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**Information technology — Security  
techniques — Digital signatures with  
appendix —**

**Part 2:  
Identity-based mechanisms**

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*Technologies de l'information — Techniques de sécurité — Signatures  
digitales avec appendice*

*Partie 2: Mécanismes basés sur des identités*

ISO/IEC 14888-2:1999

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## Foreword

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work.

In the field of information technology, ISO and IEC have established a joint technical committee, ISO/IEC JTC 1. Draft International Standards adopted by the joint technical committee are circulated to national bodies for voting. Publication as an International Standard requires approval by at least 75 % of the national bodies casting a vote.

International Standard ISO/IEC 14888-2 was prepared by Joint Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 27, *IT Security techniques*.

ISO/IEC 14888 consists of the following parts, under the general title *Information technology — Security techniques — Digital signatures with appendix*:

- *Part 1: General*
- *Part 2: Identity-based mechanisms*
- *Part 3: Certificate-based mechanisms*

Further parts may follow.

Annexes A and B of this part of ISO/IEC 14888 are for information only.

# Information technology — Security techniques — Digital signatures with appendix —

## Part 2: Identity-based mechanisms

### 1 Scope

ISO/IEC 14888 specifies a variety of digital signature mechanisms with appendix for messages of arbitrary length and is applicable in schemes providing entity authentication, data origin authentication, non-repudiation, and integrity of data.

This part of ISO/IEC 14888 specifies the general structure and the fundamental procedures which constitute the signature and verification processes of an identity-based digital signature mechanism with appendix for messages of arbitrary length.

### 2 Normative references

The following standards contain provisions which, through reference in this text, constitute provisions of this part of ISO/IEC 14888. At the time of publication, the editions indicated were valid. All standards are subject to revision, and parties to agreements based on this part of ISO/IEC 14888 are encouraged to investigate the possibility of applying the most recent editions of the standards indicated below. Members of IEC and ISO maintain registers of currently valid International Standards.

ISO/IEC 9796: 1991, *Information technology - Security techniques - Digital signature scheme giving message recovery*.

ISO/IEC 14888-1: 1998, *Information technology - Security techniques - Digital signatures with appendix - Part 1: General*.

### 3 General

The verification of a digital signature requires the signing entity's verification key. It is therefore essential for a verifier to be able to associate the correct verification key with the signing entity, or more precisely, with (parts of) the signing entity's identification data. If this association is somehow inherent in the verification key itself, the digital signature scheme is said to be "identity-based."

The key generation process of the identity-based mechanism defined in this part of ISO/IEC 14888

involves a trusted third party. The trusted third party has a secret parameter, the key generation exponent, which it uses to derive the signature keys of other entities. The secrecy of the signature keys depends unconditionally on the secrecy of the key generation exponent.

In the verification of an identity-based signature, two parameters are needed. The first one, the domain verification exponent, is common to all entities, while the second one, the signing entity's verification key, is specific to each entity. In the identity-based mechanism defined in this part of ISO/IEC 14888, an entity's verification key is derived directly from the entity's identification data, using a public function.

The identity-based signature mechanism with appendix is an example of a randomized mechanism, as described in ISO/IEC 14888-1. The descriptions of the signature and verification processes follow the general procedures specified in Clause 10 of ISO/IEC 14888-1. In particular, this part makes use of the general requirements, definitions and symbols given in ISO/IEC 14888-1.

The identity-based digital signature mechanism with appendix is defined by the specification of the following processes:

- key generation process;
- signature process; and
- verification process.

### 4 Definitions

For the purposes of this part of ISO/IEC 14888, the following definitions apply.

#### 4.1

##### domain modulus

a domain parameter, which is a positive integer resulting from the product of two distinct primes which are known only to the trusted third party

#### 4.2

##### domain verification exponent

a domain parameter which is a positive integer

**4.3****key generation exponent**

a positive integer known only to the trusted third party

**4.4****public key derivation function**

a domain parameter, whose function is to map strings of bits into positive integers

NOTE 1 This function is used to transform an entity's identification data into the entity's verification key, and satisfies the following two properties.

- It is computationally infeasible to find any two distinct inputs which map to the same output.
- Either the probability that a randomly chosen value  $Y$  is in the range of the function is negligibly small, or for a given output it is computationally infeasible to find for a given output an input which maps to this output.

NOTE 2 Negligibility and computational infeasibility depend on the specific security requirements and environment.

**4.5****trusted third party**

A security authority, or its agent, trusted by other entities with respect to security related activities

**5 Notation****5.1 Symbols**

In addition to the symbols defined in ISO/IEC 14888-1, the following symbols are used.

$D$	Key generation exponent
$I$	Identification data
$N$	Domain modulus
$P, Q$	Prime numbers
$V$	Domain verification exponent
$\gamma$	Public key derivation function
$\text{lcm}(A, B)$	The least positive integer such that $C \bmod A = 0$ and $C \bmod B = 0$

**6 Key production process**

The key production process of this identity-based signature mechanism is an application of the signature scheme specified in Annex A of ISO/IEC 9796-1. It consists of the following three procedures:

- generating domain parameters; and
- generating signature key.

An entity shall be chosen to act as a trusted third party. Using its own secrets, the trusted third party

generates the private signature key for each entity as a function of that entity's identification data.

In some instances the validation of domain parameters and keys, may be required. However, it is outside the scope of this part of ISO/IEC 14888.

**6.1 Generating domain parameters**

This procedure is executed once when the domain is set up.

The trusted third party produces the domain verification exponent  $V$  and the domain modulus  $N$ . The domain verification exponent shall be chosen to be an odd integer. The domain modulus shall be the product of two large prime integers  $P$  and  $Q$  such that  $P - 1$  and  $Q - 1$  are coprime to  $V$ . Furthermore, the trusted third party determines the key generation exponent, which is the least positive integer  $D$  such that  $DV - 1$  is a multiple of  $\text{lcm}(P - 1, Q - 1)$ .

Specifically,  $D$  shall be such that:

$$U^{DV} \bmod N = U$$

for all integers  $U$ ,  $0 < U < N$ .

The public domain parameters are  $N$  and  $V$ . The trusted third party keeps  $D$  for its own use. It shall be computationally infeasible for other entities to compute  $D$  from  $N$  and  $V$ .

NOTE — The values of  $N$  and  $V$  shall be chosen large enough to satisfy the specific domain security requirements. The length of  $N$  varies typically between 1024 bits and 2048 bits while the length of  $V$  is recommended to be at least 80 bits.

Let  $T$ ,  $T'$  and  $L$  be integers such that  $T - T' = LV$ . Let  $X$  be a signature key and  $Y$  be the corresponding verification key as defined in 6.2. Then  $X^{T'} \equiv X^T \cdot Y^L \bmod N$ .

Given a signature  $(R, S)$  corresponding to assignment  $T$ , one can then produce the signature  $(R, S')$  corresponding to assignment  $T'$  by computing  $S' = S \cdot Y^L \bmod N$  (See 7.4). Therefore,  $V$  must be chosen sufficiently large so that given  $T$ , the probability that a randomly chosen  $T'$  satisfies  $T - T' \equiv 0 \bmod V$  is sufficiently small.

The set of the domain parameters of an identity-based signature mechanism with appendix also includes a public key derivation function  $\gamma$ , which is used to transform a signing entity's identification data into a positive integer less than  $N$ .

**6.2 Producing the verification key and generating the signature key**

Each user entity has unique identification data. To generate a private signature key for an entity with identification data  $I$ , the trusted third party first

computes the verification key  $Y$  from the public key derivation function  $y$  and the identification data  $I$ .

$$Y = y(I).$$

NOTE — The probability that  $Y$  is equal to zero or an integer multiple of  $P$  or  $Q$  is negligible, provided that  $P$  and  $Q$  are sufficiently large.

The trusted authority computes the private signature key  $X$  as

$$X \equiv Y^{-D} \bmod N.$$

As a result of the key generation process, the entity with identification data  $I$  has a signature key  $X$  which satisfies the equation,

$$X^V \cdot y(I) \bmod N \equiv 1.$$

In an identity-based signature mechanism, the verifier obtains the knowledge of the signing entity's verification key from the signing entity's identification data by computing  $Y = y(I)$ . Once the verification has been computed, it can be cached for further use.

## 7 Signature process

In this clause, the signature process of an identity-based signature mechanism is described. The mechanism is randomized and follows the general model for randomized signature mechanisms described in ISO/IEC 14888-1. The signature process consists of the following procedures:

- producing pre-signature;
- preparing message;
- computing witness; and
- computing signature.

In this process the signer makes use of its signature key  $X$  and the public domain parameters  $N$  and  $V$ .

The result of this process is the signature  $\Sigma$  which has two parts,  $R$  and  $S$ . The signing entity optionally forms a text field, containing the entity's identification data. The signature and the optional text field form the appendix, which is appended to the message by the signer.

### 7.1 Producing pre-signature

The pre-signature procedure of an identity-based signature mechanism consists of two steps:

- producing randomizer  $K$ ; and
- computing pre-signature  $\Pi$ .

#### 7.1.1 Producing randomizer

The signing entity generates a randomizer, which is an integer,  $K$  with  $0 < K < N$ . Depending on the mechanism, there may be additional constraints on

this generation procedure. The output of this step is  $K$ , which the signing entity keeps secret.

#### 7.1.2 Computing pre-signature

The input to this step is the randomizer  $K$ . The output is the pre-signature  $\Pi$  computed as:

$$\Pi = K^V \bmod N.$$

### 7.2 Preparing message

Two data fields,  $M_1$  and  $M_2$  are derived from the message  $M$  as described in 8.2 of ISO/IEC 14888-1.

The process of preparing the message shall satisfy one of the following two conditions:

- the entire message shall be reconstructible given  $M_1$  and  $M_2$ ; or
- it shall be computationally infeasible to find two distinct messages  $M$  and  $M'$  such that the derived pairs  $(M_1, M_2)$  and  $(M'_1, M'_2)$  are equal.

Typically, in the first case,  $M_1 = M$  (when  $M_2$  is empty), or  $M_2 = M$  (when  $M_1$  is empty), or  $M_1 = M_2 = M$ . In the second case, either  $M_1$  or  $M_2$  or both are hash tokens of  $M$ .

### 7.3 Computing witness

The deterministic witness is computed as a hash-token  $H$  of  $M_1$  using a collision-resistant hash-function (see Figure 1).

The randomized witness  $R$  is defined as the concatenation of an optional field, which can be used to identify the hash-function and padding method and is computed using a collision-resistant hash-function.  $R$  depends on the pre-signature  $\Pi$  and optionally, on  $M_1$ , if  $M_1$  is not empty (see figure 2).

NOTE — The hash-function identifier shall be included in the hash-token unless the hash-function is uniquely determined by the signature mechanism or by the domain parameters.

### 7.4 Computing signature

The computation of a signature in an identity-based signature mechanism consists of the following steps:

- computing the first part of the signature;
- computing assignment; and
- computing the second part of the signature.

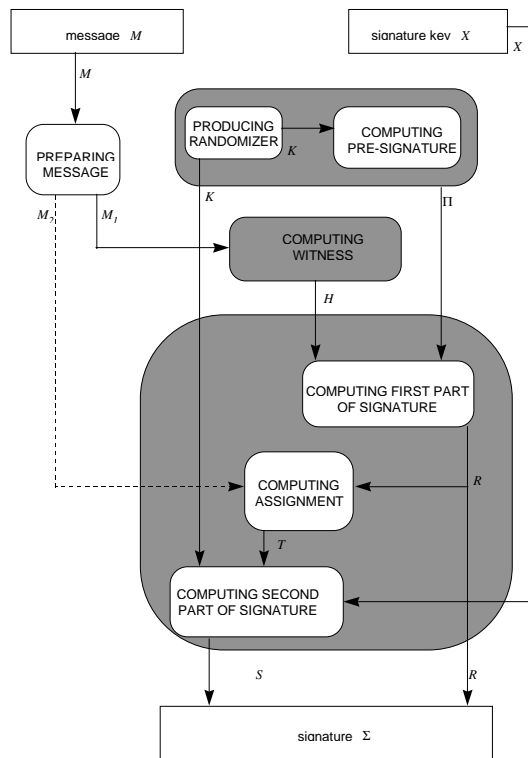


Figure 1 — Signature process with a deterministic witness

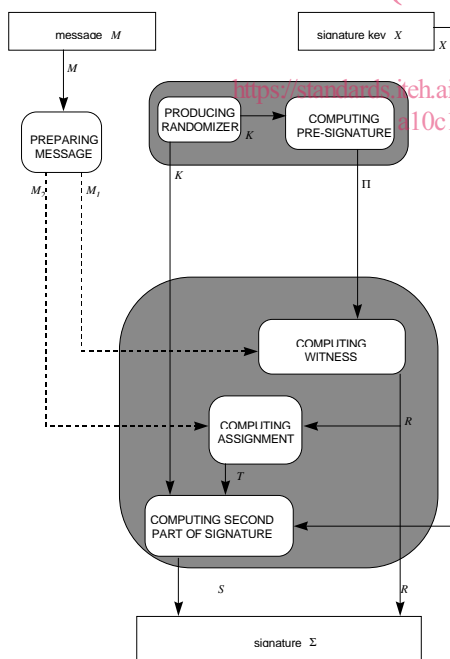


Figure 2 — Signature process with a randomized witness

#### 7.4.1 Computing the first part of the signature

If the witness is deterministic, the first part  $R$  of the signature is computed as a function of  $H$  and  $\Pi$ . This function is invertible in the following way.

- Given  $\Pi$  and  $R$ , the hash-token  $H$  can be recovered (see Figure 1).

If the witness is randomized, it is the first part of the signature  $R$  and no further computation is needed (see Figure 2).

NOTE — The domain parameters must include an agreed upon method for converting a string of bits to a positive integer, in order that this step can be carried out.

#### 7.4.2 Computing assignment

The assignment  $T$  is a positive integer and computed as a function of the first part of the signature. The assignment also depends on the second part  $M_2$  of the message, if  $M_2$  is not empty.

It is required that the method of computing the pair  $(R, T)$  satisfies the following condition.

It is computationally infeasible to find any two pairs  $(M, \Pi)$  and  $(M', \Pi')$  with the same resulting pair  $(R, T)$ .

#### 7.4.3 Computing the second part of the signature

The signature function of the identity-based signature mechanism has the following form,

$$S = K \cdot X^T \bmod N,$$

where  $K$  is the randomizer computed in 7.1.1,  $T$  is the assignment computed at 7.4.2,  $X$  is the signature key, and  $N$  is the domain modulus. The output of the signature function is the second part  $S$  of the signature.

## 8 Verification process

The verification process consists of the following procedures:

- preparing message;
- retrieving witness;
- computing verification function; and
- verifying witness.

At the beginning of the verification process the verifier must have the values of the following data items available:

- domain parameters  $N$  and  $V$ ;
- the signer's verification key  $Y$ ;
- message  $M$ ;
- signature  $\Sigma = (R, S)$ ; and
- optional text (from appendix).

A successful verification of a signature implies that the signature was created using a signature key  $X$  which corresponds to the verification key  $Y$ .

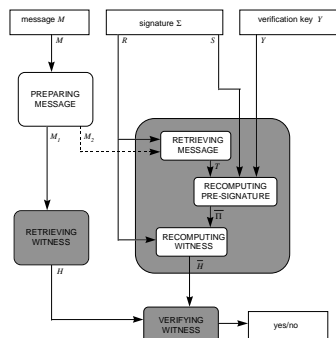


## 8.1 Preparing message

This procedure is identical to 7.2.

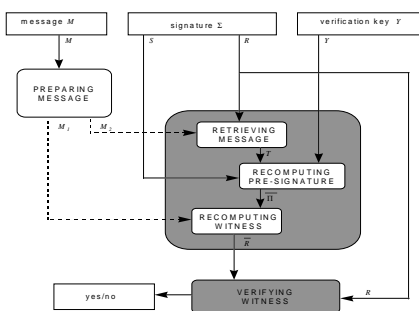
## 8.2 Retrieving witness

If the witness is deterministic, then this procedure is described in 7.3. The verification process is depicted in Figure 3.



**Figure 3 — Verification process with a deterministic witness**

If the witness is randomized, the verification process is as depicted in Figure 4. The retrieved witness is the first part  $R$  of the signature.



**Figure 4 — Verification process with a randomized witness**

## 8.3 Computing verification function

The computation of the verification function of an identity-based signature mechanism consists of the following steps:

- retrieving assignment;
- recomputing pre-signature; and
- recomputing witness.

### 8.3.1 Retrieving assignment

This step is identical to 7.4.2. The verifier computes the assignment  $T$  as a function of the value  $R$  retrieved in 8.2 and the part  $M_2$  of the message if  $M_2$  is not empty. The assignment is a positive integer.

### 8.3.2 Recomputing pre-signature

The verifier produces a recomputed value  $\bar{\Pi}$  of the pre-signature by using the formula,

$$\bar{\Pi} = Y^T \cdot S^V \bmod N$$

where  $Y$  is the verification key,  $N$  is the domain modulus,  $V$  is the domain verification exponent,  $T$  is the assignment retrieved at 8.3.1 and  $S$  is the second part of the signature.

### 8.3.3 Recomputing witness

If the witness is deterministic, it is the hash-token  $H$  of  $M_1$ . The verifier produces a recomputed value  $\bar{H}$  by recovering it from using  $R$  and  $\bar{\Pi}$ .

If the witness is randomized, the computation is identical to 7.3, where the inputs are the recomputed value  $\bar{\Pi}$  of  $\Pi$  and  $M_1$  of  $M$ . The output is the recomputed witness  $\bar{R}$ .

## 8.4 Verifying witness

At this step the retrieved value of the witness from 8.2 and the recomputed value of the witness from 8.3.3 are compared. The verification is successful if these two witness values are equal.

## 9 Guillou-Quisquater signature mechanism

The key production process, signature process and verification process of the identity-based digital signature scheme of Guillou and Quisquater are described in Clauses 6 to 8 of this part of ISO/IEC 14888 and depicted in Figures 2 and 4.

The following procedures and functions remain to be specified in more detail.

- public key derivation function;
- preparing message;
- computing witness;
- computing the first part of the signature; and
- computing assignment.

## 9.1 Public key derivation function

The public key derivation function is the redundancy generating function described in ISO/IEC 9796-1. The signing entity's identification data  $I$ , or its hash-token, is taken as the input message to the process described in 5.1 to 5.4 of ISO/IEC 9796-1. The public key  $Y = y(I)$  of the entity is set to be the output of this process, which is called the intermediate integer in ISO/IEC 9796-1.

## 9.2 Preparing message

In the Guillou-Quisquater mechanism  $M_1 = M$  and  $M_2$  is empty.

## 9.3 Computing witness

The witness  $R$  in the Guillou-Quisquater mechanism is computed as a hash-token of the data  $\Pi \parallel M$ , where  $\Pi$  is the pre-signature.

$$R = H(\Pi \parallel M).$$

## 9.4 Computing the first part of the signature

In the Guillou-Quisquater mechanism, the witness  $R$  forms the first part of the signature.

## 9.5 Computing assignment

The assignment  $T$  is equal to  $R$  represented as a positive integer.

NOTE — The domain parameters must include an agreed upon method for converting a string of bits to a positive integer in order that this step can be carried out.

## 10 Identity-based signatures with short assignment

In this clause a variant of the Guillou-Quisquater scheme is specified, which is suitable for implementation in devices with slow processors or slow input/output interface. Additional hashing is used to reduce the length of the intermediate parameters. Up to three different hash-functions can be used in the computation of the witness and the assignment. They need not be collision-resistant, but they have to be chosen in such a way that it is infeasible to find two distinct messages with the same pair  $(R, T)$ .

This mechanism differs from the Guillou-Quisquater scheme in the following procedures:

- preparing message;
- computing witness;

- computing the first part of the signature;
- computing the first part of the signature; and
- computing assignment.

### 10.1 Preparing message

In this variant, the two parts  $M_1$  and  $M_2$  of the message input are set to equal the hash-token  $H$  of the message  $M$ .

### 10.2 Computing witness

The witness  $R$  is computed by forming the hash-token  $H_2$  of the data  $H_1 \parallel H$ , where  $H$  is computed in 10.1 and is the hash-token of the pre-signature  $\Pi$ .

NOTE — The pre-computed hash-token  $H_1$  can be stored more efficiently.

### 10.3 Computing assignment

The assignment  $T$  is obtained by computing the hash-token  $H_3$  of the data  $H \parallel R$ .

## 11 Identity-based signatures giving recovery of the hash-code of message

This variant of the Guillou-Quisquater scheme has the advantage that the hash-function can be computed in parallel to the rest of the verification steps. The signature process of this identity-based digital signature mechanism is depicted in Figure 1 and the verification process in Figure 3. The witness is deterministic. This mechanism differs from the Guillou-Quisquater scheme in the following procedures:

- computing witness; and
- computing the first part of the signature.

Also, it is assumed that the randomizer  $K$  produced by the signer satisfies  $K \neq 0 \bmod P$  and  $K \neq 0 \bmod Q$ , since otherwise the factorization of  $N$  is found. Hence it can also be assumed that the pre-signature  $\Pi$  is not a multiple of either  $P$  or  $Q$ .

### 11.1 Computing witness

The witness is computed as the hash-token  $H$  of the message  $M$  using a collision-resistant hash-function.



## 11.2 Computing the first part of the signature

The first part  $R$  of the signature is computed as;

$$R = \Pi \cdot H \bmod N.$$

Given a recomputed value  $\overline{\Pi}$  of the pre-signature, the verifier obtains a recomputed value  $\overline{H}$  of the witness by computing:

$$\overline{H} = \overline{\Pi}^{-1} R \bmod N.$$

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## Annex A (informative)

### Numerical examples

The numbers are given in hexadecimal notation.

#### A.1 Numerical example of the key production process

##### A.1.1 Generating domain parameters

The domain modulus  $N$  is the product of two distinct primes  $P$  and  $Q$ . This example uses 512-bit prime numbers as  $P$  and  $Q$ , so  $N$  is a 1024 bit number.

$P =$	FFFFFFFF	EA2DE66E	D3B1B7E9	61B75DFC	D9FAE2FF
	A07A2345	9B7956FB	1B9B16D7	E1B6D59B	BDF45B85
	3CBF08EA	3BC7A1BD	541CB3A8	80E02E43	87CA7DEF
	50948E87				

$Q =$	FFFFFFFF	E275B7F4	98A3811D	E906ACF7	BFEB5CD6
	A445AF09	D7906DE1	97CC2CCD	87614718	8C7C084F
	CE9231CA	B7CFA113	13C3DDCF	F1B70A54	84494467
	8FCEF193				

$N = PQ =$

FFFFFFFF	CCA39E63	6ED9CF52	950C23A0	38AE0291
012B984A	964FFBBD	99E9DACB	91400431	0C5DD264
B1873126	44A725C5	D5BC73F4	97CFD100	89FD1342
656026BE	3FB583FE	B134FF43	6957A1E1	D975B5BE
DF1A9570	4C81A337	F06E5F9F	9388A7AC	5ABFD5CF
0356D91A	9861C69F	E50509C2	323E5270	F2015FBD
C08AA2C0	391CEE85			

The domain verification exponent is an odd integer coprime to  $P-1$  and  $Q-1$ . In this example,  $V$  is  $2^{79}+1$ , so the length of  $V$  is 80 bits.

$V =$     8000    00000000    00000001

The key generation exponent  $D$  is the positive integer such that  $DV - 1$  is a multiple of  $\text{lcm}(P-1, Q-1)$ .

$\text{lcm}(P-1, Q-1) =$

7FFFFFFFFF	E651CF31	B76CE7A9	4A8611D0	1C570148
8095CC25	4B27FDDE	CCF4ED65	C8A00218	862EE932
58C39893	225392E2	EAD39FA	4BE7E880	44FE89A1
32B0135E	1FDAC1FF	7248B06F	FE81346D	475BD565
229A2ACD	03E0E874	3EB24D61	7010B203	78D3DC8D
5C733AA2	C68845F5	78B6E378	E52EE07C	3FB51392
DA3B7034	AC5CB736			

$D =$	1BC6C0ED	36435CBF	A89C7A35	50CE3D54	C6ABC9F5
	EE5E75C9	E458AADA	6178CB20	C7339C4E	F30413A6
	586DA8B6	45A72BDF	291C9218	F0CA83EF	A4234FAD
	8394B2BF	8F4A0EF9	61E098FC	2CC5AFAA	46CCC821
	0427D3EE	3461AF0B	46895311	E1DAD21F	35217CBC
	4FD1A5B9	62E01B8B	967F97E2	41ECF56E	DBF85278
	EC058601	17D9A7B7			

### A.1.2 Producing verification key and signature key

The verification key  $Y$  is the output of the public key derivation function  $y$  with the identification data  $I$  as an input, and neither a multiple of  $P$  nor  $Q$ . This example uses a 1024-bit number  $Y$  less than  $N$ .

$Y =$	C50ECCC9	64443B0A	1C974F40	1C94E500	FA8214FC
	9B1B5EC5	2AA1201A	001EA099	FE90D01D	F32C6B43
	323F0812	42ABE843	09F926BB	9338A841	5DEF2EF6
	E709E3BD	515B5D86	C3ED4B7F	C15FA876	26E8E9C7
	0E557D5B	A8E96D7C	B55FBF41	37F601FF	47B7CCCB
	6BED4407	6F8E9805	42E37105	522E7184	42A717DF
	E89A6B62	7B6E60B7			

The Trusted authority computes the private signature key  $X$  as:

$$X = Y^{-D} \bmod N =$$

A763FA4	3895CFDD	D80627A6	A8271250	97C184E5
10F0075C	48FCB0E7	F2885275	AAA32829	C08CF352
0F42F6FD	C296DCE1	F50FBDED	D5C33C7C	63298C4F
26C2CDEE	11D927BA	C6EC4A6A	C022C063	1F30E880
07452397	7F3ACA8C	422E2461	3B7F3BB0	E61D04B8
0670A128	0ED7C8C1	A72D4B1C	C566381B	0665F83B
70FD7158	0B7A6EEC			

## A.2 Numerical example of a Guillou-Quisquater signature mechanism, described in clause 9

In this example, the hash-function in use is fixed and known to all entities of a domain and hence the hash identifiers are not required. The hash-token is produced by using SHA-1.

The domain parameters, the private signature key and the verification key are the same as A.1.

### A.2.1 Signature process

#### A.2.1.1 Producing pre-signature

The signing entity generates a randomizer, which is a random or pseudo-random integer  $K$  with  $0 < K < N$ . This example uses a 1024-bit randomizer  $K$ .

$K =$	B2045A19	83150F5B	B04CB524	2B566A37	6779F416
	5C7F1673	029C1BFC	05A84C60	E401897A	CEAD9DE5
	C7D8108B	95943332	FF6B20D3	004CCD40	36BDBB7E
	10DA755E	B03720F0	5A0CDC53	66EB4374	BE091A80
	6D339190	D2ADE1CD	9E11EF4E	A5FF6969	3D0EB942
	BFCC333D	F5FDD599	1D3B78A7	4868B0C6	381AEA61
	C24F3E05	2D8D9FFA			

The pre-signature  $\Pi$  is computed as:

$$\Pi = K^V \bmod N =$$

15B35BB7	0DDD7ED8	0FAD7EDE	A80F828E	46B3F86D
4EFB7E84	58562B6D	6F1885D0	A02FD892	8838C128
B53EE703	FAC96534	6C18A714	17D12FD7	211C3956
B6AD1A15	F4399EB0	CC065E8F	CC0039F3	E13A8EFE
5FB384CC	D0190FA9	DC995DEC	BB07947F	72124D7B
9044433C	7A416B62	99297387	0174FB6A	94A8FA8B
1CBD7E0A	2780DFD8			