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Točnost (pravilnost in natančnost) merilnih metod in rezultatov – 5. del : Alternativne metode določanja natančnosti standardne merilne metode

Accuracy (trueness and precision) of measurement methods and results -- Part 5: Alternative methods for the determination of the precision of a standard measurement method

Exactitude (justesse et fidélité) des résultats et méthodes de mesure -- Partie 5: Méthodes alternatives pour la détermination de la fidélité d'une méthode de mesure normalisée

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INTERNATIONAL STANDARD

ISO 5725-5

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Accuracy (trueness and precision) of measurement methods and results —

Part 5:
Alternative methods for the determination of the precision of a standard measurement method

Exactitude (justesse et fidélité) des résultats et méthodes de mesure —

Partie 5: Méthodes alternatives pour la détermination de la fidélité d'une méthode de mesure normalisée

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Contents

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Foreword

ISO (the International Organization for Standardization) is a world-wide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organisations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International standard requires approval by at least 75 % of the member bodies casting a vote.

ISO 5725-5 was prepared by Technical Committee ISO/TC 69, *Applications of statistical methods*, Subcommittee SC 6, *Measurement methods and results*.

ISO 5725 consists of the following parts, under the general title *Accuracy (trueness and precision) of measurement methods and results*:

— *Part 1: General principles and definitions*

— *Part 2: Basic method for the determination of repeatability and reproducibility of a standard measurement method*

— *Part 3: Intermediate measures of the precision of a standard measurement method*

— *Part 4: Basic methods for the determination of the trueness of a standard measurement method*

— *Part 5: Alternative methods for the determination of the precision of a standard measurement method*

— *Part 6: Use in practice of accuracy values*

Parts 1 to 6 of ISO 5725 together cancel and replace ISO 5725:1986, which has been extended to cover trueness (in addition to precision) and intermediate precision conditions (in addition to repeatability conditions and reproducibility conditions).

Annex A forms an integral part of this part of ISO 5725. Annexes B, C and D are for information only.

Introduction

0.1 This part of ISO 5725 uses two terms *trueness* and *precision* to describe the accuracy of a measurement method. *Trueness* refers to the closeness of agreement between the average value of a large number of test results and the true or accepted reference value. *Precision* refers to the closeness of agreement between test results.

0.2 General consideration of these quantities is given in ISO 5725-1 and so is not repeated here. This part of ISO 5725 should be read in conjunction with ISO 5725-1 because the underlying definitions and general principles are given there.

0.3 ISO 5725-2 is concerned with estimating, by means of interlaboratory experiments, standard measures of precision, namely the repeatability standard deviation and the reproducibility standard deviation. It gives a basic method for doing this using the uniform-level design. This part of ISO 5725 describes alternative methods to this basic method.

a) With the basic method there is a risk that an operator may allow the result of a measurement on one sample to influence the result of a subsequent measurement on another sample of the same material, causing the estimates of the repeatability and reproducibility standard deviations to be biased. When this risk is considered to be serious, the split-level design described in this part of ISO 5725 may be preferred as it reduces this risk.

b) The basic method requires the preparation of a number of identical samples of the material for use in the experiment. With heterogeneous materials this may not be possible, so that the use of the basic method then gives estimates of the reproducibility standard deviation that are inflated by the variation between the samples. The design for a heterogeneous material given in this part of ISO 5725 yields information about the variability between samples which is not obtainable from the basic method; it may be used to calculate an estimate of reproducibility from which the between-sample variation has been removed.

c) The basic method requires tests for outliers to be used to identify data that should be excluded from the calculation of the repeatability and reproducibility standard deviations. Excluding outliers can sometimes have a large effect on the estimates of repeatability and reproducibility standard deviations, but in practice, when applying the outlier tests, the data analyst may have to use judgement to decide which data to exclude. This part of ISO 5725 describes robust methods of data analysis that may be used to calculate repeatability and reproducibility standard deviations from data containing outliers without using tests for outliers to exclude data, so that the results are no longer affected by the data analyst's judgement.

Accuracy (trueness and precision) of measurement methods and results —

Part 5:
Alternative methods for the determination of the precision of a standard measurement method

1 Scope

This part of ISO 5725

— provides detailed descriptions of alternatives to the basic method for determining the repeatability and reproducibility standard deviations of a standard measurement method, namely the split-level design and a design for heterogeneous materials;

— describes the use of robust methods for analysing the results of precision experiments without using outlier tests to exclude data from the calculations, and in particular, the detailed use of one such method.

This part of ISO 5725 complements ISO 5725-2 by providing alternative designs that may be of more value in some situations than the basic design given in ISO 5725-2, and by providing a robust method of analysis that gives estimates of the repeatability and reproducibility standard deviations that are less dependent on the data analyst's judgement than those given by the methods described in ISO 5725-2.

2 Normative references

The following standards contain provisions which, through reference in this text, constitute provisions of this part of ISO 5725. At the time of publication, the editions indicated were valid. All standards are subject to revision, and parties to agreements based on this part of ISO 5725 are encouraged to investigate the possibility of applying the most recent editions of the standards indicated below. Members of IEC and ISO maintain registers of currently valid International Standards.

ISO 3534-1:1993, *Statistics — Vocabulary and symbols — Part 1: Probability and general statistical terms*.

ISO 3534-3:1985, *Statistics — Vocabulary and symbols — Part 3: Design of experiments*.

ISO 5725-1:1994, *Accuracy (trueness and precision) of measurement methods and results — Part 1: General principles and definitions*.

ISO 5725-2:1994, *Accuracy (trueness and precision) of measurement methods and results — Part 2: Basic method for the determination of repeatability and reproducibility of a standard measurement method.*

3 Definitions

For the purposes of this part of ISO 5725, the definitions given in ISO 3534-1 and in ISO 5725-1 apply.

The symbols used in ISO 5725 are given in annex A.

4 Split-level design

4.1 Applications of the split-level design

4.1.1 The uniform level design described in ISO 5725-2 requires two or more identical samples of a material to be tested in each participating laboratory and at each level of the experiment. With this design there is a risk that an operator may allow the result of a measurement on one sample to influence the result of a subsequent measurement on another sample of the same material. If this happens, the results of the precision experiment will be distorted: estimates of the repeatability standard deviation σ_r will be decreased and estimates of the between-laboratory standard deviation σ_L will be increased. In the split-level design, each participating laboratory is provided with a sample of each of two similar materials, at each level of the experiment, and the operators are told that the samples are not identical, but they are not told by how much the materials differ. The split-level design thus provides a method of determining the repeatability and reproducibility standard deviations of a standard measurement method in a way that reduces the risk that a test result obtained on one sample will influence a test result on another sample in the experiment.

4.1.2 The data obtained at a level of a split-level experiment may be used to draw a graph in which the data for one material are plotted against the data for the other, similar, material. An example is given in figure 1. Such graphs can help identify those laboratories that have the largest biases relative to the other laboratories. This is useful when it is possible to investigate the causes of the largest laboratory biases with the aim of taking corrective action.

4.1.3 It is common for the repeatability and reproducibility standard deviations of a measurement method to depend on the level of the material. For example, when the test result is the proportion of an element obtained by chemical analysis, the repeatability and reproducibility standard deviations usually increase as the proportion of the element increases. It is necessary, for a split-level experiment, that the two similar materials used at a level of the experiment are so similar that they can be expected to give the same repeatability and reproducibility standard deviations. For the purposes of the split-level design, it is acceptable if the two materials used for a level of the experiment give almost the same level of measurement results, and nothing is to be gained by arranging that they differ substantially.

In many chemical analysis methods, the matrix containing the constituent of interest can influence the precision, so for a split-level experiment two materials with similar matrices are required at each level of the experiment. A sufficiently similar material can sometimes be prepared by spiking a material with a small addition of the constituent of interest. When the material is a natural or manufactured product, it can be difficult to find two products that are sufficiently similar for the purposes of a split-level experiment: a possible solution may be to use two batches of the same product. It should be remembered that the object of choosing the materials for the split-level design is to provide the operators with samples that they do not expect to be identical.

4.2 Layout of the split-level design

4.2.1 The layout of the split-level design is shown in table 1.

The p participating laboratories each test two samples at q levels.

The two samples within a level are denoted a and b, where a represents a sample of one material, and b represents a sample of the other, similar, material.

4.2.2 The data from a split-level experiment are represented by:

y_{ijk}

where

subscript i represents the laboratory (i = 1, 2, ..., p);

subscript j represents the level (j = 1, 2, ..., q);

subscript k represents the sample (k = a or b).

4.3 Organization of a split-level experiment

4.3.1 Follow the guidance given in clause 6 of ISO 5725-1:1994 when planning a split-level experiment.

Subclause 6.3 of ISO 5725-1:1994 contains a number of formulae (involving a quantity denoted generally by A) that are used to help decide how many laboratories to include in the experiment. The corresponding formulae for the split-level experiment are set out below.

NOTE — These formulae have been derived by the method described in NOTE 24 of ISO 5725-1:1994.

To assess the uncertainties of the estimates of the repeatability and reproducibility standard deviations, calculate the following quantities.

For repeatability

$$A_r = 1{,}96\sqrt{1/[2(p-1)]} \qquad (1)$$

For reproducibility

$$A_R = 1{,}96\sqrt{\left\{\left[1+2\left(\gamma^2-1\right)\right]^2+1\right\}/\left[8\gamma^4(p-1)\right]} \qquad (2)$$

with $\gamma = \sigma_R/\sigma_r$.

If the number n of replicates is taken as two in equations (9) and (10) of ISO 5725-1:1994, then it can be seen that equations (9) and (10) of ISO 5725-1:1994 are the same as equations (1) and (2) above, except that sometimes $p - 1$ appears here in place of p in ISO 5725-1:1994. This is a small difference, so table 1 and figures B.1 and B.2 of ISO 5725-1:1994 may be used to assess the uncertainty of the estimates of the repeatability and reproducibility standard deviations in a split-level experiment.

To assess the uncertainty of the estimate of the bias of the measurement method in a split-level experiment, calculate the quantity A as defined by equation (13) of ISO 5725-1:1994 with n = 2 (or use table 2 of ISO 5725-1:1994), and use this quantity as described in ISO 5725-1.

To assess the uncertainty of the estimate of a laboratory bias in a split-level experiment, calculate the quantity A_w as defined by equation (16) of ISO 5725-1:1994 with n = 2. Because the number of replicates in a split-level experiment is, in effect, this number of two, it is not possible to reduce the uncertainty of the estimate of laboratory bias by increasing the number of replicates. (If it is necessary to reduce this uncertainty, the uniform-level design should be used instead.)

4.3.2 Follow the guidance given in clauses 5 and 6 of ISO 5725-2:1994 with regard to the details of the organization of a split-level experiment. The number of replicates, n in ISO 5725-2, may be taken to be the number of split-levels in a split-level design, i.e. two.

The a samples should be allocated to the participants at random, and the b samples should also be allocated to the participants at random and in a separate randomization operation.

It is necessary in a split-level experiment for the statistical expert to be able to tell, when the data are reported, which result was obtained on material *a* and which on material *b*, at each level of the experiment. Label the samples so that this is possible, and be careful not to disclose this information to the participants.

Table 1 — Recommended form for the collation of data for the split-level design

Laboratory	Level									
	1		2			*j*			*q*	
	a	*b*	*a*	*b*		*a*	*b*		*a*	*b*
1										
2										
i										
p										

4.4 Statistical model

4.4.1 The basic model used in this part of ISO 5725 is given as equation (1) in clause 5 of ISO 5725-1:1994. It is stated there that for estimating the accuracy (trueness and precision) of a measurement method, it is useful to assume that every measurement result is the sum of three components:

$$y_{ijk} = m_j + B_{ij} + e_{ijk} \quad (3)$$

where, for the particular material tested,

m_j represents the general average (expectation) at a particular level j = 1, ..., q;

B_{ij} represents the laboratory component of bias under repeatability conditions in a particular laboratory i = 1, ..., p at a particular level j = 1, ..., q;

e_{ijk} represents the random error of test result k = 1, ..., n , obtained in laboratory i at level j, under repeatability conditions.

4.4.2 For a split-level experiment, this model becomes:

$$y_{ijk} = m_{jk} + B_{ij} + e_{ijk} \quad (4)$$

This differs from equation (3) in 4.4.1 in only one feature: the subscript k in m_{jk} implies that according to equation (4) the general average may now depend on the material *a* or *b* (k = 1 or 2) within the level j.

The lack of a subscript k in B_{ij} implies that it is assumed that the bias associated with a laboratory i does not depend on the material *a* or *b* within a level. This is why it is important that the two materials should be similar.

4.4.3 Define the cell averages as:

$$y_{ij} = (y_{ija} + y_{ijb}) / 2 \quad (5)$$

and the cell differences as:

$$D_{ij} = y_{ija} - y_{ijb} \quad (6)$$

4.4.4 The general average for a level j of a split-level experiment may be defined as:

$$m_j = (m_{ja} + m_{jb}) / 2 \quad (7)$$

4.5 Statistical analysis of the data from a split-level experiment

4.5.1 Assemble the data into a table as shown in table 1. Each combination of a laboratory and a level gives a "cell" in this table, containing two items of data, y_{ija} and y_{ijb}.

Calculate the cell differences D_{ij} and enter them into a table as shown in table 2. The method of analysis requires each difference to be calculated in the same sense

$$a - b$$

and the sign of the difference to be retained.

Calculate the cell averages y_{ij} and enter them into a table as shown in table 3.

4.5.2 If a cell in table 1 does not contain two test results (for example, because samples have been spoilt, or data have been excluded following the application of the outlier tests described later) then the corresponding cells in tables 2 and 3 both remain empty.

4.5.3 For each level j of the experiment, calculate the average D_j and standard deviation s_{Dj} of the differences in column j of table 2:

$$D_j = \sum D_{ij} / p \quad (8)$$

$$s_{Dj} = \sqrt{\sum \left(D_{ij} - D_j\right)^2 / (p-1)} \quad (9)$$

Here, Σ represents summation over the laboratories i = 1, 2, ..., p.

If there are empty cells in table 2, p is now the number of cells in column j of table 2 containing data and the summation is performed over non-empty cells.

4.5.4 For each level j of the experiment, calculate the average y_j and standard deviation s_{yj} of the averages in column j of table 3, using:

$$y_j = \sum y_{ij} / p \quad (10)$$

$$s_{yj} = \sqrt{\sum \left(y_{ij} - y_j\right)^2 / (p-1)} \quad (11)$$

Here, Σ represents summation over the laboratories i = 1, 2, ..., p.

If there are empty cells in table 3, p is now the number of cells in column j of table 3 containing data and the summation is performed over non-empty cells.

4.5.5 Use tables 2 and 3 and the statistics calculated in 4.5.3 and 4.5.4 to examine the data for consistency and outliers, as described in 4.6. If data are rejected, recalculate the statistics.

4.5.6 Calculate the repeatability standard deviation s_{rj} and the reproducibility standard deviation s_{Rj} from:

$$s_{rj} = s_{Dj} \Big/ \sqrt{2} \tag{12}$$

$$s_{Rj}^2 = s_{yj}^2 + s_{rj}^2 \Big/ 2 \tag{13}$$

4.5.7 Investigate whether s_{rj} and s_{Rj} depend on the average y_j, and, if so, determine the functional relationships, using the methods described in subclause 7.5 of ISO 5725-2:1994.

Table 2 — Recommended form for tabulation of cell differences for the split-level design

Laboratory	Level					
	1	2		*j*		*q*
1						
2						
i						
p						

Table 3 — Recommended form for tabulation of cell averages for the split-level design

Laboratory	Level					
	1	2		*j*		*q*
1						
2						
i						
p						

4.6 Scrutiny of the data for consistency and outliers

4.6.1 Examine the data for consistency using the *h* statistics, described in subclause 7.3.1 of ISO 5725-2:1994.

To check the consistency of the cell differences, calculate the *h* statistics as:

$$h_{ij} = \left(D_{ij} - D_j\right) \Big/ s_{Dj} \tag{14}$$

To check the consistency of the cell averages, calculate the h statistics as:

$$h_{ij} = \left(y_{ij} - y_j\right) \Big/ s_{yj} \qquad (15)$$

To show up inconsistent laboratories, plot both sets of these statistics in the order of the levels, but grouped by laboratory, as shown in figures 2 and 3. The interpretation of these graphs is discussed fully in subclause 7.3.1 of ISO 5725-2:1994. If a laboratory is achieving generally worse repeatability than the others, then it will show up as having an unusually large number of large h statistics in the graph derived from the cell differences. If a laboratory is achieving results that are generally biased, then it will show up as having h statistics mostly in one direction on the graph derived from the cell averages. In either case, the laboratory should be asked to investigate and report their findings back to the organizer of the experiment.

4.6.2 Examine the data for stragglers and outliers using Grubbs' tests, described in subclause 7.3.4 of ISO 5725-2:1994.

To test for stragglers and outliers in the cell differences, apply Grubbs' tests to the values in each column of table 2 in turn.

To test for stragglers and outliers in the cell averages, apply Grubbs' tests to the values in each column of table 3 in turn.

The interpretation of these tests is discussed fully in subclause 7.3.2 of ISO 5725-2:1994. They are used to identify results that are so inconsistent with the remainder of the data reported in the experiment that their inclusion in the calculation of the repeatability and reproducibility standard deviations would affect the values of these statistics substantially. Usually, data shown to be outliers are excluded from the calculations, and data shown to be stragglers are included, unless there is a good reason for doing otherwise. If the tests show that a value in one of tables 2 or 3 is to be excluded from the calculation of the repeatability and reproducibility standard deviations, then the corresponding value in the other of these tables should also be excluded from the calculation.

4.7 Reporting the results of a split-level experiment

4.7.1 Advice is given in subclause 7.7 of ISO 5725-2:1994 on:

— reporting the results of the statistical analysis to the panel;

— decisions to be made by the panel; and

— the preparation of a full report.

4.7.2 Recommendations on the form of a published statement of the repeatability and reproducibility standard deviations of a standard measurement method are given in subclause 7.1 of ISO 5725-1:1994.

4.8 Example 1: A split-level experiment — Determination of protein

4.8.1 Table 4 contains the data from an experiment [5] which involved the determination by combustion of the content of protein in feeds. There were nine participating laboratories, and the experiment contained 14 levels. Within each level, two feeds were used having similar mass fraction of protein in feed.

4.8.2 Tables 5 and 6 show the cell averages and differences, calculated as described in clause 4.5.1, for just Level 14 (j = 14) of the experiment.

Using equations (8) and (9) in 4.5.3, the differences in table 5 give:

D_{14} = 8,34 %

s_{D14} = 0,436 1 %

and applying equations (10) and (11) in 4.5.4 to the averages in table 6 gives:

y_{14} = 85,46 %

s_{Y14} = 0,453 4 %

so the repeatability and reproducibility standard deviations are, using equations (12) and (13) in 4.5.6:

s_{r14} = 0,31 %

s_{R14} = 0,50 %

Table 7 gives the results of the calculations for the other levels.

4.8.3 Figure 1 shows the results for samples a from table 4 plotted against the corresponding results for samples b, for Level 14, in a “Youden plot”. Laboratory 5 gives a point in the bottom left-hand corner of the graph, and Laboratory 1 gives a point in the top right-hand corner: this indicates that the data from Laboratory 5 have a consistent negative bias over samples a and b, and that the data from Laboratory 1 have a consistent positive bias over the two samples. It is common to find this sort of pattern when plotting the data from a split-level design as in figure 1. The figure also shows that the results for Laboratory 4 are unusual, as the point for this laboratory is some distance from the line of equality for the two samples. The other laboratories form a group in the middle of the plot. This figure thus provides a case for investigating the causes of the biases at the three laboratories.

NOTE — For further information on the interpretation of “Youden plots”, see references [7] and [8].

4.8.4 The values of the h statistics, calculated as described in 4.6.1, are shown in tables 5 and 6, for only Level 14. The values for all levels are plotted in figures 2 and 3.

In figure 3, the h statistics for cell averages show that Laboratory 5 gave negative h statistics at all levels, indicating a consistent negative bias in their data. In the same figure, Laboratories 8 and 9 gave h statistics that are nearly all positive, indicating consistent positive biases in their data (but smaller than the negative bias in Laboratory 5). Also, the h statistics for Laboratories 1, 2 and 6 indicate a bias that changes with level in each of these laboratories. Such interactions between the laboratories and the levels may provide clues as to the causes of the laboratory biases.

Figure 2 does not reveal any noteworthy pattern.

4.8.5 Values of the Grubbs' statistics are given in table 8. These tests again indicate that the data from Laboratory 5 are suspect.

4.8.6 At this point in the analysis, the statistical expert should initiate an investigation at Laboratory 5 of the possible causes of the suspect data, before proceeding with the analysis of the data. If the cause cannot be identified, there is a case in this instance for excluding all data from Laboratory 5 from the calculation of the repeatability and reproducibility standard deviations. The analysis would then continue with an investigation of possible functional relationships between the repeatability and reproducibility standard deviations and the general average. This does not raise any issues that have not already been covered in ISO 5725-2, so it will not be considered here.

Table 4 — Example 1: Determination of mass fraction of protein in feed, expressed as a percentage

Laboratory	Level									
	1		2		3		4		5	
	a	*b*	*a*	*b*	*a*	*b*	*a*	*b*	*a*	*b*
1	11,11	10,34	10,91	9,81	13,74	13,48	13,79	13,00	15,89	15,26
2	11,12	9,94	11,38	10,31	14,00	13,12	13,44	13,06	15,69	15,10
3	11,26	10,46	10,95	10,51	13,38	12,70	13,54	13,18	15,83	15,73
4	11,07	10,41	11,66	9,95	13,01	13,16	13,58	12,88	15,08	15,63
5	10,69	10,31	10,98	10,13	13,24	13,33	13,32	12,59	15,02	14,90
6	11,73	11,01	12,31	10,92	14,01	13,66	14,04	13,64	16,43	15,94
7	11,13	10,36	11,38	10,44	12,94	12,44	13,63	13,06	15,75	15,56
8	11,21	10,51	11,32	10,84	13,09	13,76	13,85	13,49	15,98	15,89
9	11,80	11,21	11,35	9,88	13,85	14,46	13,96	13,77	16,51	15,72
Laboratory	**Level**									
	6		7		8		9		10	
	a	*b*	*a*	*b*	*a*	*b*	*a*	*b*	*a*	*b*
1	20,14	19,78	20,33	20,06	46,45	44,42	52,05	49,40	65,84	59,14
2	19,25	20,25	20,36	19,94	46,69	44,62	51,94	48,81	66,31	59,19
3	20,48	19,86	20,56	20,11	46,90	44,56	52,18	48,90	66,06	58,52
4	21,54	20,06	20,64	20,46	47,13	45,29	51,73	48,56	65,93	58,93
5	19,90	19,66	20,56	19,24	45,83	43,73	50,84	47,91	64,19	57,94
6	20,31	20,27	20,85	20,63	46,86	43,96	52,18	49,03	65,73	58,77
7	20,00	20,56	20,25	20,19	46,25	44,31	52,25	49,44	66,06	59,19
8	20,43	20,69	20,85	20,27	47,11	44,40	52,44	48,81	65,66	59,38
9	20,64	21,01	20,78	20,89	47,09	45,15	52,19	48,46	66,33	59,47
Laboratory	**Level**									
	11		12		13		14			
	a	*b*	*a*	*b*	*a*	*b*	*a*	*b*		
1	84,16	80,86	85,38	81,71	87,64	88,23	90,24	82,10		
2	84,50	81,06	85,56	82,44	88,81	88,38	89,88	81,44		
3	82,26	79,43	85,26	82,15	88,58	88,12	89,48	81,67		
4	84,39	80,08	85,20	81,76	88,47	87,98	90,04	80,73		
5	81,71	79,01	83,58	79,74	86,43	86,19	88,59	80,46		
6	82,85	81,16	84,44	80,90	87,78	86,89	89,40	80,88		
7	86,25	81,00	84,88	81,44	88,06	88,00	89,31	81,38		
8	84,59	81,16	84,96	81,71	88,50	87,98	89,94	81,56		
9	83,05	80,93	84,73	81,94	88,24	88,05	89,75	81,35		