

INTERNATIONAL STANDARD

NORME INTERNATIONALE

**Short-circuit currents in three-phase AC systems –
Part 3: Currents during two separate simultaneous line-to-earth short circuits
and partial short-circuit currents flowing through earth**

**Courants de court-circuit dans les réseaux triphasés à courant alternatif –
Partie 3: Courants durant deux courts-circuits monophasés simultanés séparés
à la terre et courants de court-circuit partiels s'écoulant à travers la terre**



THIS PUBLICATION IS COPYRIGHT PROTECTED

Copyright © 2009 IEC, Geneva, Switzerland

All rights reserved. Unless otherwise specified, no part of this publication may be reproduced or utilized in any form or by any means, electronic or mechanical, including photocopying and microfilm, without permission in writing from either IEC or IEC's member National Committee in the country of the requester.

If you have any questions about IEC copyright or have an enquiry about obtaining additional rights to this publication, please contact the address below or your local IEC member National Committee for further information.

Droits de reproduction réservés. Sauf indication contraire, aucune partie de cette publication ne peut être reproduite ni utilisée sous quelque forme que ce soit et par aucun procédé, électronique ou mécanique, y compris la photocopie et les microfilms, sans l'accord écrit de la CEI ou du Comité national de la CEI du pays du demandeur.

Si vous avez des questions sur le copyright de la CEI ou si vous désirez obtenir des droits supplémentaires sur cette publication, utilisez les coordonnées ci-après ou contactez le Comité national de la CEI de votre pays de résidence.

IEC Central Office
3, rue de Varembe
CH-1211 Geneva 20
Switzerland
Email: inmail@iec.ch
Web: www.iec.ch

About the IEC

The International Electrotechnical Commission (IEC) is the leading global organization that prepares and publishes International Standards for all electrical, electronic and related technologies.

About IEC publications

The technical content of IEC publications is kept under constant review by the IEC. Please make sure that you have the latest edition, a corrigenda or an amendment might have been published.

- Catalogue of IEC publications: www.iec.ch/searchpub

The IEC on-line Catalogue enables you to search by a variety of criteria (reference number, text, technical committee,...). It also gives information on projects, withdrawn and replaced publications.

- IEC Just Published: www.iec.ch/online_news/justpub

Stay up to date on all new IEC publications. Just Published details twice a month all new publications released. Available on-line and also by email.

- Electropedia: www.electropedia.org

The world's leading online dictionary of electronic and electrical terms containing more than 20 000 terms and definitions in English and French, with equivalent terms in additional languages. Also known as the International Electrotechnical Vocabulary online.

- Customer Service Centre: www.iec.ch/webstore/custserv

If you wish to give us your feedback on this publication or need further assistance, please visit the Customer Service Centre FAQ or contact us:

Email: csc@iec.ch
Tel.: +41 22 919 02 11
Fax: +41 22 919 03 00

A propos de la CEI

La Commission Electrotechnique Internationale (CEI) est la première organisation mondiale qui élabore et publie des normes internationales pour tout ce qui a trait à l'électricité, à l'électronique et aux technologies apparentées.

A propos des publications CEI

Le contenu technique des publications de la CEI est constamment revu. Veuillez vous assurer que vous possédez l'édition la plus récente, un corrigendum ou amendement peut avoir été publié.

- Catalogue des publications de la CEI: www.iec.ch/searchpub/cur_fut-f.htm

Le Catalogue en-ligne de la CEI vous permet d'effectuer des recherches en utilisant différents critères (numéro de référence, texte, comité d'études,...). Il donne aussi des informations sur les projets et les publications retirées ou remplacées.

- Just Published CEI: www.iec.ch/online_news/justpub

Restez informé sur les nouvelles publications de la CEI. Just Published détaille deux fois par mois les nouvelles publications parues. Disponible en-ligne et aussi par email.

- Electropedia: www.electropedia.org

Le premier dictionnaire en ligne au monde de termes électroniques et électriques. Il contient plus de 20 000 termes et définitions en anglais et en français, ainsi que les termes équivalents dans les langues additionnelles. Egalement appelé Vocabulaire Electrotechnique International en ligne.

- Service Clients: www.iec.ch/webstore/custserv/custserv_entry-f.htm

Si vous désirez nous donner des commentaires sur cette publication ou si vous avez des questions, visitez le FAQ du Service clients ou contactez-nous:

Email: csc@iec.ch
Tél.: +41 22 919 02 11
Fax: +41 22 919 03 00

INTERNATIONAL STANDARD

NORME INTERNATIONALE

**Short-circuit currents in three-phase AC systems –
Part 3: Currents during two separate simultaneous line-to-earth short circuits
and partial short-circuit currents flowing through earth**

**Courants de court-circuit dans les réseaux triphasés à courant alternatif –
Partie 3: Courants durant deux courts-circuits monophasés simultanés séparés
à la terre et courants de court-circuit partiels s'écoulant à travers la terre**

INTERNATIONAL
ELECTROTECHNICAL
COMMISSION

COMMISSION
ELECTROTECHNIQUE
INTERNATIONALE

PRICE CODE
CODE PRIX

XA

ICS 17.220.01; 29.240.20

ISBN 978-2-88910-328-7

CONTENTS

FOREWORD.....	5
1 Scope and object.....	7
2 Normative references	8
3 Terms and definitions	8
4 Symbols	10
5 Calculation of currents during two separate simultaneous line-to-earth short circuits	12
5.1 Initial symmetrical short-circuit current	12
5.1.1 Determination of $\underline{M}_{(1)}$ and $\underline{M}_{(2)}$	12
5.1.2 Simple cases of two separate simultaneous line-to-earth short circuits.....	13
5.2 Peak short-circuit current, symmetrical short circuit breaking current and steady-state short-circuit current	13
5.3 Distribution of the currents during two separate simultaneous line-to-earth short circuits.....	14
6 Calculation of partial short-circuit currents flowing through earth in case of an unbalanced short circuit.....	14
6.1 General.....	14
6.2 Line-to-earth short circuit inside a station	15
6.3 Line-to-earth short circuit outside a station.....	16
6.4 Line-to-earth short circuit in the vicinity of a station	18
6.4.1 Earth potential \underline{U}_{ETn} at the tower n outside station B	19
6.4.2 Earth potential of station B during a line-to earth short circuit at the tower n	19
7 Reduction factor for overhead lines with earth wires	20
8 Calculation of current distribution and reduction factor in case of cables with metallic sheath or shield earthed at both ends	21
8.1 Overview	21
8.2 Three-core cable	22
8.2.1 Line-to-earth short circuit in station B	22
8.2.2 Line-to-earth short circuit on the cable between station A and station B	23
8.3 Three single-core cables	26
8.3.1 Line-to-earth short circuit in station B	26
8.3.2 Line-to-earth short circuit on the cable between station A and station B	26
Annex A (informative) Example for the calculation of two separate simultaneous line-to-earth short-circuit currents.....	30
Annex B (informative) Examples for the calculation of partial short-circuit currents through earth	33
Annex C (informative) Example for the calculation of the reduction factor r_1 and the current distribution through earth in case of a three-core cable	43
Annex D (informative) Example for the calculation of the reduction factor r_3 and the current distribution through earth in case of three single-core cables	48

Figure 1 – Driving point impedance \underline{Z}_P of an infinite chain, composed of the earth wire impedance $\underline{Z}_Q = \underline{Z}'_Q d_T$ and the footing resistance R_T of the towers, with equal distances d_T between the towers	9
Figure 2 – Driving point impedance \underline{Z}_{Pn} of a finite chain with n towers, composed of the earth wire impedance $\underline{Z}_Q = \underline{Z}'_Q d_T$, the footing resistance R_T of the towers, with equal distances d_T between the towers and the earthing impedance \underline{Z}_{EB} of station B from Equation (29)	10
Figure 3 – Characterisation of two separate simultaneous line-to earth short circuits and the currents I_{KEE}''	12
Figure 4 – Partial short-circuit currents in case of a line-to-earth short circuit inside station B	15
Figure 5 – Partial short-circuit currents in case of a line-to-earth short circuit at a tower T of an overhead line	16
Figure 6 – Distribution of the total current to earth \underline{I}_{ETtot}	17
Figure 7 – Partial short-circuit currents in the case of a line-to-earth short circuit at a tower n of an overhead line in the vicinity of station B	18
Figure 8 – Reduction factor r for overhead lines with non-magnetic earth wires depending on soil resistivity ρ	21
Figure 9 – Reduction factor of three-core power cables	23
Figure 10 – Reduction factors for three single-core power cables	27
Figure A.1 – Two separate simultaneous line-to earth short circuits on a single fed overhead line (see Table 1)	30
Figure B.1 – Line-to-earth short circuit inside station B – System diagram for stations A, B and C	34
Figure B.2 – Line-to-earth short circuit inside station B – Positive-, negative- and zero-sequence systems with connections at the short-circuit location F within station B	34
Figure B.3 – Line-to-earth short circuit outside stations B and C at the tower T of an overhead line – System diagram for stations A, B and C	36
Figure B.4 – Line-to-earth short circuit outside stations B and C at the tower T of an overhead line – Positive-, negative- and zero-sequence systems with connections at the short-circuit location F	37
Figure B.5 – Earth potentials $u_{ETn} = U_{ETn}/U_{ET}$ with $U_{ET} = 1,912$ kV and $u_{EBn} = U_{EBn}/U_{EB}$ with $U_{EB} = 0,972$ kV, if the line-to-earth short circuit occurs at the towers $n = 1, 2, 3, \dots$ in the vicinity of station B	42
Figure C.1 – Example for the calculation of the cable reduction factor and the current distribution through earth in a 10-kV-network, $U_n = 10$ kV; $c = 1,1$; $f = 50$ Hz	44
Figure C.2 – Short-circuit currents and partial short-circuit currents through earth for the example in Figure C.1	45
Figure C.3 – Example for the calculation of current distribution in a 10-kV-network with a short circuit on the cable between A and B (data given in C.2.1 and Figure C.1)	46
Figure C.4 – Line-to-earth short-circuit currents, partial currents in the shield and partial currents through earth	47
Figure D.1 – Example for the calculation of the reduction factor and the current distribution in case of three single-core cables and a line-to-earth short circuit in station B	49
Figure D.2 – Positive-, negative- and zero-sequence system of the network in Figure D.1 with connections at the short-circuit location (station B)	50
Figure D.3 – Current distribution for the network in Figure D.1, depending on the length, ℓ , of the single-core cables between the stations A and B	51

Figure D.4 – Example for the calculation of the reduction factors r_3 and the current distribution in case of three single-core cables and a line-to-earth short circuit between the stations A and B	52
Figure D.5 – Positive-, negative- and zero-sequence system of the network in Figure D.4 with connections at the short-circuit location (anywhere between the stations A and B)	52
Figure D.6 – Current distribution for the cable in Figure D.4 depending on ℓ_A , $R_{EF} \rightarrow \infty$	54
Figure D.7 – Current distribution for the cable in Figure D.4 depending on ℓ_A , $R_{EF} = 5 \Omega$	56
Table 1 – Calculation of initial line-to-earth short-circuit currents in simple cases	13
Table 2 – Resistivity of the soil and equivalent earth penetration depth	20
Table C.1 – Results for the example in Figure C.1	45
Table C.2 – Results for the example in Figure C.3, $\ell = 5$ km	47
Table C.3 – Results for the example in Figure C.3, $\ell = 10$ km	47

iTeh STANDARD PREVIEW (standards.iteh.ai)

IEC 60909-3:2009

<https://standards.iteh.ai/catalog/standards/sist/6a4bc3ab-2e41-4046-8067-c5c558ea1ab5/iec-60909-3-2009>

INTERNATIONAL ELECTROTECHNICAL COMMISSION

SHORT-CIRCUIT CURRENTS IN THREE-PHASE AC SYSTEMS –**Part 3: Currents during two separate simultaneous
line-to-earth short circuits and partial short-circuit
currents flowing through earth**

FOREWORD

- 1) The International Electrotechnical Commission (IEC) is a worldwide organization for standardization comprising all national electrotechnical committees (IEC National Committees). The object of IEC is to promote international co-operation on all questions concerning standardization in the electrical and electronic fields. To this end and in addition to other activities, IEC publishes International Standards, Technical Specifications, Technical Reports, Publicly Available Specifications (PAS) and Guides (hereafter referred to as "IEC Publication(s)"). Their preparation is entrusted to technical committees; any IEC National Committee interested in the subject dealt with may participate in this preparatory work. International, governmental and non-governmental organizations liaising with the IEC also participate in this preparation. IEC collaborates closely with the International Organization for Standardization (ISO) in accordance with conditions determined by agreement between the two organizations.
- 2) The formal decisions or agreements of IEC on technical matters express, as nearly as possible, an international consensus of opinion on the relevant subjects since each technical committee has representation from all interested IEC National Committees.
- 3) IEC Publications have the form of recommendations for international use and are accepted by IEC National Committees in that sense. While all reasonable efforts are made to ensure that the technical content of IEC Publications is accurate, IEC cannot be held responsible for the way in which they are used or for any misinterpretation by any end user.
- 4) In order to promote international uniformity, IEC National Committees undertake to apply IEC Publications transparently to the maximum extent possible in their national and regional publications. Any divergence between any IEC Publication and the corresponding national or regional publication shall be clearly indicated in the latter.
- 5) IEC provides no marking procedure to indicate its approval and cannot be rendered responsible for any equipment declared to be in conformity with an IEC Publication.
- 6) All users should ensure that they have the latest edition of this publication.
- 7) No liability shall attach to IEC or its directors, employees, servants or agents including individual experts and members of its technical committees and IEC National Committees for any personal injury, property damage or other damage of any nature whatsoever, whether direct or indirect, or for costs (including legal fees) and expenses arising out of the publication, use of, or reliance upon, this IEC Publication or any other IEC Publications.
- 8) Attention is drawn to the Normative references cited in this publication. Use of the referenced publications is indispensable for the correct application of this publication.
- 9) Attention is drawn to the possibility that some of the elements of this IEC Publication may be the subject of patent rights. IEC shall not be held responsible for identifying any or all such patent rights.

International Standard IEC 60909-3 has been prepared by IEC technical committee 73: Short-circuit currents.

This International Standard is to be read in conjunction with IEC 60909-0.

This third edition cancels and replaces the second edition published in 2003. This edition constitutes a technical revision.

The main changes with respect to the previous edition are listed below:

- New procedures are introduced for the calculation of reduction factors of the sheaths or shields and in addition the current distribution through earth and the sheaths or shields of three-core cables or of three single-core cables with metallic non-magnetic sheaths or shields earthed at both ends;
- The information for the calculation of the reduction factor of overhead lines with earth wires are corrected and given in the new Clause 7;

- A new Clause 8 is introduced for the calculation of current distribution and reduction factor of three-core cables with metallic sheath or shield earthed at both ends;
- The new Annexes C and D provide examples for the calculation of reduction factors and current distribution in case of cables with metallic sheath and shield earthed at both ends.

The text of this standard is based on the following documents:

FDIS	Report on voting
73/148/FDIS	73/149/RVD

Full information on the voting for the approval of this standard can be found in the report on voting indicated in the above table.

This publication has been drafted in accordance with the ISO/IEC Directives, Part 2.

A list of all parts of the IEC 60909 series, published under the general title *Short-circuit currents in three-phase a.c. systems*, can be found on the IEC website.

The committee has decided that the contents of this publication will remain unchanged until the maintenance result date indicated on the IEC web site under "<http://webstore.iec.ch>" in the data related to the specific publication. At this date, the publication will be

- reconfirmed,
- withdrawn,
- replaced by a revised edition, or
- amended.

iTeh STANDARD PREVIEW
(standards.iteh.ai)

IEC 60909-3:2009

The contents of the corrigendum of September 2013 have been included in this copy.

<http://standards.iteh.ai/en/standards/iec/60909-3-2009>
c5c558ea1ab5/iec-60909-3-2009

SHORT-CIRCUIT CURRENTS IN THREE-PHASE AC SYSTEMS –

Part 3: Currents during two separate simultaneous line-to-earth short circuits and partial short-circuit currents flowing through earth

1 Scope and object

This part of IEC 60909 specifies procedures for calculation of the prospective short-circuit currents with an unbalanced short circuit in high-voltage three-phase a.c. systems operating at nominal frequency 50 Hz or 60 Hz, i. e.:

- a) currents during two separate simultaneous line-to-earth short circuits in isolated neutral or resonant earthed neutral systems;
- b) partial short-circuit currents flowing through earth in case of single line-to-earth short circuit in solidly earthed or low-impedance earthed neutral systems.

The currents calculated by these procedures are used when determining induced voltages or touch or step voltages and rise of earth potential at a station (power station or substation) and the towers of overhead lines.

Procedures are given for the calculation of reduction factors of overhead lines with one or two earth wires.

The standard does not cover:

- a) short-circuit currents deliberately created under controlled conditions as in short circuit testing stations, or
- b) short-circuit currents in the electrical installations on board ships or aeroplanes, or
- c) single line-to-earth fault currents in isolated or resonant earthed systems.

The object of this standard is to establish practical and concise procedures for the calculation of line-to-earth short-circuit currents during two separate simultaneous line-to-earth short circuits and partial short-circuit currents through earth, earth wires of overhead lines and sheaths or shields of cables leading to conservative results with sufficient accuracy. For this purpose, the short-circuit currents are determined by considering an equivalent voltage source at the short-circuit location with all other voltage sources set to zero. Resistances of earth grids in stations or footing resistances of overhead line towers are neglected, when calculating the short-circuit currents at the short-circuit location.

This standard is an addition to IEC 60909-0. General definitions, symbols and calculation assumptions refer to that publication. Special items only are defined or specified in this standard.

The calculation of the short-circuit currents based on the rated data of the electrical equipment and the topological arrangement of the system has the advantage of being possible both for existing systems and for systems at the planning stage. The procedure is suitable for determination by manual methods or digital computation. This does not exclude the use of special methods, for example the super-position method, adjusted to particular circumstances, if they give at least the same precision.

As stated in IEC 60909-0, short-circuit currents and their parameters may also be determined by system tests.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

IEC 60909-0:2001, *Short-circuit currents in three-phase a.c. systems – Part 0: Calculation of currents*

IEC/TR 60909-2:2008, *Short-circuit currents in three-phase a.c. systems – Part 2: Data of electrical equipment for short-circuit current calculations*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

3.1

two separate simultaneous line-to earth short circuits

line-to-earth short circuits at different locations at the same time on different conductors of a three-phase a.c. network having a resonant earthed or an isolated neutral

3.2

initial short-circuit currents during two separate simultaneous line-to-earth

short circuits I''_{KEE}

r.m.s value of the initial short-circuit currents flowing at both short-circuit locations with the same magnitude

[IEC 60909-3:2009](https://standards.iteh.ai/catalog/standards/sist/6a4bc3ab-2e41-4046-8067-5f58a1b57ec/iec-60909-3-2009)

3.3

partial short-circuit current through earth $I_{E\delta}$

r.m.s. value of the current flowing through earth in a fictive line in the equivalent earth penetration depth δ

NOTE In case of overhead lines remote from the short-circuit location and the earthing system of a station, where the distribution of the current between earthed conductors and earth is nearly constant, the current through earth depends on the reduction factor of the overhead line (Figures 4 and 5). In case of cables with metallic sheaths or shields, earthed at both ends in the stations A and B, current through earth between the stations A and B (Figures 9a) and 10a)), respectively between the short-circuit location and the stations A or B (Figures 9b) and 10b)).

3.4

total current to earth I_{ETot} at the short-circuit location on the tower T of an overhead line

r. m. s. value of the current flowing to earth through the footing resistance of an overhead line tower far away from a station connected with the driving point impedances of the overhead line at both sides, see Figure 5

3.5

total current to earth I_{EBtot} at the short-circuit location in the station B

r.m.s. value of the current flowing to earth through the earthing system of a station B (power station or substation) with connected earthed conductors (earth wires of overhead lines or sheaths or shields or armouring of cables or other earthed conductors as for instance metallic water pipes), see Figure 4

3.6

current to earth I_{ETn}

r.m.s. value of the current flowing to earth causing the potential rise at an overhead line tower n in the vicinity of a station

3.7

current to earth I_{EBn}

r.m.s. value of the current flowing to earth causing the potential rise U_{EBn} of a station B, in case of a line-to-earth short circuit at an overhead line tower n in the vicinity of the station B

3.8

reduction factor r

for overhead lines, which determines the part of the line-to-earth short-circuit current flowing through the earth remote from the short-circuit location and the earthing systems of the stations

3.9

reduction factor r_1

for three-core cables with metallic sheath or shield earthed at both ends

3.10

reduction factor r_3

for three single-core cables with metallic sheaths or shields earthed at both ends

3.11

driving point impedance Z_P of an infinite chain

composed of the earth-wire impedance Z_Q between two towers with earth return and the footing resistance R_T of the overhead line towers (Figure 1):

$$Z_P = 0,5Z_Q + \sqrt{(0,5Z_Q)^2 + R_T Z_Q} \quad (1)$$

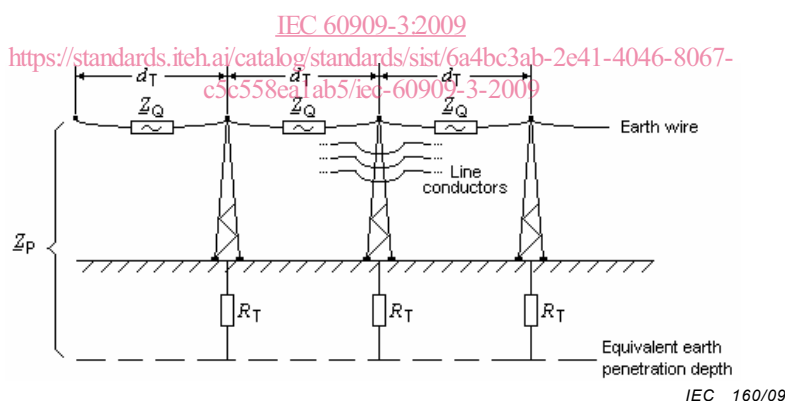


Figure 1 – Driving point impedance Z_P of an infinite chain, composed of the earth wire impedance $Z_Q = Z_Q d_T$ and the footing resistance R_T of the towers, with equal distances d_T between the towers

The driving point impedance Z_P can be assumed constant at a distance from the short-circuit location F longer than the far-from-station distance D_F defined by Equation (19).

3.12

driving point impedance Z_{Pn} of a finite chain

with n towers of an overhead line as given in Figure 2 and with the impedance Z_{EB} at the end, calculated according to Equation (2).

$$Z_{Pn} = \frac{Z_P (Z_{EB} + Z_P) k^n + (Z_P - Z_Q) (Z_{EB} - Z_P + Z_Q) k^{-n}}{(Z_{EB} + Z_P) k^n - (Z_{EB} - Z_P + Z_Q) k^{-n}} \quad (2)$$

with

$$\underline{k} = 1 + \frac{\underline{Z}_P}{R_T} \quad (3)$$

NOTE For $n \rightarrow \infty$, Equation (2) is leading to Equation (1). In practical cases, this is true already for $n \approx 10 \dots 15$.

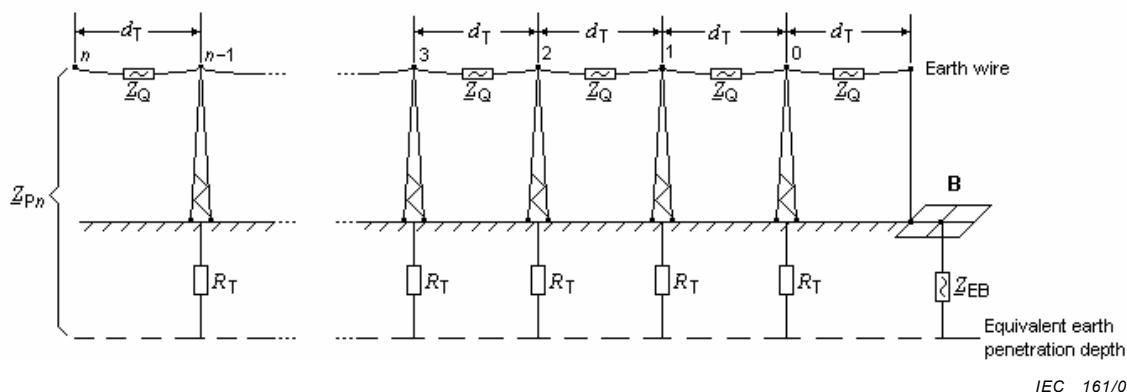


Figure 2 – Driving point impedance \underline{Z}_{Pn} of a finite chain with n towers, composed of the earth wire impedance $\underline{Z}_Q = \underline{Z}'_Q d_T$, the footing resistance R_T of the towers, with equal distances d_T between the towers and the earthing impedance \underline{Z}_{EB} of station B from Equation (29)

(standards.iteh.ai)

4 Symbols

IEC 60909-3:2009

All equations are written as quantity equations, in which the symbols represent physical quantities possessing both numerical values and dimensions. Symbols of complex quantities are underlined in the text and equations of this standard.

$cU_n / \sqrt{3}$	Equivalent voltage source (IEC 60909-0)
D_F	Far-from-station distance (Equation (19))
d_T	Distance between two towers
d_{L1L2}	Distance between the line conductors L1 and L2
d_{Q1Q2}	Distance between the earth wires Q1 and Q2
I_{bEE}	Short circuit breaking current in case of two separate simultaneous line-to-earth short circuits
I_E	Current flowing to earth (I_{EA} , I_{EB} , I_{EC} and I_{ET} in the Figures 4, 5, 7)
I_{EBn}	Current to earth in station B with a short-circuited tower n in the vicinity of station B (Figure 7)
I_{EBtot}	Total current to earth in the station B if a short circuit with earth connection occurs in station B (Figure 4)
I_{ETn}	Current to earth at the short-circuited tower n in the vicinity of a station (Figure 7)
I_{ETtot}	Total current to earth at a short-circuited tower T far away from stations (see Figure 5)
I_{KEE}''	Initial symmetrical short-circuit current in case of two separate simultaneous line-to-earth short circuits
I_{KE2E}''	Initial symmetrical short-circuit current flowing to earth in the case of a line-to-line short circuit with earth connection (IEC 60909-0)

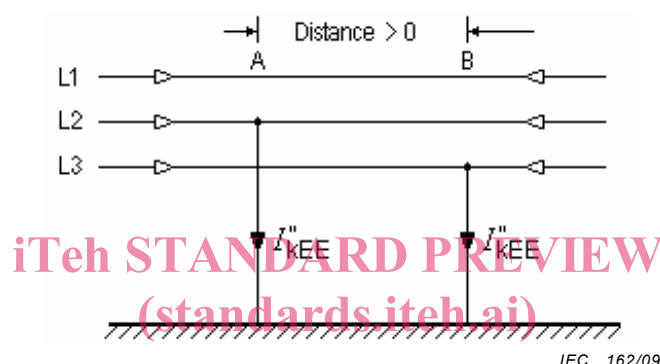
$I_{E\delta}$	Partial short-circuit current flowing through earth (for instance in Figure 4: $I_{E\delta A} = r_A \times 3I_{(0)A}$ or in Figure 9b): Current $I_{E\delta A}$ flowing back to the station A according to Equation (45))
I_Q	Earth wire current
I_S	Current in the sheath or shield of a cable (in case of three single-core cables: I_{S1} , I_{S2} and I_{S3})
I_T	Partial short-circuit current through the footing resistance R_T of an overhead line tower
i_{pEE}	Peak short-circuit current in case of two separate simultaneous line-to-earth short circuits
$M_{(1)}, M_{(2)}$	Coupling impedances in the positive- and the negative-sequence system
R_{EA}, R_{EB}	Resistance of the earth grid in the station A or B
R_{EF}	Resistance to earth at the short-circuit location of a cable (Figure 9b) or 10b))
R_T	Footing resistance of an overhead line tower
r	Reduction factor for overhead line with earth wires
r_1	Reduction factor of the sheath or shield of a three-core cable (Figure 9a))
r_3	Reduction factor of the sheaths or shields of three single core cables (Figure 10a))
r_Q	Earth wire radius
r_S	Radius of the metallic sheath or shield of a cable (medium value)
$Z_{(1)A}, Z_{(1)B}$	Positive-sequence short-circuit impedance of a three-phase a.c. system at the connection point A, B (Annex B)
$Z_{(0)}$	Zero-sequence short-circuit impedance of the entire network between the short-circuit locations A and B (admittances between line conductors and earth are disregarded)
Z_{EB}	Earthing impedance of a station B according to Equation (29)
Z_{EBtot}	Total earthing impedance of a station B according to Equation (17)
Z_{ET}	Earthing impedance of the short-circuited tower according to Equation (28)
Z_{ETtot}	Total earthing impedance of the short-circuited tower according to Equation (23)
Z_P	Driving point impedance of an infinite chain (Equation (1) and Figure 1)
Z_{Pn}	Driving point impedance of a finite chain (Equation (2) and Figure 2)
$Z_Q = Z'_Q d_T$	Earth-wire impedance between two towers with earth return
Z'_Q	Earth-wire impedance per unit length with earth return
Z'_{QL}	Mutual impedance per unit length between earth wire and line conductors with earth return
Z'_S	Impedance per unit length of a metallic sheath or shield with earth return
Z'_{SL}	Mutual impedance per unit length between the sheath (or the shield) and a core inside the sheath (or the shield) of a cable with earth return
Z_U	Input impedance of sheaths, shields or armouring of cables or other metallic pipes or pipelines (Equation (17))

δ	Equivalent earth penetration depth (Equation (36))
μ_0	Magnetic constant, $\mu_0 = 4\pi \times 10^{-7}$ Vs/Am
ρ	Resistivity of the soil
α	Angular frequency, $\alpha = 2\pi f$ ($f = 50$ Hz or 60 Hz)

5 Calculation of currents during two separate simultaneous line-to-earth short circuits

5.1 Initial symmetrical short-circuit current

Figure 3 shows the short-circuit current I''_{KEE} during two separate simultaneous line-to-earth short circuits on different line conductors at the locations A and B with a finite distance between them. It is assumed that the locations A and B are far from stations.



NOTE The direction of current arrows is chosen arbitrarily.

Figure 3 – Characterisation of two separate simultaneous line-to earth short circuits and the currents I''_{KEE}

In networks with isolated or with resonant earthed neutral the initial symmetrical short-circuit current I''_{KEE} is calculated with

$$I''_{KEE} = \frac{3cU_n}{\left| \underline{Z}_{(1)A} + \underline{Z}_{(2)A} + \underline{Z}_{(1)B} + \underline{Z}_{(2)B} + \underline{M}_{(1)} + \underline{M}_{(2)} + \underline{Z}_{(0)} \right|} \quad (4)$$

NOTE For derivation of Equation (4) see ITU-T – *Directives concerning protection of telecommunication lines against harmful effects from electric power and electrified railway lines*, Volume V: *Inducing currents and voltages in power transmission and distribution systems*, 1999.

In case of a far-from-generator short circuit, where $\underline{Z}_{(1)} = \underline{Z}_{(2)}$ and $\underline{M}_{(1)} = \underline{M}_{(2)}$, the initial short-circuit current becomes

$$I''_{KEE} = \frac{3cU_n}{\left| 2\underline{Z}_{(1)A} + 2\underline{Z}_{(1)B} + 2\underline{M}_{(1)} + \underline{Z}_{(0)} \right|} \quad (5)$$

5.1.1 Determination of $\underline{M}_{(1)}$ and $\underline{M}_{(2)}$

The positive- and the negative-sequence coupling impedances $\underline{M}_{(1)}$ and $\underline{M}_{(2)}$ are determined as follows:

A voltage source is introduced at the short-circuit location A as the only active voltage of the network. If $\underline{I}_{(1)A}$ and $\underline{I}_{(2)A}$ are the currents due to this voltage source in the positive- and the negative-sequence system at the short-circuit location A, and if $\underline{U}_{(1)B}$ and $\underline{U}_{(2)B}$ are the resulting voltages in the positive- and negative-sequence system at the location B, then

$$\underline{M}_{(1)} = \frac{\underline{U}_{(1)B}}{\underline{I}_{(1)A}} \quad \underline{M}_{(2)} = \frac{\underline{U}_{(2)B}}{\underline{I}_{(2)A}} \quad (6)$$

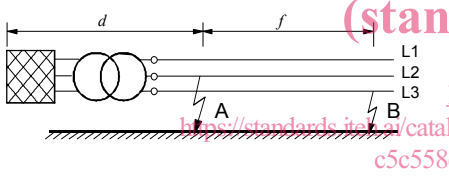
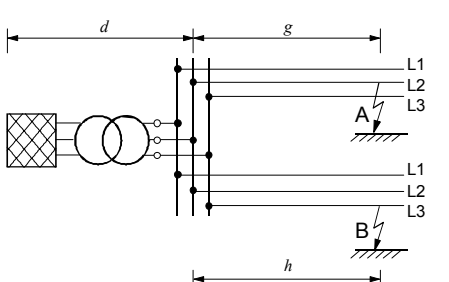
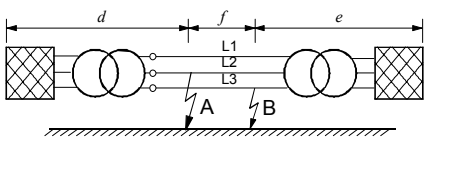
The coupling impedances may also be determined at the short-circuit location B instead of A

$$\underline{M}_{(1)} = \frac{\underline{U}_{(1)A}}{\underline{I}_{(1)B}} \quad \underline{M}_{(2)} = \frac{\underline{U}_{(2)A}}{\underline{I}_{(2)B}} \quad (7)$$

5.1.2 Simple cases of two separate simultaneous line-to-earth short circuits

In simple cases, the current I_{kEE}'' can be calculated as shown in Table 1, if $\underline{Z}_{(1)} = \underline{Z}_{(2)}$ and $\underline{M}_{(1)} = \underline{M}_{(2)}$ (far-from-generator short circuit). Equations (8) to (10) are derived from Equation (5). The indices in these equations refer to the relevant impedances in the respective network.

Table 1 – Calculation of initial line-to-earth short-circuit currents in simple cases

a)		<p>Single-fed radial line</p> $I_{kEE}'' = \frac{3cU_n}{\left 6\underline{Z}_{(1)d} + 2\underline{Z}_{(1)f} + \underline{Z}_{(0)f} \right } \quad (8)$
b)		<p>Two single-fed radial lines</p> $I_{kEE}'' = \frac{3cU_n}{\left 6\underline{Z}_{(1)d} + 2(\underline{Z}_{(1)g} + \underline{Z}_{(1)h}) + \underline{Z}_{(0)g} + \underline{Z}_{(0)h} \right } \quad (9)$
c)		<p>Double-fed single line</p> $I_{kEE}'' = \frac{3cU_n}{\left \frac{6\underline{Z}_{(1)d}\underline{Z}_{(1)e} + 2\underline{Z}_{(1)f}(\underline{Z}_{(1)d} + \underline{Z}_{(1)e})}{\underline{Z}_{(1)d} + \underline{Z}_{(1)f} + \underline{Z}_{(1)e}} + \underline{Z}_{(0)f} \right } \quad (10)$
The voltage factor, c , shall be taken from Table 1 of IEC 60909-0.		

5.2 Peak short-circuit current, symmetrical short circuit breaking current and steady-state short-circuit current

The peak short-circuit current is calculated according to IEC 60909-0: