# INTERNATIONAL STANDARD

ISO 8423

First edition 1991-11-15

# Sequential sampling plans for inspection by variables for percent nonconforming (known standard deviation)

## iTeh STANDARD PREVIEW

Plans d'échantillonnage progressif pour le contrôle par mesures des pourcentages de non conformes (écart-type connu)

ISO 8423:1991 https://standards.iteh.ai/catalog/standards/sist/a7b9e329-b6b5-49ce-8dfdafa01b2a3070/iso-8423-1991



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International Organization for Standardization Case Postale 56 • CH-1211 Genève 20 • Switzerland

Printed in Switzerland

Bibliography

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### Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75% of the member bodies casting a vote

> ISO/TC 69, Applications of statistical methods, Sub-Committee SC 5, Acceptance sampling.

https://standards.iteAnnexes/AarBaand.Caforman.integral.part of this International Standard. Annex Dais for information only.

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## Sequential sampling plans for inspection by variables for percent nonconforming (known standard deviation)

#### Section 1: General

#### Scope 1.1

1.1.1 This International Standard specifies sequential sampling plans and procedures for inspection by variables of discrete items. It is RI complementary to ISO 8422. The plans in the main body of the standard are indexed in terms of the site specification limit U, a lower specification limit producer's risk point and the consumer's risk point.

Annex A specifies sequential sampling plans[Sand423:1991] procedures indexed inhttermsnofdsthe acceptable lards/sist/a7 quality level (AQL) to supplement the system 300/iso-8423-1991 x > sampling plans in ISO 3951.

The purpose of this International Standard is to provide procedures based on a sequential assessment of inspection results, that may be used to induce the supplier through the economic and psychological pressure of non-acceptance of lots of inferior quality to supply lots of a quality having a high probability of acceptance. At the same time the consumer is protected by a prescribed upper limit to the probability of accepting lots of poor quality.

**1.1.2** The sampling plans in this International Standard are primarily designed for use when all of the following conditions are satisfied:

- a) where the inspection procedure is to be applied to a continuing series of lots of discrete items all supplied by one producer using one production process. If there are different producers, this International Standard shall be applied to each one separately;
- b) where only a single quality characteristic x of these items is taken into consideration, which must be measurable on a continuous scale. If several such characteristics are of importance, this International Standard does not apply;

c) where production is stable (under statistical control) and the quality characteristic x has a known standard deviation and is distributed according to a normal distribution or a close approximation to the normal distribution;

d) where a contract or standard defines an upper L, or both; an item is qualified as nonconforming when its measured quality characteristic x satis-

fies one of the following inequalities:

$$x < L \qquad \qquad \dots (1.2)$$

either

x > U

or

$$x < L \tag{1.3}$$

Inequalities (1.1) and (1.2) are called cases with a single specification limit, and (1.3) a case with double specification limits. In this last situation a further distinction is made between separate or combined double specification limits according to whether the risks are considered for each limit separately or for both limits combined (see 2.3.3).

#### 1.2 Normative references

The following standards contain provisions which, through reference in this text, constitute provisions of this International Standard. At the time of publication, the editions indicated were valid. All standards are subject to revision, and parties to agreements based on this International Standard are encouraged to investigate the possibility of applying the most recent editions of the standards indicated below. Members of IEC and ISO maintain registers of currently valid International Standards.

ISO 2854:1976, Statistical interpretation of data — Techniques of estimation and tests relating to means and variances.

ISO 2859-1:1989, Sampling procedures for inspection by attributes — Part 1: Sampling plans indexed by acceptable quality level (AQL) for lot-by-lot inspection.

ISO 3534-1:—<sup>1)</sup>, Statistics — Vocabulary and symbols — Part 1: Probability and general statistical terms.

ISO 3534-2:—<sup>1)</sup>, Statistics — Vocabulary and symbols — Part 2: Statistical quality control.

ISO 3951:1989, Sampling procedures and charts for inspection by variables for percent nonconforming.

ISO 8422:1991, Sequential sampling plans for inspection by attributes. **1.3.1.4 maximum process standard deviation for separate double specification limits [MPSD (sep.)]:** The upper limit to those values of the process standard deviation for which acceptance sampling is applicable in the case of separate double specification limits. (See 2.4.3.2.)

**1.3.1.5 cumulative sample size**  $(n_{cum})$ : When sampling inspection of items from a lot is performed sequentially, the total number of inspected items, counting from the start of the inspection up to, and including, the item last inspected.

**1.3.1.6 least assessable quality level (LAQ):** For a given sequential sampling plan, the process quality level which entails the largest average sample size.

**1.3.1.7 leeway** (y): A quantity derived from the measured value on an item. In the case of a single lower specification limit and in the case of double specification limits, the leeway is obtained by subtracting the numerical value of the lower specification limit from the measured value. In the case of an upper specification limit, the leeway is obtained by subtracting the measured value from the numerical value of the upper specification limit.

## Teh STAND Anumerical value of the upper specification limit.

1.3.1 Definitions

1.3

**Definitions and symbol** 

(standart.35.8 cumulative leeway (Y): When sampling inspection of items from a lot is performed sequentially, the value calculated by summing the leeways obtained from the start of the inspection up to, and dard, the

For the purposes of this International Standard, the bar at log standar

**1.3.1.1 separate double specification limits:** The term used when both upper and lower limits are specified and separate AQLs [or separate producer's and consumer's risks] apply to each limit. (See 2.3.3.)

NOTE 1 The words in brackets have been added to the definition given in ISO 3951 as a broader definition is required in this International Standard.

**1.3.1.2 combined double specification limits**: The term used when both upper and lower limits are specified and an AQL is given [or the producer's and consumer's risks] which applies to the combined percent nonconforming at the two limits. (See 2.3.3.)

**1.3.1.3 limiting process standard deviation for combined double specification limits [LPSD (com.)]:** The upper limit to those values of the process standard deviation for which sequential sampling is applicable in the case of combined double specification limits. (See 2.4.3.1.)

**1.3.1.9 acceptance value for sequential sampling** (A): A value derived from the specified parameters of the sampling plan and the cumulative sample size. Whether the lot may yet be accepted is determined by comparing the cumulative leeway with the acceptance value.

**1.3.1.10** rejection value for sequential sampling (R): A value derived from the specified parameters of the sampling plan and the cumulative sample size. Whether the lot may yet be considered unacceptable is determined by comparing the cumulative leeway with the rejection value.

#### 1.3.2 Symbols

The symbols used in this International Standard are as follows:

- A Acceptance value for sequential sampling.
- $A_{\rm t}$  Acceptance value corresponding to the curtailed value of the cumulative sample size.

<sup>1)</sup> To be published.

CRQ	Consumer's risk quality level (in per- cent nonconforming).	<i>p</i> <sub>A</sub>	Producer's risk quality level (in proportion nonconforming). $P_a = 1 - \alpha$ when $p = p_a$ .	
ſ	In the case of separate double speci- fication limits, a coefficient, which in conjunction with $\sigma$ and $(U - L)$ deter- mines the applicability of accentance	P <sub>g</sub>	Least assessable quality level (in proportion nonconforming). $p_g = 1 - F(g)$ .	
sampling. (See 2.4.3.2.)		<i>P</i> <sub>R</sub>	Consumer's risk quality level (in proportion nonconforming). $P_a = \beta$ when	
r	tion.	D	$p = p_{\rm R}$ .	
g	Multiplier of the cumulative sample size that is used to determine the ac- ceptance values and the rejection val- ues (slope of the acceptance and rejection lines).	PRQ	Producer's risk quality level (in percent nonconforming).	
		R	Rejection value for sequential sampl- ing.	
h <sub>A</sub>	Constant that is used to determine the acceptance values (intercept of the acceptance line).	U	Upper specification limit (as a super- script to a parameter or a variable, denotes its value for $U$ ).	
h <sub>R</sub>	Constant that is used to determine the rejection values (intercept of the rejection line).	x	Measured value of the characteristic on an item of product.	
L	Lower specification limit (as a super-	у	Leeway, defined as	
script to a parameter or a variable. denotes its value for $D$ TANDARD PREVIE $y \neq U - x$ for a single fication limit				
LAQ	Least assessable quality texet (in percision of the second	teh.ai)	y = x - L for a single lower speci- fication limit, and	
LPSD (com.) Limiting process standard deviation for 23:1991 combined double specificationalimits ndards/sist/a7b9e329-b6b5-4992-8dx - L for double specification				
MPSD (sep.) Maximum process standard deviation				
	for separate double specification lim- its.	Y	Cumulative leeway obtained by adding the leeways up to, and including, the item last inspected	
n <sub>0</sub>	Sample size for a single sampling plan corresponding to the sequential sam-	7	The <i>P</i> fractile of the standardized	
	pling plan.	<sup>2</sup> p	normal distribution:	
$n_{av}$	Average sample size.		$z_{0.05} = -1,644.9$	
<i>n</i> <sub>cum</sub>	Cumulative sample size.		since	
n <sub>t</sub>	Curtailment value of the cumulative sample size.		F(-1,644 9) = 0.05	
р	Process quality level (in proportion nonconforming).		$z_{0,10} = -1,281.6$	
	NOTE 2 To convert p to percent noncon-		since	
forming, multiply by 100.				

- $\alpha$  The producer's risk.<sup>2)</sup>
- $\beta$  The consumer's risk.<sup>2)</sup>
- $\sigma$  Standard deviation of x in the process. ( $\sigma^2$ , the square of the standard deviation, is known as the variance.)
- $\psi$  In the case of combined double specification limits, a coefficient which in conjunction with  $\sigma$  and (U - L) determines the applicability of sequential sampling. (See 2.4.3.1.)
- λ Index parameter that is used to determine approximations to the OC curve at general quality levels. (See C.2.2.)

# 1.4 **Principle of sequential sampling by** variables

Under a sequential sampling plan by variables, items are selected at random and subjected to inspection one by one. After the inspection of each individual item, the cumulative leeway is calculated and used to assess whether there is sufficient information to sentence the lot at that stage of the inspection. lot is considered acceptable and sampling of that lot is terminated.

If, on the other hand, the cumulative leeway is such that the risk of non-acceptance for a lot of satisfactory quality (the producer's risk) is sufficiently low, the lot shall be considered not acceptable, and sampling of that lot is terminated.

If the cumulative leeway does not allow either of the above decisions to be taken, then an additional item is inspected. The process is continued until sufficient sample information has been accumulated to warrant a decision that the lot is acceptable or not acceptable.

NOTE 3 In the case of separate double specification limits, the assessment of the cumulative leeway is performed for each limit separately. If, at a given stage, the risk of judging a lot of satisfactory quality to be unacceptable is sufficiently low for one or other of the limits, inspection terminates and the lot is not accepted. Alternatively, if at a given stage the risk of judging a lot of unsatisfactory quality to be acceptable is sufficiently low for one of the limits, then the lot is considered to be acceptable with respect to that limit and inspection for that limit is terminated; inspection is continued until

mation to sentence the lot at that stage of the in DAa satisfactory results are obtained also for the other spection. If, at a given stage the cumulative leeway istauchdards. The obtained also for the other acceptable. The obtained also for the other spectron.

that the risk of accepting a lot of unsatisfactory b) inspection for the other limit leads to non-acceptance quality (the consumer's risk) is sufficiently low, the ISO 8423:06the lot.

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 $H_0: p = p_A$ 

against the alternative hypothesis

 $H_1: p = p_R$ 

<sup>2)</sup>  $\alpha$  and  $\beta$  may be considered to be the type I and type II risks, respectively, when testing the null hypothesis

### Section 2: Choice of sampling plan

# 2.1 Factors determining the choice of a sequential sampling plan by variables

#### 2.1.1 Choice between variables and attributes

**2.1.1.1** The first question to consider is whether it is desirable to inspect by variables rather than by attributes. The following points should be taken into account.

- a) In terms of economics, it is necessary to compare the total cost of the relatively simple inspection of a larger number of items of product by an attributes plan with the generally more elaborate procedure required by a variables plan, which is usually more expensive in time and money per item.
- b) A variables plan can be less readily understood than an attributes plan; for example, it may at first be difficult to accept that, when inspecting by variables, a decision not to accept a lot may be based on measurements taken on a sample that does not contain any nonconforming items.
- c) A comparison of the size of the samples required  $\frac{1}{2}$  mined as for sampling plans for inspection by attributes ds/sist/a/byc329-bob5-49ce-8dff and equivalent sampling plans for inspection byso-8423-1991 variables shows that a variables sampling plan requires a smaller sample size to give the same producer's and consumer's risks than an attributes sampling plan. A variables sampling plan therefore has a substantial advantage when the inspection process is expensive, for example in the case of destructive testing. 2.1.2 Choice betwee
- d) The sampling plans in this International Standard only apply to the case of a single quality characteristic. If conformance to specification is to be assessed in terms of more than one quality characteristic, the standard shall be applied separately to each of these. In such a situation it is recommended that all the quality characteristics be treated as attributes and that attributes sampling plans from ISO 2859-1 or ISO 8422 be used.

**2.1.1.2** The sequential sampling plans in this International Standard may only be used when there is reason to believe that the distribution of measurements is normal and when there is valid evidence that the standard deviation of the process can be considered constant and taken to be  $\sigma$ .

If inspection is carried out on a continuing series of lots, the hypothesis of normality can be verified using results previously obtained using a single sampling plan, and the stability of the standard deviation may emerge from a control chart measuring process variability. If it appears that the standard deviation is in control, the (weighted) root mean square value of observed standard deviations may be presumed to be  $\sigma$ , the "known" standard deviation of the process. In order to verify that the variability remains under control, the standard deviation in subsequent samples should still be calculated.

If inspection is carried out on an isolated lot, there will be no evidence about the standard deviation of the process, and therefore this International Standard does not apply to the inspection of isolated lots.

#### NOTES

4 Tests for departure from normality are dealt with in section two of ISO 2854:1976, which provides examples of graphical methods which can be used to verify that the distribution of the data is sufficiently normal to justify the use of sampling by variables.

5 A more comprehensive treatment of tests of normality is given in ISO 5479.

c) A comparison of the size of the samples required 3:1991 then the weighted root mean square estimate s is determined as  $r_{2}$  as  $r_{2}$  as  $r_{3}$ .

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1	$/(n_1-1)s_1^2 + (n_2-1)s_2^2 + + (n_k-1)s_k^2$
-	$n_1 - 1 + n_2 - 1 + \dots + n_k - 1$

where  $n_1, n_2, ..., n_k$  denote the sizes of the k samples.

## 2.1.2 Choice between sequential and single sampling plans

The average sample size is the average of the various sample sizes which may occur under a sampling plan for a given level of the process quality. The use of sequential sampling plans leads to a smaller average sample size than single sampling plans having the same operating characteristic. For good or very poor quality lots, the savings over the corresponding single sampling plans may reach, or even exceed, 50 %.

On the other hand, the actual number of items inspected for a particular lot when using a sequential sampling plan may considerably exceed that of the corresponding single sampling plan. For the sequential sampling plans in this International Standard, a curtailment rule (see 2.1.4) has been introduced in order to limit the potential number of inspected items. Annex C gives a method for determining approximate values of the average sample size. As the ultimate sample size from a particular lot is not known in advance, the selection of the sample may present organizational difficulties when sequential sampling plans are used. Moreover, the scheduling of inspection operations may present difficulties when using a sequential sampling plan. A further disadvantage is that the execution of a sequential sampling plan is more easily misunderstood by the inspectors than the simpler rules for single sampling.

When the inspection procedure is applied to the case of separate double specification limits on a single quality characteristic, it may happen that inspection concerning one of the limits terminates favourably long before enough information has been accumulated to warrant a decision regarding the other limit. Therefore sampling has to continue for some time before an overall decision can be taken.

The balance between the advantages of a smaller average sample size and the organizational disadvantages associated with a fluctuating inspection load results in sequential sampling by variables being suitable when only a single quality characteristic is considered and when the inspection of individual items is costly in comparison with inspection overheads.

#### 2.1.3 Caution

The choice between single and sequential sampling <u>ISO 8</u> plans shall be made before the inspection of a lot is started. During the inspection of a lot, it is not per<u>52a307</u> mitted to switch between one type of sampling plan to another as the operating characteristic of the plan may be drastically changed if the actual inspection results influence the choice of acceptance criterion.

#### 2.1.4 Curtailment of the sample size

Although a sequential sampling plan is on average much more economical than the equivalent single sampling plan, it may occur, during the inspection of a particular lot, that acceptance or nonacceptance comes at a very late stage because the cumulative leeway remains between the acceptance value and the rejection value for a long time. With the graphical method this corresponds to the random progress of the step curve remaining in the indecision zone. Such a situation is most likely to occur when the quality of the lot is close to LAQ.

In order to alleviate this disadvantage, a maximum cumulative sample size  $n_t$  is set before sampling begins, and inspection is stopped if the cumulative sample size reaches the curtailment value,  $n_t$ , with-

out a decision having been made. The acceptance or non-acceptance of the lot is then determined in accordance with a rule which is also agreed in advance of sampling. The curtailment rules of this International Standard have been determined in such a way that the producer's and consumer's risks are hardly affected by this deviation from the principles underlying the statistical theory of sequential sampling inspection. The curtailment rules to be used are given in 2.4.2.

# 2.2 Particular reservations on the inspection of small lots

The statistical theory underlying the sequential sampling plans in this International Standard is based on the assumption that the samples are taken from an infinitely large population. When sampling is carried out without replacement from a lot, the theory remains valid for all practical purposes if the cumulative sample size does not exceed one-tenth of the lot size N; the theory remains approximately valid even for cumulative sample sizes up to one-seventh of N. Unfortunately, in contrast to the situation for single sampling plans, the actual cumulative sample size that is necessary in a sequential sampling plan will not be known in ad-

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In the case of a small lot it is therefore advisable to ensure that the size of the lot is sufficiently large to allow a curtailed sequential sampling plan to operate under sampling without replacement, in accordance with the specified producer's and consumer's risks. For the general sequential sampling plans described in 2.3.2 and 2.4.1, it is therefore recommended that the lot size exceed  $7n_t$ , where  $n_t$  is the curtailment value of the sequential sampling plan.

NOTE 7 If the lot size is not sufficiently large to satisfy the above requirement, both the consumer's and the producer's risks will generally become less than their specified values.

#### 2.3 Selection of a sampling plan

#### 2.3.1 Plans matching those of ISO 3951

If it is required to find a sequential sampling plan matching a " $\sigma$ " method plan from ISO 3951:1989, then annex A may be used. Annex A contains sequential sampling plans indexed by acceptable quality level (AQL) and sample size code letter. The operating characteristic curves of these plans match, as closely as practicable, those of the corresponding " $\sigma$ " method plans in ISO 3951.



Figure 1 — Operating characteristic curve for a sampling plan with producer's risk  $\alpha = 0.05$  and consumer's risk  $\beta = 0.10$ 

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#### 2.3.2 General plans

The general method described in 2.3.2 and 2.4.1 is used when the requirements of the sequential sam<sub>123:199</sub> pling plan are specified in terms of two points on the operating characteristic curve of the plan. The point corresponding to the higher probability of acceptance shall be designated the *producer's risk point*; the other shall be designated the *consumer's risk point*.

The first step when designing a sequential sampling plan by the general method is to choose the producer's and consumer's risk points, if they have not already been dictated by circumstances. For this purpose, a producer's risk of  $\alpha = 0.05$  and a consumer's risk of  $\beta = 0.10$  are often used. (See figure 1.)

When the desired sequential sampling plan is required to have approximately the same operating characteristic as an existing sampling plan, the producer's risk point and the consumer's risk point may be read off from a graph or a table of the operating characteristic of that plan. When no such plan exists, the producer's and consumer's risk points have to be determined from direct considerations of the conditions under which the sampling plan will operate.

#### 2.3.3 Specifying quality levels

When only a single specification limit is considered, the proportion nonconforming in incoming product relates to that limit.

When both upper and lower specification limits are (standards.i given.atimay be appropriate to consider quality lev-.3.2 and 2.4.1 is sequential sam<sub>123:199</sub> the limits are known as "separate double specitication limits". Alternatively, an overall quality level ication limits". Alternatively, an overall quality level bility of acceptbility of accepttocer's risk point; consumer's risk

#### 2.4 Pre-operation preparations

#### **2.4.1** Obtaining the parameters $h_A$ , $h_R$ and g

The criteria for acceptance and for non-acceptance of a lot that are invoked at each stage of the inspection are determined from the parameters  $h_A$ ,  $h_R$  and g.

The values of these parameters corresponding to a producer's risk of  $\alpha = 0.05$ , a consumer's risk of  $\beta = 0.10$  and preferred values of the producer's and consumer's risk qualities are given in table 1.

Annex B gives general procedures for determining  $h_{\rm A}$ ,  $h_{\rm R}$  and g for any combination of producer's and consumer's risk points.

In the case of a single specification limit or combined double specification limits, only one set of parameters  $h_A$ ,  $h_R$  and g shall be determined.

With separate double specification limits, two sets of parameters shall be determined:

 $h_{\rm A}^{(U)}$ ,  $h_{\rm R}^{(U)}$  and  $g^{(U)}$ , corresponding to the upper limit, and

 $h_{A}^{(L)}$ ,  $h_{R}^{(L)}$  and  $g^{(L)}$ , corresponding to the lower limit.

#### 2.4.2 Determination of the curtailment value of the sample size

#### 2.4.2.1 Standard procedures

- a) If the sample size  $n_0$  of the single sampling plan that is equivalent to the sequential sampling plan under consideration is known, the curtailment value for the cumulative sample size is determined as  $n_{\rm t} = 1,50n_0$ , rounded up to the nearest integer.
- b) If the sample size of the equivalent single sampling plan is not known, the curtailment value is determined from the producer's and consumer's risk points.

The curtailment values corresponding to a producer's risk of  $\alpha = 0.05$ , a consumer's risk of  $\beta = 0.10$  and preferred values of the producer's and consumer's risk qualities care given in table 1.

Annex B gives general procedures for determining  $n_{\rm f}$  for any combination of producer's and ISO 84value of the process standard deviation is given by consumer's risk points.

In the case of separate double specification 2a3070/iso-8423-1991

NOTE 8 limits, the curtailment value is determined for each of the limits separately according to the above rule. The curtailment value to be used for the curtailed sequential sampling plan is taken as the larger of the two values obtained.

#### 2.4.2.2 Truncation for small lots

If the resulting value of n exceeds the lot size, then the sequential sampling plan shall be used with the curtailment value n of the sample size equal to the lot size.

#### 2.4.2.3 Example

The specified minimum withstand voltage for certain insulators is 200 kV. Lots from a steady production are submitted for inspection. Production is stable and it has been verified that the withstand voltages vary within a lot in accordance with a normal distribution. It has further been documented that the standard deviation within a lot is stable and can be taken to be  $\sigma = 1,2$  kV.

It has been decided to use a sequential sampling plan with the following properties:

a) If submitted quality is 0,5 % nonconforming, then the probability of acceptance shall be 0,95.

b) If submitted quality is 2.0 % nonconforming, then the probability of acceptance shall be 0,10.

These requirements are achieved by fixing the producer's risk point at  $p_A = 0,005$ ,  $\alpha = 0,05$  and the consumer's risk point at  $p_R = 0,02$ ,  $\beta = 0,10$ .

The specification refers to a single, lower limit. From table 1 it is seen that the required sequential sampling plan has the parameters

 $h_{\Delta} = 4,312$  $h_{\rm R} = 5,536$ g = 2,315 $n_{\rm t} = 49$ 

The same values would have resulted from using the general procedure given in annex B.

#### 2.4.3 Maximum values of process standard deviation

#### 2.4.3.1 Limiting process standard deviation for combined double specification limits, LPSD (com.)

An the case of combined double specification limits, sequential sampling is only applicable if the process (standar standard deviation  $\sigma$  is sufficiently small in relation to the specification interval (U-L). The limiting

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where  $\psi$  depends only on PRQ, the producer's risk quality.

Table 2 gives values of  $\psi$  corresponding to preferred values of PRQ.

#### 2.4.3.2 Maximum process standard deviation for separate double specification limits, MPSD (sep.)

In the case of separate double specification limits. sampling by variables is only applicable if the process standard deviation  $\sigma$  is sufficiently small in relation to the specification interval (U-L). The maximum tolerable value of the process standard deviation is given by

 $\mathsf{MPSD} = (U - L)f$ 

where f depends on  $PRQ^{(l)}$  and  $PRQ^{(L)}$ , the producer's risk qualities for the upper and the lower specification limit, respectively.

Table 3 gives values of f corresponding to preferred values of PRQ<sup>(*U*)</sup> and PRQ<sup>(*L*)</sup>.

If, in the case of separate double specification limits,  $\sigma$  exceeds MPSD, the lot shall immediately be judged not acceptable without a sample being drawn.

NOTE 9 When  $\sigma$  exceeds MPSD, no lot can satisfy both requirements

$$p^{(U)} < PRQ^{(U)}$$

and

$$p^{(L)} < \mathsf{PRQ}^{(L)}$$

and therefore acceptance sampling is pointless.

#### 2.4.4 Choosing the form of the sampling plan

This International Standard gives two methods: a numerical method and a graphical method.

The numerical method has the advantage of being accurate, thereby avoiding disputes about acceptance or non-acceptance. The graphical method is well suited to the inspection of series of lots, as the chart need only to be drawn once, but the method is less accurate due to the inaccuracy inherent in plotting points and in drawing straight lines. On the other hand, the method does have the advantage of displaying the increase in the information on the quality of the lot as additional items are inspected, information being represented by the progress of a broken line within the indecision zone until the line reaches, or crosses, one of the boundaries of that zone.

The numerical method is the standard method. The graphical method may be used only with the proviso that "close" decisions to accept or not to accept a lot shall always be resolved by the numerical method.

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