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**Elektromagnetna združljivost (EMC) - 4-7. del: Preskusne in merilne tehnike – Splošno vodilo za harmonične in interharmonične meritve in merilno opremo za napajalne sisteme in nanje priključeno opremo (77A/562/CDV)**

Electromagnetic compatibility (EMC) - Part 4-7: Testing and measurement techniques - General guide on harmonics and interharmonics measurements and instrumentation, for power supply systems and equipment connected thereto (77A/562/CDV)

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**77A/562/CDV**

**COMMITTEE DRAFT FOR VOTE (CDV)  
PROJET DE COMITÉ POUR VOTE (CDV)**

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Also of interest to the following committees Intéresse également les comités suivants		Supersedes document Remplace le document <b>77A/527/CD, 77A/550/CC</b>	
Functions concerned Fonctions concernées			
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Titre : Amendement à la CEI 61000-4-7 : Compatibilité électromagnétique (CEM) – Techniques d'essai et de mesures – Guide général relatif aux mesures d'harmoniques et d'interharmoniques, ainsi qu'à l'appareillage de mesure, applicable aux réseaux d'alimentation et aux appareils qui y sont raccordés

Title : Amendment to IEC 61000-4-7 Ed.2: Electromagnetic compatibility (EMC) : Testing and measurement techniques - General guide on harmonics and interharmonics measurements and instrumentation, for power supply systems and equipment connected thereto

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Note d'introduction

Introductory note

The French version will be circulated later

**ATTENTION  
VOTE PARALLÈLE  
CEI – CENELEC**

L'attention des Comités nationaux de la CEI, membres du CENELEC, est attirée sur le fait que ce projet de comité pour vote (CDV) de Norme internationale est soumis au vote parallèle.

Un bulletin de vote séparé pour le vote CENELEC leur sera envoyé par le Secrétariat Central du CENELEC.

**ATTENTION  
IEC – CENELEC  
PARALLEL VOTING**

The attention of IEC National Committees, members of CENELEC, is drawn to the fact that this Committee Draft for Vote (CDV) for an International Standard is submitted for parallel voting.

A separate form for CENELEC voting will be sent to them by the CENELEC Central Secretariat.

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## 1 FOREWORD

2 This amendment has been prepared by subcommittee 77A: Low Frequency Phenomena,  
3 of IEC technical committee 77: Electromagnetic Compatibility.

4 The text of this amendment is based on the following documents:

FDIS	Report on voting
77A/XX/FDIS	//A/XX/RVD

5  
6 Full information on the voting for the approval of this amendment can be found in the  
7 report on voting indicated in the above table.

8 The committee has decided that the contents of this amendment and the base publication  
9 will remain unchanged until the maintenance result date<sup>1)</sup> indicated on the IEC web site  
10 under "http://webstore.iec.ch" in the data related to the specific publication. At this date,  
11 the publication will be

- 12 • reconfirmed,  
13 • withdrawn,  
14 • replaced by a revised edition, or  
15 • amended.

16

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1) The National Committees are requested to note that for this publication the maintenance result date is 2010

17 *Page 15 and 17*

18 *Replace 3.1, by*

19 Notations: The following notations are used in the present guide for the Fourier series  
20 development because it is easier to measure phase angles by observations of the zero  
21 crossings:

22

$$23 \quad f(t) = c_0 + \sum_{k=1}^{\infty} c_k \sin\left(\frac{k}{N} \omega_1 t + \varphi_k\right) \quad (1)$$

24 *In 3.1, replace equation system (2) by*

$$25 \quad \text{with: } \begin{cases} c_k = |b_k + ja_k| = \sqrt{a_k^2 + b_k^2} \\ Y_{C,k} = \frac{c_k}{\sqrt{2}} \\ \varphi_k = \pi + \arctan\left(\frac{a_k}{b_k}\right) \text{ if } b_k < 0 & \varphi_k = \arctan\left(\frac{a_k}{b_k}\right) \text{ if } b_k > 0 \\ \varphi_k = \frac{\pi}{2} \text{ if } b_k = 0 \text{ and } a_k > 0 & \varphi_k = -\frac{\pi}{2} \text{ if } b_k = 0 \text{ and } a_k < 0 \\ \varphi_k = 0 \text{ if } b_k < \varepsilon \text{ and } a_k \leq \varepsilon, \end{cases} \quad (2)$$

with  $\varepsilon = 0,05\% U_{\text{nom}}$  and  $\varepsilon = 0,15\% I_{\text{nom}}$   
or  $\varepsilon = 0,15\% U_{\text{nom}}$  and  $\varepsilon = 0,5\% I_{\text{nom}}$   
respectively, see Table 1 in 61000-4-7 Ed.2

26 *In 3.1, replace equation system (3) by*

$$27 \quad \text{and: } \begin{cases} b_k = \frac{2}{T_N} \int_0^{T_N} f(t) \times \sin\left(\frac{k}{N} \omega_1 t\right) dt \\ a_k = \frac{2}{T_N} \int_0^{T_N} f(t) \times \cos\left(\frac{k}{N} \omega_1 t\right) dt \\ c_0 = \frac{1}{T_N} \int_0^{T_N} f(t) dt \end{cases} \quad (3)$$

28

29 *and replace the list of symbols below equation (3) by:*

30  $\omega_1$  is the angular frequency of the fundamental ( $\omega_1 = 2\pi f_{H,1}$ );

31  $T_N$  is the width (or duration) of the time window; the time window is that time span of a  
32 time function over which the Fourier transform is performed;

33  $c_0$  is the d.c. component;

34  $c_k$  is the amplitude of the component with frequency  $f_{C,k} = \frac{k}{N} f_{H,1}$  ;

35  $Y_{C,k}$  r.m.s. value of  $c_k$ ;

36

37  $f_{H,1}$  is the fundamental frequency of the power system;

38  $k$  is the ordinal number (order of the spectral component) related to the frequency resolution

39  $\left(f_{C,1} = 1/T_N\right)$ .

40  $N$  is the number of fundamental periods within the window width;

41  $\varphi_k$  phase angle of spectral line  $k$

42

43 NOTE 1 - Strictly speaking these definitions apply to steady-state signals only. The Fourier series is actually  
44 in most cases performed digitally, i.e. as a Discrete Fourier Transform DFT, or a variant thereof, being the  
45 FFT.

46 The analogue signal  $f(t)$  which has to be analyzed is sampled, A/D-converted and stored. Each group of  $M$   
47 samples forms a time window on which DFT is performed. According to the principles of Fourier series  
48 expansion, the window width  $T_N$  determines the frequency resolution  $f_{C,1} = 1/T_N$  (i.e. the frequency separation  
49 of the spectral components) for the analysis. Therefore the window width  $T_N$  must be an integer multiple  $N$  of  
50 the fundamental period  $T_l$  of the system voltage:  $T_N = N \times T_l$ . The sampling rate is in this case  $f_s = M/(NT_l)$   
51 (where  $M$  = Number of samples within  $T_N$ ).

52 Before DFT-processing, the samples in the time window are often weighted by multiplying them with a special  
53 symmetrical function ('windowing function'). However, for periodic signals and synchronous sampling it is  
54 preferable to use a rectangular weighting window which multiplies each sample by unity.

55 The DFT-processor yields the orthogonal Fourier-coefficients  $a_k$  and  $b_k$  of the corresponding spectral-  
56 component frequencies  $f_{C,k} = k/T_N$ ,  $k = 0, 1, 2, \dots, M-1$ . However, only  $k$  values up to half of the maximum value  
57 are useful, the other half just duplicates them.

58 Under synchronized conditions, the component of harmonic order  $h$  related to the fundamental frequency  $f_{H,1}$  appears as the  
59 spectral component of order  $k$ , where  $k = hN$ .

60 NOTE 2 – The Fast Fourier Transform FFT is a special algorithm allowing short computation times. It requires  
61 that the number of samples  $M$  be an integer power of 2,  $M = 2^i$ , with  $i \geq 10$  for example

62 NOTE 3 – The symbol  $Y$  is replaced, as required by the symbol  $I$  for currents, by the symbol  $U$  for voltages.  
63 The index  $C$  qualifies the variable as spectral component

64

65 *Replace 3.2.1 by:*

66 **Harmonic frequency**

67  $f_{H,h}$

68 frequency which is an integer multiple of the fundamental frequency of the mains  
69 frequency ( $f_{H,h} = h \times f_{H,1}$ )

70

71 NOTE 1 The harmonic frequency  $f_{H,h}$  is identical with the frequency component  $f_{C,k}$  with  $k = h \times N$

72

73 *Replace 3.2.2 by:*

74 **Harmonic order**

75  **$h$**

76 (integer) ratio of a harmonic frequency to the fundamental frequency of the power  
77 system. In connection with the analysis using DFT and synchronisation between  $f_{H,1}$  and  
78  $f_s$  (sampling rate), the harmonic order  $h$  corresponds to the spectral component  $k = h \times N$   
79 ( $k$  = number of the spectral component,  $N$  = number of periods of the fundamental  
80 frequency in time  $T_N$ )

81 *Replace 3.2.3, by:*

82 **r.m.s. value of a harmonic component**

83  $Y_{H,h}$

84 r.m.s. value of one of the components having a harmonic frequency in the analysis of a  
85 non-sinusoidal waveform

86 For brevity, such a component may be referred to simply as a “harmonic”

87 NOTE 1 The harmonic component  $Y_{H,h}$  is identical with the spectral component  $Y_{C,k}$  with  $k = h \times N$  ;  
88 ( $Y_{H,h} = Y_{C,h \times N}$ ). The symbol  $Y$  is replaced, as required by the symbol  $I$  for currents, by the symbol  $U$  for  
89 voltages. The index  $H$  qualifies the variable  $I$  or  $U$  as harmonic.

90 NOTE 2 For the purposes of this standard, the time window has a width of  $N=10$  (50 Hz systems) or  $N=12$   
91 (60 Hz system) fundamental periods, i.e. approximately 200 ms (see 4.4.1). This yields  $Y_{H,h} = Y_{C,10 \times h}$  (50 Hz  
92 systems) and  $Y_{H,h} = Y_{C,12 \times h}$  (60 Hz systems).

93 *Page 19*

94 *Replace 3.2.4, by:*

95 **r.m.s. value of a harmonic group**

96  $Y_{g,h}$

97 square root of the sum of the squares of the r.m.s. value of a harmonic and the spectral  
98 components adjacent to it within the time window, thus summing the energy contents of  
99 the neighbouring components with that of the harmonic proper. See also equation 8 and  
100 Figure 4. The harmonic order is given by the harmonic considered.

101 NOTE 1 – The symbol  $Y$  is replaced, as required by the symbol  $I$  for currents, by the symbol  $U$  for voltages.

102 *Replace 3.2.5, by:*

103 **r.m.s. value of a harmonic subgroup**

104  $Y_{sg,h}$

105 square root of the sum of the squares of the r.m.s. value of a harmonic and the two  
106 spectral components immediately adjacent to it. For the purpose of including the effect of  
107 voltage fluctuation during voltage surveys, a subgroup of output components of the DFT  
108 is obtained by summing the energy contents of the frequency components directly  
109 adjacent to a harmonic with that of the harmonic proper. (See also equation 9 and  
110 Figure 6). The harmonic order is given by the harmonic considered.

111 NOTE 1 – The symbol  $Y$  is replaced, as required by the symbol  $I$  for currents, by the symbol  $U$  for voltages.

112 *Replace 3.3.1, by:*

113 **Total Harmonic Distortion**

114  $THD_Y$

115  $THD_Y$  (symbol)

116 ratio of the r.m.s. value of the sum of all the harmonic components ( $Y_{H,h}$ ) up to a specified  
117 order ( $h_{max}$ ) to the r.m.s. of the fundamental component ( $H_{H,1}$ ):

$$118 \quad THD_Y = \sqrt{\sum_{h=2}^{h_{max}} \left( \frac{Y_{H,h}}{Y_{H,1}} \right)^2} \quad (4)$$

119

120 NOTE 1 – The symbol  $Y$  is replaced, as required, by the symbol  $I$  for currents or by the symbol  $U$  for voltages.

121 NOTE 2 – The value of  $h_{max}$  is 40 if no other value is defined in a standard concerned with limits (IEC61000-3-series).

122 *Replace 3.3.2, by:*

123 **Group total harmonic distortion**

124 **THDG<sub>Y</sub>**

125 *THDG<sub>Y</sub>* (symbol)

126 ratio of the r.m.s. value of the harmonic groups ( $Y_{g,h}$ ) to the r.m.s. value of the group  
127 associated with the fundamental ( $Y_{g,1}$ ):

$$128 \quad THDG_Y = \sqrt{\sum_{h_{\min}}^{h_{\max}} \left( \frac{Y_{g,h}}{Y_{g,1}} \right)^2} \quad \text{Where } h_{\min} \geq 2 \quad (5)$$

129 NOTE 1 –The symbol  $Y$  is replaced, as required, by the symbol  $I$  for currents or by the symbol  $U$  for voltages.

130 NOTE 2 –The value of  $h_{\min}$  is 2 and that of  $h_{\max}$  is 40 if no other values are defined in a standard concerned with limits (e.g.  
131 61000-3-series)

132 *Page 21*

133 *Replace 3.3.3, by:*

134 **Sub-group total harmonic distortion**

135 **THDS<sub>Y</sub>**

136 *THDS<sub>Y</sub>*

137 ratio of the r.m.s. value of the harmonic sub-groups ( $Y_{sg,h}$ ) to the r.m.s. value of the sub-  
138 group associated with the fundamental ( $Y_{sg,1}$ ):

$$139 \quad THDS_Y = \sqrt{\sum_{h_{\min}}^{h_{\max}} \left( \frac{Y_{sg,h}}{Y_{sg,1}} \right)^2} \quad \text{Where } h_{\min} \geq 2 \quad (6)$$

140 NOTE 2 –The value of  $h_{\min}$  is 2 and that of  $h_{\max}$  is 40 if no other values are defined in a standard concerned with limits (e.g.  
141 61000-3-series)

142 SIST EN 61000-4-7:2003/A1:2009

<https://standards.iteh.ai/catalog/standards/sist/e5998255-4368-4de3-9adb-f3976e181b81/sist-en-61000-4-7-2003-a1-2009>

143 *Replace 3.3.4, by:*

144 **Partial Weighted Harmonic Distortion**

145 **PWHD<sub>H,Y</sub>**

146 *PWHD<sub>H,Y</sub>* (symbol)

147 ratio of the r.m.s. value, weighted with the harmonic order  $h$ , of a selected group of higher  
148 order harmonics (from the order  $h_{\min}$  to  $h_{\max}$ ) to the r.m.s. value of the fundamental:

$$149 \quad PWHD_{H,Y} = \sqrt{\sum_{h=h_{\min}}^{h_{\max}} h \left( \frac{Y_{H,h}}{Y_{H,1}} \right)^2} \quad (7)$$

150 NOTE 1 The concept of partial weighted harmonic distortion is introduced to allow for the possibility of  
151 specifying a single limit for the aggregation of higher order harmonic components. The partial weighted group  
152 harmonic distortion,  $PWHD_{g,Y}$ , can be evaluated by replacing the quantity  $Y_{H,h}$  by the quantity  $Y_{g,h}$ . The partial  
153 weighted sub-group harmonic distortion  $PWHD_{sg,Y}$  can be evaluated by replacing the quantity  $Y_{H,h}$  by the  
154 quantity  $Y_{sg,h}$ . The type of  $PWHD$  ( $PWHD_{H,Y}$ ,  $PWHD_{g,Y}$  or  $PWHD_{sg,Y}$ ) is defined in each standard which uses the  $PWHD$ , e.g.  
155 in standards concerned with limits (IEC 61000-3-series).

156 NOTE 2 The values of  $h_{\min}$  and  $h_{\max}$  are defined in each standard which uses the  $PWHD_Y$ , e.g. in standard  
157 concerned with limits (IEC 61000-3-series).



158 *Replace 3.4.1, by:*

159 **R.M.S. value of a spectral component**

160  $Y_{C,k}$

161 In the analysis of a waveform, the r.m.s. value of a component whose frequency is a multiple of the  
162 reciprocal of the duration of the time window.

163 NOTE 1 – If the duration of the time window is multiple of the fundamental frequency, only some of the spectral components  
164 have frequencies which are integer multiples of the fundamental frequency.

165 NOTE 2 – The frequency interval between two consecutive spectral components is the reciprocal of the width  
166 of the time window, approximately 5 Hz for the purposes of this standard.

167 NOTE 3 – The symbol  $Y$  is replaced, as required, by the symbol  $I$  for currents or by the symbol  $U$  for voltages.

168 *Replace 3.4.2, by:*

169 **R.M.S. value of an interharmonic component**

170  $Y_{C,h}$

171 r.m.s. value of a spectral component,  $Y_{C,k \neq h \times N}$ , with a frequency between two consecutive harmonic  
172 frequencies (see Figure 4). For brevity, such a component may be referred to simply as an  
173 “interharmonic”.

174 NOTE 1 – The frequency of the interharmonic component is given by the frequency of the spectral line. This frequency is not  
175 an integer multiple of the fundamental frequency.

176 NOTE 2 – A difference is made between an “interharmonic component”  $Y_{C,k}$  for  $k \neq h \times N$  produced as a physical component  
177 by an equipment e.g. at 183,333 Hz, and a “spectral component”  $Y_{C,k}$  for  $k=1,2,3\dots$  as the result of the waveform analysis e.g.  
178 for a 50Hz system at 185 Hz for  $k = 37 \neq h \times N$ . A “spectral component” is a “harmonic component” for  $k = h \times N$ .

179

180 *Page 23*

181 *Replace 3.4.3, by:*

182 **R.M.S. value of an interharmonic group**

183  $Y_{ig,h}$

184 r.m.s. value of all spectral components in the interval between two consecutive harmonic  
185 frequencies (see Figure 4).

186 NOTE – For the purpose of this standard, the r.m.s. value of the interharmonic group between the harmonic  
187 orders  $h$  and  $h+1$  is designated as ' $Y_{ig,h}$ ', e.g. the group between  $h=5$  and  $h=6$  is designated as  $Y_{ig,5}$ .

188

189 *Replace 3.4.4, by:*

190 **R.M.S. value of an interharmonic centred subgroup**

191  $Y_{isg,h}$

192 The r.m.s. value of all spectral components in the interval between two consecutive  
193 harmonic frequencies, excluding frequency components directly adjacent to the harmonic  
194 frequencies (see Figure 6).

195 NOTE – For the purpose of this standard, the r.m.s. value of the centred subgroup between the harmonic  
196 orders  $h$  and  $h+1$  is designated as ' $Y_{isg,h}$ ', e.g. the group between  $h=5$  and  $h=6$  is designated as  $Y_{isg,5}$ .

197 *Replace 3.4.5, by:*

198 **Interharmonic group frequency**

199  $f_{ig,h}$

200 The interharmonic group frequency is the mean of the two harmonic frequencies between  
201 which the group is situated, i.e.  $f_{ig,h} = (f_h + f_{h+1})/2$ .

202 *Add 3.4.6, by:*

### 203 Interharmonic centred subgroup frequency ( $f_{\text{isg},h}$ )

204 The interharmonic centred subgroup frequency is the mean of the two harmonic  
205 frequencies between which the subgroup is situated, i.e.  $f_{\text{isg},h} = (f_h + f_{h+1})/2$ .

206 *Pages 23 and 24*

207 *Replace clauses 3.5.1 and 3.5.2 by:*

### 208 3.5.1 Symbols and Abbreviations

209 In this standard, voltage and current values are r.m.s. unless otherwise stated.

210	$a$	amplitude coefficient of a cosine component in a Fourier series
211	$b$	amplitude coefficient of a sine component in a Fourier series
212	$c$	amplitude coefficient in a Fourier series
213	$f$	frequency; function
214	$f_{C,k}$	Spectral line frequency of order $k$
215	$f_{C,1}$	the frequency of the spectral line of order 1. The frequency resolution is equal to this
216		frequency
217	$f_{g,h}$	harmonic-group frequency of order $h$
218	$f_{\text{sg},h}$	harmonic-subgroup frequency of order $h$
219	$f_{\text{ig},h}$	Interharmonic-group frequency of order $h$
220	$f_{\text{isg},h}$	Interharmonic-subgroup frequency of order $h$
221	$f_{H,h}$	harmonic component frequency of order $h$
222	$f_{H,1}$	fundamental frequency of the power system
223	$f_s$	sampling rate
224	$h_{\text{max}}$	the order of the highest harmonic that is taken into account
225	$h_{\text{min}}$	the order of the lowest harmonic that is taken into account
226	$j$	$\sqrt{-1}$
227	$t$	running time
228	$B$	bandwidth
229	$Y_{C,k}$	r.m.s. value of the spectral component of order $k$
230	$Y_{g,h}$	r.m.s. value of harmonic group
231	$Y_{\text{ig},h}$	r.m.s. value of interharmonic group
232	$Y_{\text{isg},h}$	r.m.s. value of interharmonic subgroup
233	$Y_{\text{sg},h}$	r.m.s. value of harmonic subgroup
234	$H$	harmonic
235	$I$	current (r.m.s. value)
236	$M$	integer number; number of samples within the window width
237	$N$	number of power supply periods within the window width
238	$P$	power
239	$T$	time interval
240	$T_1$	fundamental period of the power supply system
241	$T_N$	window width comprising $N$ fundamental periods
242	$U$	voltage (r.m.s. value)
243	$Y$	Variable replaceable by $I$ , $U$ .
244	$\omega$	angular frequency
245	$\omega_1$	angular frequency of the power supply
246	$\varphi$	phase angle