An American National Standard

# Standard Terminology of Symbols and Definitions Relating to Magnetic Testing<sup>1</sup>

This standard is issued under the fixed designation A 340; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon  $(\epsilon)$  indicates an editorial change since the last revision or reapproval.

#### INTRODUCTION

In preparing this glossary of terms, an attempt has been made to avoid, where possible, vector analysis and differential equations so as to make the definitions more intelligible to the average worker in the field of magnetic testing. In some cases, rigorous treatment has been sacrificed to secure simplicity, but it is believed that none of the definitions will prove to be misleading.

It is the intent of this glossary to be consistent in the use of symbols and units with those found in ANSI/IEEE 260-1978 and USA Standard Y 10.5-1968.

# Part 1—Symbols Used in Magnetic Testing

Symbol	Term	H'	apparent magnetic field strength
		$\Delta H$	excursion range of magnetic field strength
α	cross-sectional area of B coil	$H_b$	biasing magnetic field strength
Α	cross-sectional area of specimen	$H_c$	coercive field strength
A'	solid area	$H_c$	apparent coercive field strength
	magnetic induction	$H_{ci}$	intrinsic coercive field strength
В	normal induction	$H_{cs}$	coercivity
	magnetic flux density	$H_d$	demagnetizing field strength
. 5	(https://stan	Ha ards liter	incremental magnetic field strength
ΔΒ	excursion range of induction	$H_{\Delta}^{-}$	apparent incremental magnetic field strength
$B_b$ .	biased induction	$H_g$	air gap magnetic field strength
$B_d$	remanent induction	HE Preview	Tac magnetic field strength (from an assumed
B <sub>dm</sub>	remanence		peak value of magnetizing current
$B_dH_d$	energy product	$H_m$	maximum magnetic field strength in a hyster-
$(B_dH_d)_m$	maximum energy product		esis loop
$B_{\!\scriptscriptstyle \Delta}$	incremental induction	H <sub>max</sub> 0_00 A	maximum magnetic field strength in a flux-
$B_i$	intrinsic induction AS I M	A max U=99A	current loop
B <sub>m</sub> https://standar	maximum induction in a hysteresis loop	H'max 1473-406d-89fd-	apparent maximum magnetic field strength in
B <sub>max</sub> https://standar	maximum induction in a flux current loop	3 max 14 / 3-4000-8910-	a flux-current loop
B <sub>r</sub>	residual induction	$H_{p}$	ac magnetic field strength (from a measured
B',	apparent residual induction	•	peak value of exciting current)
$B_{rs}$	retentivity	$H_t$	instantaneous magnetic field strength (coinci-
B <sub>s</sub> cf	saturation induction crest factor		dent with $B_{\rm max}$ )
CM	cyclically magnetized condition	$H_z$	ac magnetic field strength force (from an as-
			sumed peak value of exciting current)
d	lamination thickness	I	ac exciting current (rms value)
D <sub>B</sub>	demagnetizing coefficient	$I_c$	ac core loss current (rms value)
df	distortion factor	$I_{dc}$	constant current
$D_m$	magnetic dissipation factor	$I_m$	ac magnetizing current (rms value)
E	exciting voltage	J	magnetic polarization
E <sub>1</sub>	induced primary voltage	k'	coupling coefficient
$E_2$	induced secondary voltage	$\ell$	flux path length
E <sub>f</sub>	flux volts	$\ell_1$	effective flux path length
†	cyclic frequency in hertz	$\ell_{m{g}}$	gap length
F #	magnetomotive force	$\check{\mathscr{L}}$ (also $\phi$ N)	flux linkage
ff	form factor	$\mathscr{L}_{m}$	mutual flux linkage
Н	magnetic field strength	L	self inductance
		$L_1$	core inductance
		$L_{\Delta}$	incremental inductance
		$L_i^-$	intrinsic inductance
<sup>1</sup> These definitions are under the jurisdiction of ASTM Committee A-6 on		L <sub>m</sub>	mutual inductance
Magnetic Properties and are the direct responsibility of Subcommittee A06.92 on		L <sub>0</sub>	initial inductance
Terminology and Definitions.		Ls	series inductance
Current edition approved Oct. 10, 1999. Published December 1999. Originally		L <sub>w</sub>	winding inductance
Current cutton approved Oc	1. 10, 1999. Fublished December 1999. Originally	**	<del>-</del>

Copyright © ASTM, 100 Barr Harbor Drive, West Conshohocken, PA 19428-2959, United States.

published as A 340 - 49. Last previous edition A 340 - 99.



M	magnetic moment	γ	loss angle
M	magnetization	cos γ	magnetic power factor
m	total mass of a specimen	$\gamma_{p}$	proton gyromagnetic ratio
$m_1$	active mass of a specimen	$\Gamma_m$	magnetic constant
$N_D$	demagnetizing factor	δ	density
$N_1$	turns in a primary winding	K	susceptibility
N <sub>2</sub>	turns in a secondary winding	ac Permeabilities:	
$N_1I/\ell_1$	ac excitation	$\mu_a$	ideal permeability
p	magnetic pole strength	$\mu_{L}$	inductance permeability
<b>7</b> P	permeance	$\mu_{\Delta}L$	incremental inductance permeability
P	active (real) power	$\mu_{od}$	initial dynamic permeability
P <sub>a</sub>	apparent power	$\mu_p$	peak permeability
P <sub>a (B;f)</sub>	specific apparent power	$\mu_{\Delta p}$	incremental peak permeability
· a (B;1)	opcome apparem perior	$\mu_i$	instantaneous permeability
$P_{c}$	total core loss	$\mu_z$	impedance permeability
$P_{c (B;f)}$	specific core loss	$\mu_{\Delta z}$	incremental impedance permeability
C (B;1)	opositio della locci	dc Permeabilities:	moromornal impodurico pormodoliny
$P_{c\Delta}$	incremental core loss	μ	normal permeability
$P_e$	normal eddy current core loss	μ <sub>abs</sub>	absolute permeability
$P_{\Delta e}^{-}$	incremental eddy current core loss	$\mu_d$	differential permeability
$P_h$	normal hysteresis core loss	$\mu_{\Delta}$	incremental permeability
$P_{\Delta h}$	incremental hysteresis core loss	$\mu_{ m eff}$	effective circuit permeability
$P_q^{-\cdots}$	reactive (quadrature) power	$\mu_i$	intrinsic permeability
$P_r^{\gamma}$	residual core loss	$\mu_{\Delta i}$	incremental intrinsic permeability
$P_w$	winding loss (copper loss)	$\mu_m$	maximum permeability
$P_z$	exciting power	$\mu_0$	initial permeability
$P_{z (B;f)}^{-}$	specific exciting power	$\mu_{r}$	relative permeability
- (-)/		$\mu_{\nu}$ (also $\Gamma_{m}$ )	space permeability
$Q_m$	magnetic storage factor	$\mu_{rev}$	reversible permeability
R	reluctance	μ'/cot γ	figure of merit
$R_1$	core resistance	ν	reluctivity
$R_w$	winding resistance	π	the numeric 3.1416
s"	lamination factor (stacking factor)	ρ	resistivity
SCM	symmetrically cyclically magnetized condition	ondards	magnetic flux
$T_c$	Curie temperature	• mdards	flux linkage (see $\mathcal{L}$ )
w	lamination width	X	mass susceptibility
$\underline{\underline{W}}_h$	hysteresis loop loss	xo orde itak	initial susceptibility
<u>~</u> "	linear expansion, coefficient (average)	mai us.itei	angular frequency in radians per second
$\Delta \chi$	incremental tolerance		9 / 1
β	hysteretic angle		
•	hysteretic angle		

## Part 2—Definition of Terms Used in Magnetic Testing

### https://standards.iteh.ai/catalog/standards/sist/741fc33f-d473-406d-89fd-d882b2975cc3/astm-a340-99a

ac excitation,  $N_1I/\ell_1$ —the ratio of the rms ampere-turns of exciting current in the primary winding of an inductor to the effective flux path length of the inductor.

active (real) power, P—the product of the rms current, I, in an electrical circuit, the rms voltage, E, across the circuit, and the cosine of the angular phase difference,  $\theta$  between the current and the voltage.

#### $P = EI \cos\theta$

Note 1—The portion of the active power that is expended in a magnetic core is the total core loss,  $P_c$ .

**aging coefficient**—the percentage change in a specific magnetic property resulting from a specific aging treatment.

Note 2—The aging treatments usually specified are:

- (a) 100 h at 150°C or
- (b) 600 h at 100°C.

aging, magnetic—the change in the magnetic properties of a material resulting from metallurgic change due to a normal or specified aging condition.

Note 3—This term implies a deterioration of the magnetic properties of magnetic materials for electronic and electrical applications, unless otherwise specified.

air-gap magnetic field strength,  $H_g$ —the magnetic field

strength required to produce the induction existing at some point in a nonmagnetic gap in a magnetic circuit.

Note 4—In the cgs-emu system of units,  $H_g$  is numerically equal to the induction existing at such a point and exceeds the magnetic field strength in the magnetic material.

amorphous alloy—a semiprocessed alloy produced by a rapid quenching, direct casting process resulting in metals with noncrystalline structure.

ampere (turn), A—the unit of magnetomotive force in the SI system of units. The symbol A represents the unit of electric current, ampere, in the SI system of units.

**ampere per metre, A/m**—the unit of magnetic field strength in the SI system of units.

**anisotropic material**—a material in which the magnetic properties differ in various directions.

antiferromagnetic material—a feebly magnetic material in which almost equal magnetic moments are lined up antiparallel to each other. Its susceptibility increases as the temperature is raised until a critical (Neél) temperature is reached; above this temperature the material becomes paramagnetic.

**apparent coercive field strength,**  $H'_{c}$ —the value of apparent

- magnetic field strength on a flux-current loop coincident, with zero induction.
- **apparent magnetic field strength,** H'—the magnetic field strength value expressed in terms of the instantaneous exciting current, i:

(In cgs-emu system of units)  $H' = 0.4\pi N_1 I/\ell_1$ 

- apparent magnetic field strength, incremental,  $H'_{\Delta}$ —the magnetic field strength value developed for incremental flux-current loop.
- apparent magnetic field strength, maximum,  $H'_{\text{max}}$ —the maximum value of H' attained in a flux-current loop.
- **apparent power,**  $P_a$ —the product (volt-amperes) of the rms exciting current and the applied rms terminal voltage in an electric circuit containing inductive impedance. The components of this impedance as a result of the winding will be linear, while the components as a result of the magnetic core will be nonlinear. The unit of apparent power is the volt-ampere, VA.
- **apparent power, specific,**  $P_{a(B;f)}$ —the value of the apparent power divided by the active mass of the specimen, that is, volt-amperes per unit mass. The values of voltage and current are those developed at a maximum value of cyclically varying induction B and specified frequency f.
- **apparent residual induction,** B'<sub>r</sub>—the value of induction on a flux-current loop when the apparent magnetic field strength has a zero value.
- **area,** A—the geometric cross-sectional area of a magnetic path which is perpendicular to the direction of the induction.
- **Bloch wall**—a domain wall in which the magnetic moment at any point is substantially parallel to the wall surface. See also **domain wall.**
- **Bohr magneton**—a constant that is equal to the magnetic moment of an electron because of its spin. The value of the constant is  $(9\ 274\ 078\times 10^{-21}\ erg/gauss$  or  $9\ 274\ 078\times 10^{-24}\ J/T)$ .
- **cgs-emu system of units**—the system for measuring physical quantities in which the base units are the centimetre, gram, and second, and the numerical value of the magnetic constant,  $\Gamma_m$ , is unity.
- coercive field strength,  $H_c$ —the (dc) magnetic field strength required to restore the magnetic induction to zero after the material has been symmetrically cyclically magnetized.
- coercive field strength, intrinsic,  $H_{c\ell}$ —the (dc) magnetic field strength required to restore the instrinsic magnetic induction to zero after the material has been symmetrically cyclically magnetized.
- **coercivity,**  $H_{cs}$ —the maximum value of coercive field strength that can be attained when the magnetic material is symmetrically cyclically magnetized to saturation induction,  $B_S$ .
- **core, laminated**—a magnetic component constructed by stacking suitably thin pieces of magnetic material which are stamped, sheared, or milled from sheet or strip material. Individual pieces usually have an insulating surface coating to minimize eddy current losses in the assembled core.
- core, mated—two or more magnetic core segments assembled with the magnetic flux path perpendicular to the mating surface.
- core, powder (dust)—a magnetic core comprised of small

- particles of electrically insulated metallic ferromagnetic material. These cores are characterized by low hysteresis and eddy current losses.
- **core, tape-wound**—a magnetic component constructed by the spiral winding of strip material onto a suitable mandrel. The strip material usually has an insulating surface coating which reduces interlaminar eddy current losses in the finished core. *core loss current, ac*—, *I<sub>c</sub>*—See **current, ac core loss.**
- core loss, ac eddy current, incremental,  $P_{\Delta e}$ —the power loss caused by eddy currents in a magnetic material that is cyclically magnetized.
- core loss, ac eddy current, normal,  $P_e$ —the power losses as a result of eddy currents in a magnetic material that is symetrically cyclically magnetized.
- Note 5—The voltage is generally assumed to be across the parallel combination of core inductance,  $L_1$ , and core resistance,  $R_1$ .
- **core loss, ac, incremental,**  $P_{c\Delta}$ —the core loss in a magnetic material when the material is subjected simultaneously to a dc biasing magnetizing force and an alternating magnetizing force.
- **core loss, residual,**  $P_r$ —the portion of the core loss power,  $P_c$ , which is not attributed to hysteresis or eddy current losses from classical assumptions.
- **core loss, ac, specific,**  $P_{c(B;f)}$ —the active power (watts) expended per unit mass of magnetic material in which there is a cyclically varying induction of a specified maximum value, B, at a specified frequency, f.
- **core loss, ac, (total),**  $P_c$ —the active power (watts) expended in a magnetic circuit in which there is a cyclically alternating induction.
- Note 6—Measurements of core loss are normally made with sinusoidally alternating induction, or the results are corrected for deviations from the sinusoidal condition.
- core plate—a generic term for any insulating material, formed metallurigically or applied externally as a thin surface coating, on sheet or strip stock used in the construction of laminated and tape wound cores.
- **coupling coefficient,** k'—the ratio of the mutual inductance between two windings and the geometric mean of the individual self-inductances of the windings.
- **crest factor,** *cf*—the ratio of the maximum value of a periodically alternating quantity to its rms value.
- Note 7—For a sinusoidal variation the crest factor is  $\sqrt{2}$  .
- Curie temperature,  $T_c$ —the temperature above which a ferromagnetic material becomes paramagnetic.
- **current, ac core loss,**  $I_c$ —the rms value of the in-phase component (with respect to the induced voltage) of the exciting current supplied to a coil which is linked with a ferromagnetic core.
- **current, ac exciting,** *I*—the rms value of the total current supplied to a coil that is linked with a ferromagnetic core.
- Note 8—Exciting current is measured under the condition that any other coil linking the same core carries no current.
- **current, ac, magnetizing,**  $I_m$ —the rms value of the magnetizing component (lagging with respect to applied voltage) of

the exciting current supplied to a coil that is linked with a ferromagnetic core.

current, dc,  $I_{dc}$ —a steady-state dc current. A dc current flowing in an inductor winding will produce a unidirectional magnetic field in the magnetic material.

customary units—a set of industry-unique units from the cgs-emu system of units and U.S. inch-pound systems and units derived from the two systems.

Note 9-Examples of customary units used in ASTM A-6 standards include:

Quantity Name	Quantity Symbol	Unit Name	Unit Symbol
Magnetic field strength	Н	oersted	Oe
Magnetic induction (magnetic	В	gauss	G
flux density)			
Specific core loss	$P_c(\beta;f)$	watt/pound	W/lb

**cyclically magnetized condition,** CM—a magnetic material is in a cyclically magnetized condition when, after having been subjected to a sufficient number of identical cycles of magnetizing field, it follows identical hysteresis or fluxcurrent loops on successive cycles which are not symmetrical with respect to the origin of the axes.

demagnetization curve—the portion of a flux versus dc current plot (dc hysteresis loop) that lies in the second or fourth quadrant, that is, between the residual induction point,  $B_r$ , and the coercive force point,  $H_c$ . Points on this curve are designated by the coordinates,  $B_d$  and  $H_d$ .

**demagnetizing coefficient,**  $D_B$ —is defined by the equation:

$$D_R = \lceil \Gamma_m (H_a - H) \rceil / B_i$$

where:

 $H_a$  = applied magnetic field strength,

= magnetic field strength actually existing in the magnetic material,

 $B_i$  = intrinsic induction, and 1/catalog/standards/sist/74 $\Gamma_m$  = 1 in the cgs system and  $4\pi \times 10^{-7}$ , henry/metre in the mksa system (rationalized).

Note 10-For a closed, uniform magnetic circuit, the demagnetizing coefficient is zero.

**demagnetizing factor,**  $N_D$ —defined as  $4\pi$  times the demagnetizing coefficient,  $D_B$ .

**demagnetizing field strength,**  $H_d$ —a magnetic field strength applied in such a direction as to reduce the induction in a magnetized body. See demagnetization curve.

**density,**  $\delta$ — the ratio of mass to volume of a material. In the cgs-emu system of units, g/cm<sup>3</sup>. In SI units, kg/m<sup>3</sup>.

diamagnetic material—a material whose relative permeability is less than unity.

Note 11—The intrinsic induction,  $B_i$ , is oppositely directly to the applied magnetizing force H.

dissipation factor, magnetic,  $D_m$ —the tangent of the hysteretic angle that is equal to the ratio of the core loss current,  $I_c$ , to the magnetizing current,  $I_m$ . Thus:

$$D_m = \tan \beta = \cot \gamma = I_c/I_m = \omega L_1/R_1 = I/Q_m$$

Note 12—This dissipation factor is also given by the ratio of the energy dissipated in the core per cycle of a periodic SCM excitation (hysteresis and eddy current heat loss) to  $2\pi$  times the maximum energy stored in the

distortion, harmonic—the departure of any periodically varying waveform from a pure sinusoidal waveform.

Note 13—The distorted waveform that is symmetrical about the zero amplitude axis and is most frequently encountered in magnetic testing contains only the odd harmonic components, that is fundamental, 3rd harmonic, 5th harmonic, and so forth. Nonsymmetrical distorted waveforms must contain some even harmonic components, in addition to the fundamental and, perhaps, some odd harmonic components.

**distortion factor,** df—a numerical measure of the distortion in any ac nonsinusoidal waveform. For example, if by Fourier analysis or direct measurement  $E_1$ ,  $E_2$ ,  $E_3$ , and so forth are the effective values of the pure sinusoidal harmonic components of a distorted voltage waveform, then the distortion factor is the ratio of the root mean square of the second and all higher harmonic components to the fundamental compo-

$$df = [E_2^2 + E_3^2 + E_4^2 + \cdots]^{1/2} E_1$$

Note 14—There are no dc components  $(E_0)$  in the distortion factor.

domains, ferromagnetic-magnetized regions, either macroscopic or microscopic in size, within ferromagnetic materials. Each domain, in itself, is magnetized to intrinsic saturation at all times, and this saturation induction is unidirectional within the domain.

domain wall—a boundary region between two adjacent domains within which the orientation of the magnetic moment of one domain changes into a different orientation of the magnetic moment in the other domain.

eddy current—an electric current developed in a material as a result of induced voltages developed in the material.

effective circuit permeability,  $\mu_{eff}$ —when a magnetic circuit consists of two or more components, each individually homogeneous throughout but having different permeability values, the effective (overall) permeability of the circuit is that value computed in terms of the total magnetomotive force, the total resulting flux, and the geometry of the circuit.

electrical steel—a term used commercially to designate strip or sheet used in electrical applications and historically has referred to flat-rolled, low-carbon steels or alloyed steels with silicon or aluminum, or both. Common types of electrical steels used in the industry are grain-oriented electrical steel, nonoriented electrical steel, and magnetic lamination steel.

electrical steel, grain oriented—a flat-rolled silicon-iron alloy usually containing approximately 3 % silicon, having enhanced magnetic properties in the direction of rolling and normally used in transformer cores.

electrical steel, nonoriented—a flat-rolled silicon-iron or silicon-aluminum-iron alloy containing 0.0 to 3.5 % silicon and 0.0 to 1.0 % aluminum and having similar core loss in all directions.

emu—the notation emu is an indicator of electromagnetic units. When used in conjunction with magnetic moment, M, it denotes units of ergs per oersted, erg/Oe. A moment of 1 erg/Oe is produced by a current of 10 amperes (1 abampere) flowing in a loop of area 1 cm<sup>2</sup>. The work done to rotate a moment of 1 erg/Oe from parallel to perpendicular in a uniform field of 1 Oe is 1 erg. The conversion to the SI units of magnetic moment J/T (joule/tesla) or A m<sup>2</sup> is given by

$$\frac{\text{erg/Oe (cgs-emu)}}{\text{J/T (SI)}} \equiv \frac{10 \text{ amperes cm}^2 \text{ (cgs-emu)}}{\text{A m}^2 \text{ (SI)}} = 10^{-3} \tag{1}$$

Magnetization, M, the magnetic moment per unit volume, has units erg/(Oe-cm<sup>3</sup>), often expressed as emu/cm<sup>3</sup>.

**energy product,**  $B_dH_d$ —the product of the coordinate values of any point on a demagnetization curve.

energy-product curve, magnetic—the curve obtained by plotting the product of the corresponding coordinates,  $B_d$  and  $H_d$ , of points on the demagnetization curve as abscissa against the induction,  $B_d$ , as ordinates.

Note 15—The maximum value of the energy product,  $(B_dH_d)_m$ , corresponds to the maximum value of the external energy.

Note 16-The demagnetization curve is plotted to the left of the vertical axis and usually the energy-product curve to the right.

**energy product, maximum**  $(B_dH_d)_m$ —for a given demagnetization curve, the maximum value of the energy product.

equipment test level accuracy—(1) For a single test equipment, using a large group of test specimens, the average percentage of test deviation from the correct average value.

(2) The average percentage deviation from the average value obtained from similar tests, on the same test specimen or specimens, when measured with a number of other test equipments that have previously been proven to have both suitable reproducibility of measurement and test level, and whose calibrations and quality have general acceptance for standardization purposes and where better equipment for establishing the absolute accuracy of test is not available.

exciting current, ac, I—See current, ac exciting.

**exciting power, rms,**  $P_z$ —the product of the ac rms exciting current and the rms voltage induced in the exciting (primary) winding on a magnetic core. al/catalog/standa

Note 17—This is the apparent volt-amperes required for the excitation of the magnetic core only. When the core has a secondary winding, the induced primary voltage is obtained from the measured open-circuit secondary voltage multiplied by the appropriate turns ratio.

exciting power, specific,  $P_{z(B;f)}$ —the value of the ac rms exciting power divided by the active mass of the specimen (volt-amperes/unit mass) taken at a specified maximum value of cyclically varying induction B and at a specified frequency f.

exciting voltage, E—the ac rms voltage across a winding linking the flux of a magnetic core. The voltage across the winding equals that across the assumed parallel combination of core inductance  $L_1$ , and core resistance,  $R_1$ .

feebly magnetic material—a material generally classified as" nonmagnetic," whose maximum normal permeability is less than 4.

ferrimagnetic material—a material whose atomic magnetic moments are both ordered and anti-parallel but being unequal in magnitude produce a net magnetization in one direction.

ferrite—a term referring to magnetic oxides in general, and especially to material having the formula M O Fe<sub>2</sub> O<sub>3</sub>, where M is a divalent metal ion or a combination of such ions. Certain ferrites, magnetically "soft" in character, are useful for core applications at radio and higher frequencies because of their advantageous magnetic properties and high volume resistivity. Other ferrites, magnetically "hard" in character, have desirable permanent magnet properties.

ferromagnetic material—a material whose magnetic moments are ordered and parallel producing magnetization in one direction.

**figure of merit, magnetic,**  $\mu'/\cot \gamma$ —the ratio of the real part of the complex relative permeability to the dissipation factor of a ferromagnetic material.

Note 18—The figure of merit index of the magnetic efficiency of the core in various ac electromagnetic devices.

flux-current loop, incremental (biased)—the curve developed by plotting magnetic induction, B, versus magnetic field strength, H, when the magnetic material is cyclically magnetized while under dc bias condition. This loop will not be symmetrical about the B and H axes.

flux-current loop, normal—the curve developed by plotting magnetic induction, B, versus magnetic field strength, H, when the magnetic material is symmetrically cyclically magnetized.

Note 19—The area of the loop is proportional to the sum of the static hysteresis loss and all dynamic losses.

flux linkage,  $\mathcal{L}$ —the sum of all flux lines in a coil.

$$\mathcal{L} = \phi_1 + \phi_2 + \phi_3 + \cdots \phi_N$$

where:

 $\phi_I$  = flux linking turn 1;

Note 20—When the coupling coefficient, k', is less than unity, the flux linkage equals the product of the average flux linking the turns and the total number of turns. When the coupling coefficient is equal to unity, the flux linkage equals the product of the total flux linking the coil and the total number of turns.

flux linkage, mutual,  $\mathcal{L}_m$ —the flux linkage existing between two windings on a magnetic circuit. Mutual linkage is maximum when the coupling coefficient is unity.

flux path length,  $\ell$ —the distance along a flux loop.

flux path length, effective,  $\ell_1$  —the calculated length of the flux paths in a magnetic core, which is used in the calculations of certain magnetic parameters.

**flux volts,**  $E_f$ —the voltage induced in a winding of a magnetic component when the magnetic material is subjected to repeated magnetization under SCM or CM conditions.

$$E_f = 4.443 \ B_{\rm max} A' N f \times 10^{-8} \ {
m V} \ (SCM \ {
m excitation})$$
  
 $E_f = 2.221 \ \Delta \ B A' \ N f \times 10^8 \ {
m V} \ (CM \ {
m excitation})$   
 $E_f = 1.1107 \ E_{\rm avg}$ 

which

A' =solid cross-sectional area of the core in cm<sup>2</sup>,

N = number of winding turns, and

= the frequency in hertz.

form factor, ff—the ratio of the rms value of a periodically alternating quantity to its average absolute value.

Note 21—For a sinusoidal variation, the form factor is:

$$\pi/2\sqrt{2} = 1.1107$$

frequency, angular, ω—the number of radians per second traversed by a rotating vector that represents any periodically varying quantity.

Note 22—Angular frequency,  $\omega$ , is equal to  $2\pi$  times the cyclic frequency, f.

**frequency, cyclic,** *f*—the number of hertz (cycles/second) of a periodic quantity.

**gap length,**  $\ell_g$ —the distance that the flux transverses in the central region of a gap in a core having an "air" (nonmagnetic) gap in the flux path may be considered unity in the gap.

gauss (plural gausses), G—the unit of magnetic induction in the cgs-emu system of units. The gauss is equal to 1 maxwell per square centimetre of  $10^{-4}$  tesla. See magnetic induction (flux density).

**gilbert, Gb**—the unit of magnetomotive force in the cgs-emu system of units. The gilbert is a magnetomotive force of  $4\pi/10$  ampere-turns. See **magnetomotive force.** 

**gyromagnetic ratio, proton,**  $\gamma_p$ —the ratio of the magnetic moment of a hydrogen nucleus to its angular momentum.

Note 23—The gyromagnetic ratio is used to calculate the magnetic field from a measured resonance frequency when using the nuclear magnetic resonance technique.

The relationship is:

$$B = (2\pi f/\gamma_p)$$
 gausses  $= (2\pi f/\gamma_p) \times 10^{-4}$  teslas

where:

f = resonance frequency in cycles per second (hertz) and  $\gamma_p$  = gyromagnetic ratio (the accepted value at present for water is  $2.675 \ 12 \times 10^4 \ \text{gauss}^{-1} \ \text{s}^{-1}$ ).

henry (plural henries), H—the unit of self- or mutual inductance. The henry is the inductance of a circuit in which a voltage of 1 V is induced by a uniform rate of change 1 A/s in the circuit. Alternatively, it is the inductance of a circuit in which an electric current of 1 A/s produces a flux linkage of one weber turn (Wb turn) or 10<sup>8</sup> maxwell-turns. See inductance, mutual, and inductance, self.

**hertz, Hz**—the unit of cyclic frequency, f.

**hysteresis loop, biased**—an incremental hysteresis loop that lies entirely in any one quadrant.

Note 24—In this case, both of the limiting values of H and B are in the same direction.

**hysteresis loop, incremental**—the hysteresis loop, nonsymmetrical with respect to the *B* and *H* axes, exhibited by a ferromagnetic material in a *CM* condition.

Note 25—In this case, both of the limiting values H may have opposite polarity, but definitely have different absolute values of  $H_m$ . An incremental loop may be initiated at either some point on a normal hysteresis loop or at some point on the normal induction curve of the specimen.

**hysteresis loop, intrinsic**—a hysteresis loop obtained with a ferromagnetic material by plotting (usually to rectangular coordinates) corresponding dc values of intrinsic induction,  $B_i$ , for ordinates and magnetic field strength H for abscissae. **hysteresis loop, normal**—a closed curve obtained with a

ferromagnetic material by plotting (usually to rectangular coordinates) corresponding dc values of magnetic induction (B) for ordinates and magnetic field strength (H) for abscissa when the material is passing through a complete cycle between equal definite limits of either magnetic field strength,  $\pm H_m$ , or magnetic induction,  $\pm B_m$ . In general, the normal hysteresis loop has mirror symmetry with respect to the origin of the B and H axes, but this may not be true for special materials.

**hysteresis loop loss,**  $W_h$ —the power expended in a single slow excursion around a normal hysteresis loop. The energy is the integrated area enclosed by the loop measured in gauss-oersteds. Using the cgs-emu system of units:

$$W_h = (\int HdB/4\pi) \text{ ergs}$$

where the integrated area enclosed by the loop is measured in gauss-oersteds.

hysteresis loss, incremental,  $P_{\Delta h}$ —the power (watts) as a result of hysteresis expended in a ferromagnetic material while being driven through an incremental flux-current loop by a CM-type of excitation.

**hysteresis loss, normal,**  $P_h$ —(I) the power expended in a ferromagnetic material, as a result of hysteresis, when the material is subjected to a SCM excitation.

(2) The energy loss/cycle in a magnetic material as a result of magnetic hysteresis when the induction is cyclic (but not necessarily periodic).

hysteresis loss, rotational—the hysteresis loss that occurs in a body when subjected to a constant magnetizing force, the direction of which rotates with respect to the body, either in a continuously cyclic or in a repeated oscillatory manner.

hysteresis, magnetic—the property of a ferromagnetic material exhibited by the lack of correspondence between the changes in induction resulting from increasing magnetic field strength and from decreasing magnetic field strength.

**hysteretic angle, magnetic,**  $\beta$ —the mean angle by which the fundamental component of exciting current leads the fundamental component of magnetizing current,  $I_m$ , in an inductor having a ferromagnetic core.

Note 26—Because of hysteresis, the instantaneous value of the hysteretic angle will vary during the cycle of SCM excitation. However,  $\beta$  is taken to be the mean effective value of this angle.

**inductance, core,**  $L_1$ —the effective parallel circuit inductance of a ferromagnetic core based upon a hypothetical nonresistive path that is exclusively considered to carry the magnetizing current,  $I_m$ .

Note 27—The product  $I_m^2 \omega L_1$  equals the quadrature power delivered to the core.

inductance, incremental,  $L_{\Delta}$ —the self-inductance of an electrical circuit when the ferromagnetic core has an ac cyclic magnetization produced by specified values of both ac and dc components of the exciting current.

**inductance, initial,**  $L_0$ —the limiting value of the core inductance,  $L_1$  reached in a ferromagnetic core when, under ac symmetrical cyclic excitation, the magnetizing current has been progressively and gradually reduced from a comparatively high value to a zero value.