



Edition 1.0 2011-06

# INTERNATIONAL STANDARD Information technology - Microprocessor Systems - Floating-Point arithmetic



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## INTERNATIONAL STANDARD

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ISO/IEC/IEEE 60559 was prepared by the Microprocessor Standards Committee of the IEEE Computer Society of the IEEE (as IEEE 754-2008). It was adopted by Joint Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 25, *Interconnection of information technology equipment* in parallel with its approval by the ISO/IEC national bodies, under the "fast-track procedure" defined in the Partner Standards Development Organization cooperation agreement between ISO and IEEE. IEEE is responsible for the maintenance of this document with participation and input from ISO/IEC national bodies.

This first edition, published as ISO/IEC/IEEE 60559, replaces the second edition of IEC 60559.

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This introduction is not part of IEEE Std 754-2008, IEEE Standard for Floating-Point Arithmetic.

This standard is a product of the Floating-Point Working Group of, and sponsored by, the Microprocessor Standards Committee of the IEEE Computer Society.

This standard provides a discipline for performing floating-point computation that yields results independent of whether the processing is done in hardware, software, or a combination of the two. For operations specified in the normative part of this standard, numerical results and exceptions are uniquely determined by the values of the input data, the operation, and the destination, all under user control.

This standard defines a family of commercially feasible ways for systems to perform binary and decimal floating-point arithmetic. Among the desiderata that guided the formulation of this standard were:

- a) Facilitate movement of existing programs from diverse computers to those that adhere to this standard as well as among those that adhere to this standard.
- b) Enhance the capabilities and safety available to users and programmers who, although not expert in numerical methods, might well be attempting to produce numerically sophisticated programs.
- c) Encourage experts to develop and distribute robust and efficient numerical programs that are portable, by way of minor editing and recompilation, onto any computer that conforms to this standard and possesses adequate capacity. Together with language controls it should be possible to write programs that produce identical results on all conforming systems.
- d) Provide direct support for
  - execution-time diagnosis of anomalies,
  - smoother handling of exceptions
  - interval arithmetic at a reasonable cost.
- e) Provide for development of
  - standard elementary functions such as exp and cos
  - high precision (multiword) arithmetic
  - coupled numerical and symbolic algebraic computation.

https://standarf) Enable rather than preclude further refinements and extensions. -cec0b6fdf80a/iso-iec-iece-60559-2011

In programming environments, this standard is also intended to form the basis for a dialog between the numerical community and programming language designers. It is hoped that language-defined methods for the control of expression evaluation and exceptions might be defined in coming years, so that it will be possible to write programs that produce identical results on all conforming systems. However, it is recognized that utility and safety in languages are sometimes antagonists, as are efficiency and portability.

Therefore, it is hoped that language designers will look on the full set of operation, precision, and exception controls described here as a guide to providing the programmer with the ability to portably control expressions and exceptions. It is also hoped that designers will be guided by this standard to provide extensions in a completely portable way.

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## INFORMATION TECHNOLOGY — MICROPROCESSOR SYSTEMS —

### **Floating-Point arithmetic**

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#### 1. Overview

#### 1.1 Scope

This standard specifies formats and methods for floating-point arithmetic in computer systems—standard and extended functions with single, double, extended, and extendable precision—and recommends formats for data interchange. Exception conditions are defined and standard handling of these conditions is

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#### 1.2 Purpose

This standard provides a method for computation with floating-point numbers that will yield the same result whether the processing is done in hardware, software, or a combination of the two. The results of the computation will be identical, independent of implementation, given the same input data. Errors, and error conditions, in the mathematical processing will be reported in a consistent manner regardless of implementation.

#### **1.3 Inclusions**

This standard specifies:

- Formats for binary and decimal floating-point data, for computation and data interchange.
- Addition, subtraction, multiplication, division, fused multiply add, square root, compare, and other operations.
- Conversions between integer and floating-point formats.
- Conversions between different floating-point formats.
- Conversions between floating-point formats and external representations as character sequences.
- Floating-point exceptions and their handling, including data that are not numbers (NaNs).

#### **1.4 Exclusions**

This standard does not specify:

- Formats of integers.
- Interpretation of the sign and significand fields of NaNs.

#### 1.5 Programming environment considerations

This standard specifies floating-point arithmetic in two radices, 2 and 10. A programming environment may conform to this standard in one radix or in both.

This standard does not define all aspects of a conforming programming environment. Such behavior should be defined by a programming language definition supporting this standard, if available, and otherwise by a particular implementation. Some programming language specifications might permit some behaviors to be defined by the implementation.

Language-defined behavior should be defined by a programming language standard supporting this standard. Then all implementations conforming both to this floating-point standard and to that language standard behave identically with respect to such language-defined behaviors. Standards for languages intended to reproduce results exactly on all platforms are expected to specify behavior more tightly than do standards for languages intended to maximize performance on every platform.

Because this standard requires facilities that are not currently available in common programming languages, the standards for such languages might not be able to fully conform to this standard if they are no longer being revised. If the language can be extended by a function library or class or package to provide a conforming environment, then that extension should define all the language-defined behaviors that would normally be defined by a language standard.

**Implementation-defined** behavior is defined by a specific implementation of a specific programming environment conforming to this standard. Implementations define behaviors not specified by this standard nor by any relevant programming language standard or programming language extension.

Conformance to this standard is a property of a specific implementation of a specific programming environment, rather than of a language specification.

However a language standard could also be said to conform to this standard if it were constructed so that the every conforming implementation of that language also conformed automatically to this standard.

#### 1.6 Word usage

In this standard three words are used to differentiate between different levels of requirements and optionality, as follows:

- may indicates a course of action permissible within the limits of the standard with no implied preference ("may" means "is permitted to")
- **shall** indicates mandatory requirements strictly to be followed in order to conform to the standard and from which no deviation is permitted ("shall" means "is required to")
- should indicates that among several possibilities, one is recommended as particularly suitable, without mentioning or excluding others; or that a certain course of action is preferred but not necessarily required; or that (in the negative form) a certain course of action is deprecated but not prohibited ("should" means "is recommended to").

Further:

- might indicates the possibility of a situation that could occur, with no implication of the likelihood
  of that situation ("might" means "could possibly")
- see followed by a number is a cross-reference to the clause or subclause of this standard identified by that number
- NOTE introduces text that is informative (that is, is not a requirement of this standard).

#### 2. Definitions, abbreviations, and acronyms

#### 2.1 Definitions

For the purposes of this standard, the following terms and definitions apply.

**2.1.1 applicable attribute:** The value of an attribute governing a particular instance of execution of a computational operation of this standard. Languages specify how the applicable attribute is determined.

**2.1.2 arithmetic format:** A floating-point format that can be used to represent floating-point operands or results for the operations of this standard.

**2.1.3 attribute:** An implicit parameter to operations of this standard, which a user might statically set in a programming language by specifying a constant value. The term attribute might refer to the parameter (as in "rounding-direction attribute") or its value (as in "roundTowardZero attribute").

**2.1.4 basic format:** One of five floating-point representations, three binary and two decimal, whose encodings are specified by this standard, and which can be used for arithmetic. One or more of the basic formats is implemented in any conforming implementation.

**2.1.5 biased exponent:** The sum of the exponent and a constant (bias) chosen to make the biased exponent's range nonnegative.

2.1.6 binary floating-point number: A floating-point number with radix two

**2.1.7 block:** A language-defined syntactic unit for which a user can specify attributes. Language standards might provide means for users to specify attributes for blocks of varying scopes, even as large as an entire program and as small as a single operation.

**2.1.8 canonical encoding:** The preferred encoding of a floating point representation in a format. Applied to declets, significands of finite numbers, infinities, and NaNs, especially in decimal formats.

2.1.9 canonicalized number: A floating-point number whose encoding (if there is one) is canonical.

**2.1.10 cohort:** The set of all floating-point representations that represent a given floating-point number in a given floating-point format. In this context -0 and +0 are considered distinct and are in different cohorts.

**2.1.11 computational operation:** An operation that can signal floating-point exceptions, or that produces floating-point results, or that produces integer results by rounding them to fit destination formats according to a rounding direction rule. Comparisons are computational operations.

**2.1.12 correct rounding:** This standard's method of converting an infinitely precise result to a floating-point number, as determined by the applicable rounding direction. A floating-point number so obtained is said to be correctly rounded.

2.1.13 decimal floating-point number: A floating-point number with radix ten.

**2.1.14 declet:** An encoding of three decimal digits into ten bits using the densely-packed-decimal encoding scheme. Of the 1024 possible declets, 1000 canonical declets are produced by computational operations, while 24 non-canonical declets are not produced by computational operations, but are accepted in operands.

#### 2.1.15 denormalized number: See: subnormal number.

**2.1.16 destination:** The location for the result of an operation upon one or more operands. A destination might be either explicitly designated by the user or implicitly supplied by the system (for example, intermediate results in subexpressions or arguments for procedures). Some languages place the results of intermediate calculations in destinations beyond the user's control; nonetheless, this standard defines the result of an operation in terms of that destination's format and the operands' values.

**2.1.17 dynamic mode:** An optional method of dynamically setting attributes by means of operations of this standard to set, test, save, and restore them.

**2.1.18 exception:** An event that occurs when an operation on some particular operands has no outcome suitable for every reasonable application. That operation might signal one or more exceptions by invoking the default or, if explicitly requested, a language-defined alternate handling. Note that *event*, *exception*, and *signal* are defined in diverse ways in different programming environments.