



## Standard Practice for Measuring Ultrasonic Velocity in Materials<sup>1</sup>

This standard is issued under the fixed designation E 494; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon ( $\epsilon$ ) indicates an editorial change since the last revision or reapproval.

*This specification has been approved for use by agencies of the Department of Defense.*

### 1. Scope

1.1 This practice covers a test procedure for measuring ultrasonic velocities in materials with conventional ultrasonic pulse echo flaw detection equipment in which results are displayed in an A-scan display. This practice describes a method whereby unknown ultrasonic velocities in a material sample are determined by comparative measurements using a reference material whose ultrasonic velocities are accurately known.

1.2 This procedure is intended for solid materials 5 mm (0.2 in.) thick or greater. The surfaces normal to the direction of energy propagation shall be parallel to at least  $\pm 3^\circ$ . Surface finish for velocity measurements shall be 3.2  $\mu\text{m}$  (125  $\mu\text{in.}$ ) rms or smoother.

NOTE 1—Sound wave velocities are cited in this practice using the fundamental units of meters per second, with inches per second supplied for reference in many cases. For some calculations, it is convenient to think of velocities in units of millimeters per microsecond. While these units work nicely in the calculations, the more natural units were chosen for use in the tables in this practice. The values can be simply converted from m/sec to mm/ $\mu\text{sec}$  by moving the decimal point three places to the left, that is, 3500 m/s becomes 3.5 mm/ $\mu\text{sec}$ .

1.3 Ultrasonic velocity measurements are useful for determining several important material properties. Young's modulus of elasticity, Poisson's ratio, acoustic impedance, and several other useful properties and coefficients can be calculated for solid materials with the ultrasonic velocities if the density is known (see Appendix X1).

1.4 More accurate results can be obtained with more specialized ultrasonic equipment, auxiliary equipment, and specialized techniques. Some of the supplemental techniques are described in Appendix X2. (Material contained in Appendix X2 is for informational purposes only.)

NOTE 2—Factors including techniques, equipment, types of material, and operator variables will result in variations in absolute velocity readings, sometimes by as much as 5%. Relative results with a single combination of the above factors can be expected to be much more accurate (probably within a 1% tolerance).

<sup>1</sup> This practice is under the jurisdiction of ASTM Committee E-7 on Nondestructive Testing and is the direct responsibility of Subcommittee E07.06 on Ultrasonic Testing Procedure.

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1.5 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

### 2. Referenced Documents

#### 2.1 ASTM Standards:

- C 597 Test Method for Pulse Velocity Through Concrete<sup>2</sup>
- E 317 Practice for Evaluating Performance Characteristics of Ultrasonic Pulse-Echo Testing Systems Without the Use of Electronic Measurement Instruments<sup>3</sup>
- E 797 Practice for Measuring Thickness by Manual Ultrasonic Pulse-Echo Contact Method<sup>3</sup>
- E 1316 Terminology for Nondestructive Examinations<sup>3</sup>

### 3. Terminology

3.1 *Definitions*—For definitions of terms used in this practice, see Terminology E 1316.

### 4. Summary of Practice

4.1 Several possible modes of vibration can propagate in solids. This procedure is concerned with two velocities of propagation, namely those associated with longitudinal ( $v_l$ ) and transverse ( $v_t$ ) waves. The longitudinal velocity is independent of sample geometry when the dimensions at right angles to the beam are very large compared with beam area and wave length. The transverse velocity is little affected by physical dimensions of the sample. The procedure described in Section 6 is, as noted in the scope, for use with conventional pulse echo flaw detection equipment only.

### 5. Apparatus

5.1 The ultrasonic testing system to be used in this practice shall include the following:

5.1.1 *Test Instrument*—Any ultrasonic instrument comprising a time base, transmitter (pulser), receiver (echo amplifier), and an A-scan indicator circuit to generate, receive, and display electrical signals related to ultrasonic waves. Equipment shall allow reading the positions of  $A_k$ ,  $A_s$ ,  $A_p$ ,  $A_l$  (defined in 6.1.4 and 6.2.4), along the A-scan base line within  $\pm 0.5$  mm (0.020

<sup>2</sup> Annual Book of ASTM Standards, Vol 04.02.

<sup>3</sup> Annual Book of ASTM Standards, Vol 03.03.

in.). For maximum accuracy, the highest possible frequency that will present at least two easily distinguishable back echos, and preferably five, shall be used.

5.1.2 *Search Unit*—The search unit containing a transducer that generates and receives ultrasonic waves of an appropriate size, type and frequency, designed for tests by the contact method shall be used. Contact straight beam longitudinal mode shall be used for longitudinal velocity measurements, and contact straight beam shear mode for transverse velocity measurements.

5.1.3 *Couplant*—For longitudinal velocity measurements, the couplant should be the material used in practice, for example, clean light-grade oil. For transverse velocity measurements, a high viscosity material such as resin or solid bond shall be used. In some materials isopolybutene, honey, or other high-viscosity materials have been used effectively. Most liquids will not support transverse waves. In porous materials special nonliquid couplants are required. The couplant must not be deleterious to the material.

5.1.4 *Standard Reference Blocks:*

5.1.4.1 *Velocity Standard*—Any material of known velocity, that can be penetrated by the acoustical wave, and that has an appropriate surface roughness, shape, thickness, and parallelism. The velocity of the standard should be determined by some other technique of higher accuracy, or by comparison with water velocity that is known (see Appendix X2.5 and Appendix X4). The reference block should have an attenuation similar to that of the test material.

5.1.4.2 For horizontal linearity check, see Practice E 317.

6. Procedure

6.1 *Longitudinal Wave Velocity*—Determine bulk, longitudinal wave velocity ( $v_l$ ) by comparing the transit time of a longitudinal wave in the unknown material to the transit time of ultrasound in a velocity standard ( $v_k$ ).

6.1.1 Select samples of each with flat parallel surfaces and measure the thickness of each to an accuracy of  $\pm 0.02$  mm (0.001 in.) or 0.1%, whichever is greater.

6.1.2 Align the transducer over each sample and obtain a nominal signal pattern (see Fig. 1) of as many back echos as are clearly defined. The time base (sweep control) must be set the same for both measurements.

6.1.3 Using a scale or caliper measure the distance at the base line between the leading edge of the first back echo and the leading edge of the last back echo that is clearly defined on the known and unknown sample. For better accuracy, adjust the amplitude of the last back echo by means of the gain control to approximately the same height as the first back echo, after the

position of the leading edge of the first back echo has been fixed. This allows more accurate time or distance measurements. The position of the leading edge of the last back echo is then determined. The signal has traversed a distance twice the thickness of the specimen between each back echo. The signal traversing the specimen and returning is called a round trip. In Fig. 1 the signal has made six round trips between Echo 1 and Echo 7. Count the number of round trips from first echo used to the last echo measured on both samples. This number will be one less than the number of echoes used. Note that the sample thickness, number of round trips, and distance from front to last back echo measured need not be the same.

6.1.4 Calculate the value of the unknown velocity as follows:

$$v_1 = (A_k n_1 t_1 v_k) / (A_1 n_k t_k) \tag{1}$$

where:

- $A_k$  = distance from first to  $N$ th back echo on the known material, m (in.), measured along the baseline of the A-scan display,
- $n_1$  = number of round trips, unknown material,
- $t_1$  = thickness of unknown material, m (in.),
- $v_k$  = velocity in known material, m/s (in./s),
- $A_1$  = distance from the first to the  $N$ th back echo on the unknown material, m (in.), measured along the baseline of the A-scan display,
- $n_k$  = number of round trips, known material, and
- $t_k$  = thickness, known material, m (in.).

NOTE 3—The units used in measurement are not significant as long as the system is consistent.

6.2 *Transverse Velocity*—Determine transverse velocity ( $v_s$ ) by comparing the transit time of a transverse wave in an unknown material to the transit time of a transverse wave in a material of known velocity ( $v_l$ ).

6.2.1 Select samples of each with flat parallel surfaces and measure the thickness of each to an accuracy of  $\pm 0.02$  mm (0.001 in.) or 0.1 %, whichever is greater.

6.2.2 Align the transducer (see Fig. 1) over each sample and obtain an optimum signal pattern of as many back echos as are clearly defined. The time base (sweep control) must be the same for both measurements.

6.2.3 Using a scale or caliper measure the distance at the base line between the leading edge of the first back echo and the leading edge of the last back echo that is clearly defined on the known and unknown sample. For better accuracy, adjust the amplitude of the last back echo by means of the gain control to approximately the same height as the first back echo, after the position of the leading edge of the first back echo has been fixed. This adds high frequency components of the signal which have been attenuated. Then determine the position of the leading edge of the last back echo. Count the number of round trips from first echo used to the last echo measured on both samples. This number will be one less than the number of echoes used. Note that the sample thickness, number of round trips, and distance from first to last back echo measured need not be the same.

6.2.4 Calculate the value of the unknown velocity as follows:

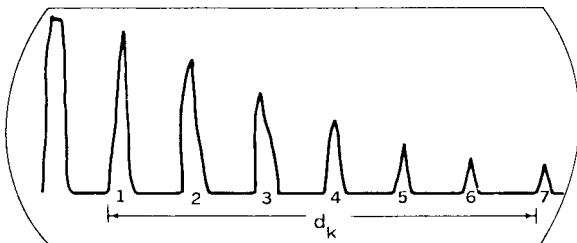


FIG. 1 Initial Pulse and 7 Back Echoes

$$v_s = (A_t n_s t_s v_t) / (A_s n_t t_t) \quad (2)$$

where:

- $A_t$  = distance from first to Nth back echo on the known material, m (in.), measured along the baseline of the A-scan display,
- $n_s$  = number of round trips, unknown material,
- $t_s$  = thickness of unknown material, m (in.),
- $v_t$  = velocity of transverse wave in known material, m/s (in./s),
- $A_s$  = distance from the first to the Nth back echo on the unknown material, m (in.), measured along the baseline of the A-scan display,
- $n_t$  = number of round trips, known material, and
- $t_t$  = thickness, known material, m (in.). (See Note 3).

- 7.1.2.1  $A_t$  = \_\_\_\_\_ m (in.)
- 7.1.2.2  $n_s$  = \_\_\_\_\_
- 7.1.2.3  $t_s$  = \_\_\_\_\_ m (in.)
- 7.1.2.4  $v_t$  = \_\_\_\_\_ m/s (in./s)
- 7.1.2.5  $A_s$  = \_\_\_\_\_ m (in.)
- 7.1.2.6  $n_t$  = \_\_\_\_\_
- 7.1.2.7  $t_t$  = \_\_\_\_\_ m (in.)
- 7.1.2.8  $v_s$  (using Eq 2) = \_\_\_\_\_ m/s (in./s)
- 7.1.3 Horizontal linearity
- 7.1.4 Test frequency
- 7.1.5 Couplant
- 7.1.6 Search unit:
  - 7.1.6.1 Frequency
  - 7.1.6.2 Size
  - 7.1.6.3 Shape
  - 7.1.6.4 Type
  - 7.1.6.5 Serial number
- 7.1.7 Sample geometry
- 7.1.8 Instrument:
  - 7.1.8.1 Name
  - 7.1.8.2 Model number
  - 7.1.8.3 Serial number
  - 7.1.8.4 Pertinent control settings

**7. Report**

7.1 The following are data which should be included in a report on velocity measurements:

7.1.1 Longitudinal Wave:

- 7.1.1.1  $A_k$  = \_\_\_\_\_ m (in.)
  - 7.1.1.2  $n_l$  = \_\_\_\_\_
  - 7.1.1.3  $t_l$  = \_\_\_\_\_ m (in.)
  - 7.1.1.4  $v_k$  = \_\_\_\_\_ m/s (in./s)
  - 7.1.1.5  $A_l$  = \_\_\_\_\_ m (in.)
  - 7.1.1.6  $n_k$  = \_\_\_\_\_
  - 7.1.1.7  $t_k$  = \_\_\_\_\_ m (in.)
  - 7.1.1.8  $v_l$  (using Eq 1) = \_\_\_\_\_ m/s (in./s)
- 7.1.2 Transverse Wave:

**8. Keywords**

8.1 measure of ultrasonic velocity; nondestructive testing; ultrasonic properties of materials; ultrasonic thickness gages; ultrasonic velocity

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**APPENDIXES**

**(Nonmandatory Information)**

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**X1. FORMULAS**

X1.1 Using the technique of this practice will give results in some instances which are only approximate calculations. The determination of longitudinal and transverse velocity of sound in a material makes it possible to approximately calculate the elastic constants, Poisson's ratio, elastic moduli, acoustic impedance, reflection coefficient, and transmission coefficient. In this Appendix, the formulas for calculating some of these factors are as follows (see Note X1.1):

X1.1.1 Poisson's Ratio:

$$\sigma = [1 - 2(v_s/v_l)^2] / 2[1 - (v_s/v_l)^2]$$

where:

- $\sigma$  = Poisson's ratio,
- $v_s$  = ultrasonic transverse velocity, m/s (or in./s), and
- $v_l$  = ultrasonic longitudinal velocity, m/s (or in./s).

X1.1.2 Young's Modulus of Elasticity:

$$E = (\rho v_s^2 (3v_l^2 - 4v_s^2)) / (v_l^2 - v_s^2)$$

where:

- $\rho$  = density, kg/m<sup>3</sup> (or lb/in.<sup>3</sup>),
- $v_l$  = longitudinal velocity, m/s (or in./s),

- $v_s$  = transverse velocity, m/s (or in./s), and
- $E$  = Young's modulus of elasticity, N/m<sup>2</sup> (or lb/in.<sup>2</sup>) (see Notes X1.2 and X1.3).

X1.1.3 Acoustic Impedance (see Note X1.3):

$$z = \rho v_l$$

where:

$z$  = acoustic impedance (kg/m<sup>2</sup>·s (or lb/in.<sup>2</sup>·s)).

X1.1.4 Shear Modulus (see Note X1.3):

$$G = \rho v_s^2$$

X1.1.5 Bulk Modulus (see Note X1.3):

$$K = \rho [v_l^2 - (4/3)v_s^2]$$

X1.1.6 Reflection Coefficient for Energy (R):

$$R = (Z_2 - Z_1)^2 / (Z_2 + Z_1)^2$$

where:

- $Z_1$  = acoustic impedance in Medium 1, and
- $Z_2$  = acoustic impedance in Medium 2.

X1.1.7 Transmission Coefficient for Energy (T):

$$T = (4Z_2 Z_1) / (Z_2 + Z_1)^2$$

NOTE X1.1—The dynamic elastic constants may differ from those determined by static tensile measurements. In the case of metals, ceramics, and glasses, the differences are of the order of 1 %, and may be corrected by known theoretical formulas. For plastics the differences may be larger, but can be corrected by correlation.

NOTE X1.2—Conversion factor:  $1 \text{ N/m}^2 = 1.4504 \times 10^{-4} \text{ lb/in.}^2$ .

NOTE X1.3—When using pounds per cubic inch for density and inches per second for velocity, results must be divided by  $g$  (acceleration due to gravity) to obtain results in pounds per square inch for  $E$ ,  $G$ , or  $K$  and also to obtain results for  $Z$  in pounds per square inch per second. Acceleration due to gravity ( $g$ ) =  $386.4 \text{ in./s} \cdot \text{s}$ .

## X2. IMPORTANT TECHNIQUES FOR MEASURING ULTRASONIC VELOCITY IN MATERIALS

### X2.1 Introduction

X2.1.1 Several techniques are available for precise measurement of ultrasonic velocity in materials. Most of these techniques require specialized or auxiliary equipment.

X2.1.2 Instruments are available commercially which automatically measure sound velocity or time interval or both. There is a growing list of manufacturers who make ultrasonic instruments, including pulser, receiver, and display designed specifically for making these measurements automatically or which can be used for these measurements even though designed primarily for other measurements (for example, thickness gages).

X2.1.3 Various methods have been introduced to solve the problem of the accurate measurement of time interval or number of waves in the specimen. It would be beyond the scope of this Appendix to attempt to include all these techniques. However, it is considered of value to those using this practice to know some of these techniques. This Appendix will be useful to those who have more refined equipment or auxiliary equipment available and to those who wish more accurate results.

X2.1.4 This Appendix will include some techniques that are only suitable for the laboratory. It is only under strictly controlled conditions such as are available in the laboratory that the greatest accuracy can be achieved. Such measurements may be slow and require very carefully prepared specimens. A list of references (1-28)<sup>4</sup> is provided for more detailed information.

### X2.2 Special Features Built Into the Ultrasonic Equipment

X2.2.1 Ultrasonic equipment is available that provides means adequate for the measurement of acoustic wave propagation with respect to time.

### X2.3 Precision Oscilloscope

X2.3.1 An auxiliary precision cathode ray oscilloscope can be used to observe the echo pattern. Using the precision calibrated horizontal display of the oscilloscope, the transit time between successive multiple back reflections is determined. Calculate velocity as follows:

$$\text{Velocity (m/s (or in./s))} = [2 \text{ thickness (m or in.)}] / [\text{Time (s)}]$$

### X2.4 Electronic Time Marker

X2.4.1 An accessory is frequently available that displays one or more visual marks, usually a step, on the display of the

basic instrument. It is usually superimposed on the standard echo pattern. The mark is moved using a calibrated control. The control reads time directly in microseconds.

X2.4.2 The technique is to align the step on the display, first with the first back reflection, and then, using the second marker, if available, with the second back reflection. Based on control readings at both instances, the elapsed time for a round trip through the specimen is determined. (Calculation is the same as in X2.3).

### X2.5 Ultrasonic Interferometer (Velocity Comparator)

X2.5.1 The measurement of ultrasonic velocity is carried out by comparing transmission times of a pulse in a specimen and in the comparison travel path. The ultrasonic velocities in liquids (for example, water) are well known and consequently the velocity in the specimen can be determined with an accuracy of about 0.1 %.

X2.5.2 In practice, the echo in the specimen is made to coincide with the echo from the interferometer travel path which is obtained by altering the latter to the point of interference. The ultrasonic velocities of the specimen and interferometer liquid are in the ratio of their lengths and these two quantities must be exactly measureable.

X2.5.3 A normal probe is clamped to the open tank by means of a clamp on one side. The frequency of the probe should be equal to that which is required for the specimen. The attenuation member must be inserted between the interferometer probe and the cable. It serves to change the height of the interferometer echo independently of other conditions of test.

X2.5.4 A reflector dips into the tank containing the liquid and is held on an adjustable mechanism so that it cannot be tilted. This mechanism can be moved to and fro rapidly by disengagement. The fine adjustment is carried out by means of a spindle. One complete revolution of the spindle changes the travel path by 1 mm. One scale division of the spindle knob represents  $1/100 \text{ mm}$  (0.0004 in.).

X2.5.5 The tank must be filled with liquid in which the ultrasonic velocity is known. In the case of water at  $20^\circ\text{C}$ , velocity =  $1483.1 \text{ m/s}$ . The temperature coefficient is  $\Delta v / \Delta t = +2.5 \text{ m/s} \cdot ^\circ\text{C}$ . A check of the temperature in the case of water is therefore absolutely necessary (see Appendix X4).

X2.5.6 Mixtures can also be used, for example, water alcohol (18% weight percentage), whose temperature coefficient is zero at room temperature.

X2.5.7 Calculate velocity as follows:

$$\text{Velocity}_x \text{ (m/s)} = \frac{\text{Velocity}_{\text{water}} \text{ (m/s)} \times \text{Thickness}_x \text{ (m)}}{\text{Distance}_{\text{in water}} \text{ (m)}}$$

or

<sup>4</sup> The boldface numbers in parentheses refer to the list of references appended to this practice.

$$\text{Velocity}_x \text{ (in./s)} = \frac{\text{Velocity}_{\text{water}} \text{ (in./s)} \times \text{Thickness}_x \text{ (in.)}}{\text{Distance}_{\text{in water}} \text{ (in.)}}$$

**X2.6 Pulse Velocity Through Concrete (see Test Method C 597)**

X2.6.1 Frequency of pulse generator 10 to 50 kHz—  
 Repetitive pulses at rate not less than 50/s.

X2.6.2 Press the faces of the search units against the faces of the concrete after establishing contact through a coupling medium. Wetting the concrete with water, oil, or other viscous materials may be used to exclude entrapped air from between the contact surfaces of the diaphragms of the search unit and the surface of the concrete. Measure the length of the shortest direct path between the centers of the diaphragms and the time of travel on the A-scan display by aligning the strobe marker pulse opposite the received wave front and reading the calibrated dial, or by counting the number of cycles of the timing wave between the transmitted and received pulse.

**X2.7 Pulse Echo Twin-Probe Method**

X2.7.1 This method uses a single-probe housing containing two elements: one a sender, the other a receiver.

X2.7.2 Since ultrasonic velocity measurements are principally measurements of time, based on the thickness of a specimen, and since many thickness measuring instruments successfully measure thickness to a high degree of accuracy using this method it seems appropriate to include this method of velocity measurement in the practice.

NOTE X2.1—With the twin-probe method the pulse-echo transit time is a non-linear function of specimen thickness, which may introduce significant errors when that technique is used for velocity measurements. The non-linearity is discussed in Practice E 797. Errors in velocity measurement can be minimized by use of a calibration block having both velocity and thickness nearly equal to that of the specimen to be measured. Single transducer systems are generally more suitable for precision velocity measurements.

X2.7.3 All instruments where the twin-probe method of thickness measurement is recommended, including A-scan display units as well as meter read-out units, have precisely calibrated scales. The parallax problem is removed from many of the A-scan display units since the scale is engraved on the inside face of the display or is integral with the output signal. Parallax is not a major problem with meter read-out units or digital read-out units.

X2.7.4 Most twin-probe thickness measuring instruments use the first echo for measurement read-out. Thus the test ranges are usually fixed and precisely calibrated. There is no need to produce several back echoes to obtain an average transit time.

X2.7.5 Specimens with curved surfaces present less measuring problems as the first back echo is more representative of depth or time than a later back echo, say the fifth from a tube wall. In small diameter tubing the error may be greater than for equivalent flat specimens.

X2.7.6 Procedure:

X2.7.6.1 Calibrate the instrument and probe on a steel step block of known velocity. By adjustment of sweep delay and range controls, ensure that thickness readings for two or more thicknesses (high and low) occur at their proper distances (Fig. X2.1). The instrument and probe are properly calibrated for (1020 or 1095) steel at 5900 m/s ( $2.32 \times 10^5$  in./s).

X2.7.6.2 Measure the thickness of part with unknown velocity without changing sweep or range controls on the instrument. Check the actual thickness of the test area with calipers or a micrometer.

X2.7.6.3 Calculate unknown velocity as follows:

$$V_x = V_{\text{steel}} \times \frac{\text{actual thickness}}{\text{indicated thickness}}$$

where:  
 $V_x$  = unknown velocity.

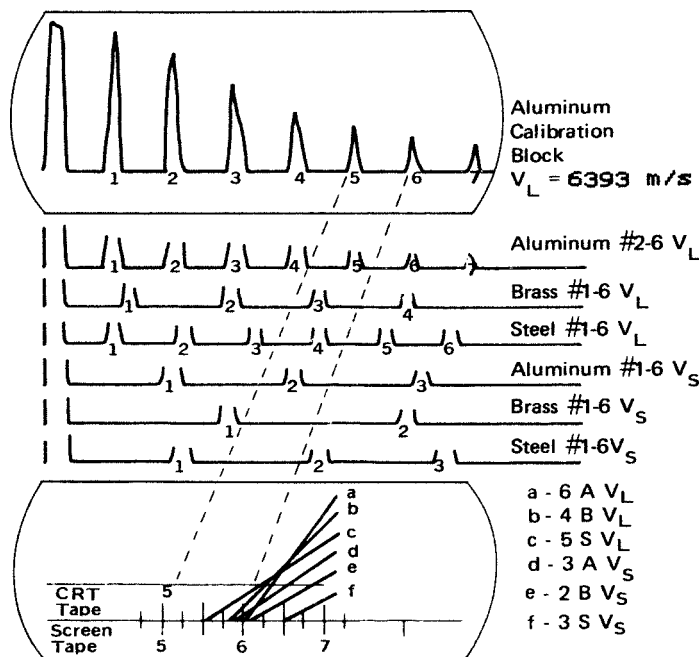


FIG. X2.1 Instrument Setup to Avoid Errors Due to Parallax

## X2.8 Harmonic Wave Method (Zero Method)

X2.8.1 Wall thickness measurement by means of ultrasonic, echo-sounding instruments will become inaccurate if only a few echoes can be utilized because of either high absorption, corrosion, or unfavorable radiation geometry. In such cases, the accuracy of the results can be improved by the tuning of the wall thickness meter to the harmonic waves of the echo frequency (harmonic wave method).

X2.8.2 Up to now the interferometer method has been used for the precision measurement of sound propagation. Further development of the harmonic wave method can replace the rather complicated and time-consuming interferometer method in all those cases where the ultimate accuracy of the latter is not required. Under normal conditions, a measuring accuracy of 0.5 % or better can be obtained with the so-called "zero-method."

X2.8.3 A modification of the method utilizes bursts of radio frequency (rf) radiated from a transducer into a long buffer rod and then into the sample, which is a few wavelengths thick. The buffer rod is long enough to contain the entire rf bursts, while the burst is long enough to occupy the three round-trips in the specimen. Thus the burst interferes with itself as it reverberates within the specimen. One characteristic echo pattern occurs when the round-trip distance in the specimen is equal to an odd number of half-wavelengths; an even number gives a different pattern. The two patterns alternate as the rf frequency is changed. One plots phase versus frequency in units of cycles versus MHz. One cycle of phase occurs for each repetition of one of the characteristic patterns; between the two patterns there is  $\frac{1}{2}$  cycle of phase. The slope of the phase versus frequency line is the delay time  $t$  in microseconds, and for a specimen of thickness  $L$ , the velocity is

$$v = 2L/t$$

## X2.9 Phase Comparison Method

X2.9.1 This method consists of superimposing the echoes of two pulses which have made different numbers of round trips. If the echoes are made exactly in phase by a critical adjustment of frequency, the expression for phase angles may be written as:

$$\gamma - [(2L W_n)/v] = -2 \pi n$$

where:

- $v$  = velocity of propagation,
- $W_n$  =  $2 \pi$  times resonant frequency ( $f_n$ ),
- $L$  = thickness,
- $n$  = number of waves, and
- $\gamma$  = phase angle due to the seal between the transducer and the specimen.

Consequently, the velocity is expressed by:

$$v = (2L f_n) / [n + (\gamma/2\pi)]$$

X2.9.2 It has been experimentally proven that size and shape effects are reduced to effectively zero whenever there are at least 100 wave lengths of sound in the specimen thickness. High frequencies (10 to 20 MHz) are generally used to minimize this effect.

X2.9.3 The main advantage of the phase comparison method is the fact that the absolute velocity can be determined

very accurately without the error introduced from coupling, since the transducer coupling effect can be evaluated. This method also makes it possible to measure the velocity on a very small specimen with linear dimensions as small as 2 mm (0.08 in.).

## X2.10 Pulse Superposition Method

X2.10.1 This method uses an rf pulse applied to the transducer at the intervals approximately equal to the round-trip delay time of waves traveling in the specimen. In order to observe the superimposed echoes just after the last applied pulse, a few applied pulses are omitted periodically. When the echoes are brought into phase adjusting the time spacing  $T$  between signals, a maximum in the resulting pulse amplitude occurs. In this condition, the following equation is satisfied:

$$\delta = (T/p) - (L/f) [m/p - (\gamma/2\pi)]$$

where:

- $\delta$  = round trip delay time,
- $f$  = rf frequency in the pulse,
- $m$  = an integer which may take on both positive and negative values, and
- $\gamma$  = a phase angle associated with wave reflected at the transducer end, and
- $p$  = an integer (1, 2, 3, . . .).

Since  $T$  is approximately some multiple of the round-trip delay time  $\delta$ , the applied pulse occurs once for every round trip delay for  $p = 1$ . Usually, a number of measurements of  $T$  at different frequencies between  $f$ , the resonance frequency of the transducer, and  $0.9 f_r$  are made to obtain the difference in  $T$  between  $f_r$  and another frequency  $f$ . The negative value of  $\Delta T$  that is smallest in magnitude corresponds to  $n = 0$ ; except for specimens of very low mechanical impedance, the delay time is then given by  $\delta = T + (\gamma/2\pi f)$ . The velocity in the sample is  $V = 2L/\delta$ , where  $L$  is the sample length.

X2.10.2 The advantage of this particular method is that the coupling to the transducer is taken into account so that this method is well suited to measurements aimed at pressure and temperature variations. With this method, the effect of coupling between transducer and specimen can be made negligibly small. So far as the accuracy of this method is concerned, it is within a few parts in  $10^5$  in ideal conditions, while that of the phase comparison in X2.9 is within one part in  $10^4$ . In this method, however, it is possible to send a strong signal into the specimen, so that the velocity measurement can be made even if the attenuation is high.

X2.10.3 The limitation of both techniques is expected to depend on various factors besides porosity, such as grain size and grain boundary conditions.

## X2.11 Phase Velocity by Pulse-Echo-Overlap Method

X2.11.1 In this method, pairs of echoes are compared by driving the x-axis of a viewing oscilloscope at a frequency equal to the reciprocal of the travel time between the echoes. By choosing the correct cyclic overlap for the rf within the echoes by the  $\Delta T$  method explained in X2.10, accurate measurement of ultrasonic phase velocity can be made. When corrections for the phase advance due to ultrasonic diffraction are applied to the travel times between various pairs of echoes,