and time.
- **interquartile range** (**IQR**), *n*—the 75th percentile (0.75 quantile) minus the 25th percentile (0.25 quantile), for a data set.
- **interval scale**, *n*—continuous scale or discrete scale with equal sized scale values and an arbitrary zero. **ISO 3534-2**, **E2282**
- **item**, *n*—an object or quantity of material on which a set of observations can be made. **E2334**
- judgment sampling, n—a procedure whereby enumerators select a few items of the population, based on visual, positional or other cues that are believed to be related to the variable of interest, so that the selected items appear to match the population.
- **kurtosis**, γ_2 , \mathbf{g}_2 , n—for a population or a sample, a measure of the weight of the tails of a distribution relative to the center, calculated as the ratio of the fourth central moment (empirical if a sample, theoretical if a population applies) to the standard deviation (sample, s, or population, σ) raised to the fourth power, minus 3 (also referred to as excess kurtosis).
- **laboratory precision,** *n*—the *precision* of test results obtained within a laboratory for identical material under conditions that include all known sources of variation within the laboratory over extended periods of time, often months.
- **latin square,** *n*—a factorial experiment having two block factors (rows and columns) and a treatment factor, with

- equal numbers of levels, and for which each treatment occurs once in each row and column.

 E1325
- **level (of a factor),** *n*—a given value, a specification of procedure or a specific setting of a factor. **E1325**
- **life test,** *n*—process of placing one or more units of product under a specified set of test conditions and measuring the time until failure for each unit. **E2696**
- **limiting quality level (LQL),** *n*—quality level having a specified consumer's risk for a given sampling plan. **E2555**
- **long term standard deviation,** σ_{LT} , n—sample standard deviation of all individual (observed) values taken over a long period of time.
- **lot**, *n*—a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes. **E2555**
- lot quality protection, n—a type of protection in which there is prescribed some chosen value of limiting percent defective in a lot (lot tolerance percent defective (LTPD)) and also some chosen value for the probability (called the consumer's risk) of accepting a submitted lot that has a percent defective equal to the lot tolerance percent defective.
- lot tolerance percent defective (LTPD), *n*—for purposes of acceptance sampling, the percentage of defective units in a lot for which the consumer has a stated low probability of acceptance of the lot.

 E1994
- lower control limit (LCL), *n*—minimum value of the control chart statistic that indicates statistical control. **E2587**
- main effect, average effect, n—a term describing a measure for the comparison of the responses at each level (version) of a factor averaged over all levels (versions) of other factors in the experiment.
- **major defect,** *n*—a defect, other than critical, that is likely to result in failure, or to reduce materially the usability of the unit of product for its intended purpose. **E2234**
- **mean,** n—of a population, μ , average or expected value of a characteristic in a population; of a sample, \bar{x} , sum of the observed values in the sample divided by the sample size.
- **mean time between failures (MTBF),** *n*—the average time to failure for a repairable item. **E3159**
- mean time to failure (MTTF), θ, n—in life testing, the average length of life of items in a lot. **E2696**
- measurement process, *n*—process used to assign a number to a property of an object or other physical entity. **E2782**
- **measurement result,** *n*—number assigned to a property of an object or other physical entity being measured. **E2782**
- **measurement system,** *n*—the collection of hardware, software, procedures and methods, human effort, environmental conditions, associated devices, and the objects that

are measured for the purpose of producing a measurement.

measurement systems analysis (MSA), *n*—any of a number of specialized methods useful for studying a measurement system and its properties. **E2782**

median, $\tilde{\mathbf{x}}$, n—the 50th percentile in a population or sample.

method of least squares, n—a technique of estimation of a parameter which minimizes $\sum e^2$, where e is the difference between the observed value and the predicted value derived from the assumed model. **E1325**

midrange, *n*—average of the minimum and maximum values in a sample.

minor defect, n—a defect that is not likely to reduce materially the usability of the unit of product for its intended purpose, or is a departure from established standards having little bearing on the effective use or operation of the unit. E2234

mixture design, *n*—a design in which two or more ingredients or components shall be mixed and the response is a property of the resulting mixture that does not depend upon the amount of the mixture.

E1325

MR chart, *n*—control chart that monitors the moving range of consecutive individual subgroup observations.

multiple sampling plan, n—a sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples.

E2234

multiple stage acceptance procedure, *n*—a procedure that involves more than one stage of sampling and testing a given quality characteristic and one or more acceptance criteria per stage.

E2709

multi-stage sampling, *n*—sampling in which the sample is selected by stages, the sampling units at each stage being selected from subunits of the larger sampling units chosen at the previous stage.

E1402

nested experiment, n—an experiment to examine the effect of two or more factors in which the same level (version) of a factor cannot be used with all levels (versions) of other factors. Synonym hierarchical experiment.

nested sampling, *n*—same as **multi-stage sampling**. **E1402**

nominal scale, *n*—scale with unordered labeled categories or ordered by convention. **ISO 3534-2, E2282**

non-conforming item, *n*—an item containing at least one non-conformity. **ISO 3534-2, E2334**

non-conformity, *n*—the non-fulfillment of a specified requirement. **ISO 3534-2, E2334**

null hypothesis, H₀, *n*—a statement about a parameter of a probability distribution or about the type of probability

distribution, tentatively regarded as true until rejected using a statistical hypothesis test.

E2586

number of failures, *n*—number of failures that have occurred at the time the decision as to lot acceptability is reached.

observation, *n*—the process of obtaining information regarding the presence or absence of an attribute of a test specimen, or of making a reading on a characteristic or dimension of a test specimen. **E2282**

observed value, *n*—the value obtained by making an observation.

operating characteristic, n—probability of acceptance using a specified acceptance sampling plan, as a function of parameters describing quality of the lot.

order statistic $\mathbf{x_{(k)}}$, n—value of the k^{th} observed value in a sample after sorting by order of magnitude. **E2586**

ordinal scale, *n*—scale with ordered labeled categories.

ISO 3534-2, E2282

ordinal test result, *n*—a test result where the final value is reported as one of the scale results on an ordinal scale.

orthogonal array, *n*—a table of coefficients identifying the levels, or some weight associated with the levels, for each factor to be used in the analysis of specified effects, which are arranged in such a manner that each effect will be

orthogonal contrasts, n—two contrasts are orthogonal if the contrast coefficients of the two sets satisfy the condition that, when multiplied in corresponding pairs, the sum of the products is equal to zero. See contrast and contrast analysis.

E1325

outlier—see outlying observation.

independent of the other effects.

outlying observation, n—an extreme observation in either direction that appears to deviate markedly in value from other members of the sample in which it appears.
 E178

p chart, *n*—control chart that monitors the fraction of occurrences of an event.

parameter, *n*—see population parameter. **E2586**

partially balanced incomplete block design (PBIB), n—an incomplete block design in which each block contains the same number k, of different versions from the t versions of the principal factor.

partially nested experiment, *n*—a nested experiment in which several factors may be crossed as in factorial experiments and other factors nested within the crossed combinations.

E1325

E178

percentile, *n*—quantile of a sample or a population, for which the fraction less than or equal to the value is expressed as a percentage. **E2586**