
**Geographic information — Spatial
schema**

Information géographique — Schéma spatial

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Tel. + 41 22 749 01 11
Fax + 41 22 749 09 47
E-mail copyright@iso.org
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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

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Introduction

This International Standard provides conceptual schemas for describing and manipulating the spatial characteristics of geographic features. Standardization in this area will be the cornerstone for other geographic information standards.

A feature is an abstraction of a real world phenomenon; it is a geographic feature if it is associated with a location relative to the Earth. Vector data consists of geometric and topological primitives used, separately or in combination, to construct objects that express the spatial characteristics of geographic features. Raster data is based on the division of the extent covered into small units according to a tessellation of the space and the assignment to each unit of an attribute value. This International Standard deals only with vector data.

In the model defined in this International Standard, spatial characteristics are described by one or more spatial attributes whose value is given by a geometric object (GM_Object) or a topological object (TP_Object). Geometry provides the means for the quantitative description, by means of coordinates and mathematical functions, of the spatial characteristics of features, including dimension, position, size, shape, and orientation. The mathematical functions used for describing the geometry of an object depend on the type of coordinate reference system used to define the spatial position. Geometry is the only aspect of geographic information that changes when the information is transformed from one geodetic reference system or coordinate system to another.

Topology deals with the characteristics of geometric figures that remain invariant if the space is deformed elastically and continuously — for example, when geographic data is transformed from one coordinate system to another. Within the context of geographic information, topology is commonly used to describe the connectivity of an n -dimensional graph, a property that is invariant under continuous transformation of the graph. Computational topology provides information about the connectivity of geometric primitives that can be derived from the underlying geometry.

Spatial operators are functions and procedures that use, query, create, modify, or delete spatial objects. This International Standard defines the taxonomy of these operators in order to create a standard for their definition and implementation. The goals are to:

- a) Define spatial operators unambiguously, so that diverse implementations can be assured to yield comparable results within known limitations of accuracy and resolution.
- b) Use these definitions to define a set of standard operations that will form the basis of compliant systems, and, thus act as a test-bed for implementers and a benchmark set for validation of compliance.
- c) Define an operator algebra that will allow combinations of the base operators to be used predictably in the query and manipulation of geographic data.

Standardized conceptual schemas for spatial characteristics will increase the ability to share geographic information among applications. These schemas will be used by geographic information system and software developers and users of geographic information to provide consistently understandable spatial data structures.

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Geographic information — Spatial schema

1 Scope

This International Standard specifies conceptual schemas for describing the spatial characteristics of geographic features, and a set of spatial operations consistent with these schemas. It treats vector geometry and topology up to three dimensions. It defines standard spatial operations for use in access, query, management, processing, and data exchange of geographic information for spatial (geometric and topological) objects of up to three topological dimensions embedded in coordinate spaces of up to three axes.

2 Conformance

2.1 Overview

Clauses 6 and 7 of this International Standard use the Unified Modeling Language (UML) to present conceptual schemas for describing the spatial characteristics of geographic features. These schemas define conceptual classes that shall be used in application schemas, profiles and implementation specifications. The document concerns ONLY externally visible interfaces and places no restriction on the underlying implementations other than what is needed to satisfy the interface specifications in the actual situation such as:

- Interfaces to software services using techniques such as COM or CORBA
- Interfaces to databases using techniques such as SQL
- Data interchange using encoding as defined in ISO 19118.

Few applications will require the full range of capabilities described by this conceptual schema. This clause, therefore, defines a set of conformance classes that will support applications whose requirements range from the minimum necessary to define data structures to full object implementation. This flexibility is controlled by a set of UML types that can be implemented in a variety of manners. Implementations that define full object functionality must implement all operations defined by the types of the chosen conformance class, as is common for UML designed object implementations. Implementations that choose to depend on external “free functions” for some or all operations, or forgo them altogether, need not support all operation, but shall always support a data type sufficient to record the state of each of the chosen UML type as defined by its member variables. Common names for “metaphorically identical” but technically different entities are acceptable. The UML model in this International Standard defines abstract types, application schemas define conceptual classes, various software systems define implementation classes or data structures, and the XML from the encoding standard (ISO 19118) defines entity tags. All of these reference the same information content. There is no difficulty in allowing the use of the same name to represent the same information content even though at a deeper level there are significant technical differences in the digital entities being implemented. This “allows” types defined in the UML model to be used directly in application schemas.

There are 39 conformance options for application schemas that define types for the instantiation of geometric or topological objects. They are differentiated on the basis of three criteria.

The first two criteria (complexity and dimensionality) determine the types defined in this schema that shall be implemented according to an application schema that conforms to a given conformance option. In defining the dimensionality of object types to be implemented, the application schema will be required to specify which of

the interpolation types for curves or surfaces they wish to implement. Curve implementations, for those application schemas including 1-dimensional objects, shall always include a “linear” interpolation technique. Application schema including 1-dimensional objects should always include a mechanism to approximate any curve as a line string to allow for transfer of data into simpler schema where needed. Surface implementations, for those application schemas including 2-dimensional objects, shall always include a “planar” interpolation technique. Application schema should always include a mechanism to approximate any surface as collections of planar surface patches to allow for transfer of data into simpler schema where needed. Additional curve and surface interpolation mechanism are optional, but if implemented, they shall follow the definition included in this International Standard.

The third criterion (functional complexity) determines the member elements (attributes, association roles and operations) of those types that shall be implemented. The most limited of such schema would define only data types, and may be used in the transfer of data or the passing of operational parameters to service providers.

The first criterion is level of data complexity. Four levels are identified:

- Geometric primitives
- Geometric complexes
- Topological complexes
- Topological complexes with geometric realization

NOTE Schemas for what is commonly called “spaghetti” data use only unstructured collections of geometric primitives. If single definitions of each component of geometry are required, then geometric complexes are introduced into the schema. Primitives within the same geometric complex share only boundaries. If the schema requires explicit topological information then the geometric complex is expanded to include the structure of a topological complex. The types of object included in a complex are controlled by the dimension of that complex. What is commonly called “chain-node” topology is a 1-dimensional topological complex. What is commonly called “full topology” in a cartographic 2D environment is a 2-dimensional topological complex realized by geometric objects in a 2D coordinate system.

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The second criterion is dimensionality. There are four levels for simple geometry:

- 0-dimensional objects
- 0- and 1-dimensional objects
- 0-, 1-, and 2-dimensional objects
- 0-, 1-, 2- and 3-dimensional objects

However, 0-dimensional complexes provide no useful information beyond that provided by 0-dimensional geometric primitives, so conformance classes are only defined for complexes of 1-, 2-, and 3-dimensions.

The third criterion is level of functional complexity. There are three levels.

- Data types only
- Simple operations
- Complete operations

Clause 8 of this International Standard defines three groups of Boolean operators that may be used to derive topological relations between geometric and topological objects. This International Standard defines four conformance classes for application schemas that implement these operators.

2.2 Conformance classes

To conform to this International Standard, an implementation shall satisfy the requirements of the Abstract test suite (ATS) in Annex A for a specified conformance class. Table 1 through Table 5 identify the clauses of the ATS that apply for each conformance class.

Table 1 — Conformance classes for geometric primitives

Dimension	Data Types	Simple Operations	Complete Operations
0	A.1.1.1	A.1.2.1	A.1.3.1
1	A.1.1.2	A.1.2.2	A.1.3.2
2	A.1.1.3	A.1.2.3	A.1.3.3
3	A.1.1.4	A.1.2.4	A.1.3.4

Table 2 — Conformance classes for geometric complexes

Dimension	Data Types	Simple Operations	Complete Operations
1	A.2.1.1	A.2.2.1	A.2.3.1
2	A.2.1.2	A.2.2.2	A.2.3.2
3	A.2.1.3	A.2.2.3	A.2.3.3

Table 3 — Conformance classes for topological complexes

Dimension	Data Types	Simple Operations	Complete Operations
1	A.3.1.1	A.3.2.1	A.3.3.1
2	A.3.1.2	A.3.2.2	A.3.3.2
3	A.3.1.3	A.3.2.3	A.3.3.3

Table 4 — Conformance classes for topological complexes with geometric realizations

Dimension	Data Types	Simple Operations	Complete Operations
1	A.4.1.1	A.4.2.1	A.4.3.1
2	A.4.1.2	A.4.2.2	A.4.3.2
3	A.4.1.3	A.4.2.3	A.4.3.3

Table 5 — Conformance classes for Boolean operators

Set operators	A.5.1
Egenhofer operators	A.5.2
Full topological operators	A.5.3
All operators	A.5.4

3 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 19109:—¹⁾, *Geographic information — Rules for application schema*

ISO 19111:—¹⁾, *Geographic information — Spatial referencing by coordinates*

ISO/IEC 11404:1996, *Information technology — Programming languages, their environments and system software interfaces — Language-independent datatypes*

4 Terms and definitions

For the purposes of this document, the following terms and definitions apply. The terms are listed alphabetically in this clause. In Annex B they are organized by their conceptual relationships.

4.1

application

manipulation and processing of data in support of user requirements [ISO 19101]

4.2

application schema

conceptual schema for data required by one or more **applications** [ISO 19101]

4.3

bag

finite, unordered collection of related items (**objects** or values) that may be repeated

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NOTE Logically, a bag is a set of pairs <item, count>

4.4

boundary

set that represents the limit of an entity

NOTE **Boundary** is most commonly used in the context of geometry, where the set is a collection of points or a collection of objects that represent those points. In other arenas, the term is used metaphorically to describe the transition between an entity and the rest of its domain of discourse.

4.5

buffer

geometric object that contains all **direct positions** whose distance from a specified **geometric object** is less than or equal to a given distance

4.6

circular sequence

sequence which has no logical beginning and is therefore equivalent to any circular shift of itself; hence the last item in the sequence is considered to precede the first item in the sequence

4.7

class

description of a **set** of **objects** that share the same attributes, operations, methods, relationships, and semantics [ISO/TS 19103]

1) To be published.

NOTE A class may use a **set of interfaces** to specify collections of **operations** it provides to its environment. The term was first used in this way in the general theory of object oriented programming, and later adopted for use in this same sense in UML.

4.8

closure

union of the **interior** and **boundary** of a **topological** or **geometric object**

4.9

coboundary

set of topological primitives of higher topological dimension associated with a particular **topological object**, such that this **topological object** is in each of their **boundaries**

NOTE If a node is on the boundary of an edge, that edge is on the coboundary of that node. Any orientation parameter associated to one of these relations would also be associated to the other. So that if the node is the end node of the edge (defined as the end of the positive directed edge), then the positive orientation of the node (defined as the positive directed node) would have the edge on its coboundary, see Figure 35.

4.10

composite curve

sequence of curves such that each curve (except the first) starts at the end point of the previous curve in the **sequence**

NOTE A composite curve, as a set of **direct positions**, has all the properties of a curve.

4.11

composite solid

connected **set of solids** adjoining one another along shared **boundary surfaces**

NOTE A composite solid, as a set of **direct positions**, has all the properties of a solid.

4.12

composite surface

connected **set of surfaces** adjoining one another along shared **boundary curves**

NOTE A composite surface, as a set of **direct positions**, has all the properties of a surface.

4.13

computational geometry

manipulation of and calculations with geometric representations for the implementation of **geometric operations**

EXAMPLE Computational geometry operations include testing for geometric inclusion or intersection, the calculation of **convex hulls** or **buffer zones**, or the finding of shortest distances between **geometric objects**.

4.14

computational topology

topological concepts, structures and algebra that aid, enhance or define **operations** on **topological objects** usually performed in **computational geometry**

4.15

connected

property of a **geometric object** implying that any two **direct positions** on the object can be placed on a **curve** that remains totally within the object

NOTE A topological object is connected if and only if all its **geometric realizations** are connected. This is not included as a definition because it follows from a theorem of topology.

4.16

connected node

node that starts or ends one or more **edges**