



SLOVENSKI STANDARD
SIST EN ISO 24157:2008

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Ophthalmic optics and instruments - Reporting aberrations of the human eye (ISO 24157:2008)

Augenoptik und ophthalmische Instrumente - Verfahren zur Darstellung von Abbildungsfehlern des menschlichen Auges (ISO 24157:2008)

Optique et instruments ophtalmiques - Méthodes de présentation des aberrations de l'oeil humain (ISO 24157:2008)

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11.040.70 Oftalmološka oprema Ophthalmic equipment

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July 2008

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English Version

Ophthalmic optics and instruments - Reporting aberrations of the human eye (ISO 24157:2008)

Optique et instruments ophtalmiques - Méthodes de présentation des aberrations de l'oeil humain (ISO 24157:2008)

Augenoptik und ophthalmische Instrumente - Verfahren zur Darstellung von Abbildungsfehlern des menschlichen Auges (ISO 24157:2008)

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Foreword

This document (EN ISO 24157:2008) has been prepared by Technical Committee ISO/TC 172 "Optics and optical instruments" in collaboration with Technical Committee CEN/TC 170 "Ophthalmic optics" the secretariat of which is held by DIN.

This European Standard shall be given the status of a national standard, either by publication of an identical text or by endorsement, at the latest by January 2009, and conflicting national standards shall be withdrawn at the latest by January 2009.

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First edition
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**Ophthalmic optics and instruments —
Reporting aberrations of the human eye**

*Optique et instruments ophtalmiques — Méthodes de présentation des
aberrations de l'œil humain*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO 24157 was prepared by Technical Committee ISO/TC 172, *Optics and photonics*, Subcommittee SC 7, *Ophthalmic optics and instruments*.

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Ophthalmic optics and instruments — Reporting aberrations of the human eye

1 Scope

This International Standard specifies standardized methods for reporting aberrations of the human eye.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 8429, *Optics and optical instruments — Ophthalmology — Graduated dial scale*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply. Symbols used are summarized in Table 1.

3.1 line of sight

line from the point of interest in object space to the centre of the entrance pupil of the eye and continuing from the centre of the exit pupil to the retinal point of fixation (generally the foveola)

3.2

Zernike polynomial function

one of a complete set of functions defined and orthogonal over the unit circle, the product of three terms, a normalization term, a radial term and a meridional term, parameterized by a dimensionless radial parameter, ρ , and a dimensionless meridional parameter, θ , designated by a non-negative radial integer index, n , and a signed meridional index, m , and given by the equation

$$Z_n^m = N_n^m R_n^{|m|}(\rho) M(m\theta) \quad (1)$$

where

N_n^m is the normalization term;

$R_n^{|m|}$ is the radial term;

$M(m\theta)$ is the meridional term;

the parameter ρ is a real number continuous over its range of 0 to 1,0;

the parameter θ is a real number continuous over its range of 0 to 2π .

NOTE For a given value of radial index n , the meridional index m may only take the values $-n, -n+2, \dots, n-2$ and n .

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3.2.1

radial term

Zernike polynomial function term with indices n and m given by the equation

$$R_n^{|m|}(\rho) = \sum_{s=0}^{0,5(n-|m|)} \frac{(-1)^s (n-s)!}{s! [0,5(n+|m|)-s]! [0,5(n-|m|)-s]!} \rho^{n-2s} \quad (2)$$

where s is an integer summation index incremented by one unit

3.2.2

radial parameter

ρ

dimensionless number taking values between 0 and 1, its value at any radial distance, r , from the aperture centre being given by the expression

$$\rho = \frac{r}{a} \quad (3)$$

where a is the value of the aperture radius

3.2.3

meridional term

Zernike polynomial function term with index m given by the equations

$$M(m\theta) = \cos(m\theta) \quad \text{if } m \geq 0 \quad (4)$$

$$M(m\theta) = \sin(|m|\theta) \quad \text{if } m < 0 \quad (5)$$

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NOTE The meridional term is also known as the *azimuthal* term.
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3.2.4

meridional parameter

θ

angular value taking values between 0 and 2π (0° and 360°), expressed in the coordinate system defined in Clause 4

NOTE This is also called the *azimuthal* angle.

3.2.5

normalization term

Zernike polynomial function term with indices n and m , equal to 1,0 for “un-normalized” functions (3.2.7) and for “normalized” functions (3.2.6) by the equation

$$N_n^m = \sqrt{(2 - \delta_{0,m})(n+1)} \quad (6)$$

where $\delta_{0,m} = 1$ if $m = 0$, $\delta_{0,m} = 0$ if $m \neq 0$.

3.2.6

normalized Zernike polynomial function

Zernike polynomial function whose normalization term takes the form given in 3.2.5 for “normalized” functions defined as orthogonal in the sense that it satisfies the following equation

$$\int_0^1 \rho d\rho \int_0^{2\pi} Z_n^m Z_{n'}^{m'} d\theta = \pi \delta_{n,n'} \delta_{m,m'} \quad (7)$$

where

$$\delta_{n,n'} = 1 \text{ if } n = n', \delta_{n,n'} = 0 \text{ if } n \neq n';$$

$$\delta_{m,m'} = 1 \text{ if } m = m', \delta_{m,m'} = 0 \text{ if } m \neq m'.$$

3.2.7

un-normalized Zernike polynomial function

Zernike polynomial function whose normalization term is equal to 1,0 and defined as orthogonal in the sense that it satisfies the equation

$$(2 - \delta_{0,m})(n+1) \int_0^1 \rho d\rho \int_0^{2\pi} Z_n^m Z_n^{m'} d\theta = \pi \delta_{n,n'} \delta_{m,m'} \quad (8)$$

where

$$\delta_{n,n'} = 1 \text{ if } n = n', \delta_{n,n'} = 0 \text{ if } n \neq n';$$

$$\delta_{m,m'} = 1 \text{ if } m = m', \delta_{m,m'} = 0 \text{ if } m \neq m';$$

$$\delta_{0,m} = 1 \text{ if } m = 0, \delta_{0,m} = 0 \text{ if } m \neq 0.$$

3.2.8

order

value of the radial index n of a Zernike polynomial function

3.3

Zernike coefficient

member of a set of real numbers, c_n^m , which is multiplied by its associated Zernike function to yield a term that is subsequently used in a sum of terms to give a value equal to the best estimate of the surface, $S(\rho, \theta)$, that has been fitted with Zernike terms, such a sum being represented by

$$S(\rho, \theta) = \sum_{\text{all } n \text{ and } m} c_n^m Z_n^m \quad (9)$$

NOTE 1 Each set of Zernike coefficients has associated with it the aperture diameter that was used to generate the set from surface elevation data. The set is incomplete without this aperture information.

NOTE 2 Annex A gives information on a method to find Zernike coefficients from wavefront slope (gradient) data.

3.3.1

normalized Zernike coefficient

Zernike coefficient generated using normalized Zernike functions and so designed to be used with them to reconstruct a surface

NOTE Normalized Zernike coefficients have dimensional units of length.

3.3.2

un-normalized Zernike coefficient

Zernike coefficient generated using un-normalized Zernike functions and so designed to be used with them to reconstruct a surface

NOTE Un-normalized Zernike coefficients have dimensional units of length.