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Statistično tolmačenje podatkov - 7. del: Mediana - Ocena in intervali zaupanja

Statistical interpretation of data - Part 7: Median - Estimation and confidence intervals

Interprétation statistique des données - Partie 7: Médiane - Estimation et intervalles de confiance

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Statistical interpretation of data —

Part 7:
Median — Estimation and confidence intervals

Interprétation statistique des données —
Partie 7: Médiane — Estimation et intervalles de confiance

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 3.

Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this part of ISO 16269 may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

International Standard ISO 16269-7 was prepared by Technical Committee ISO/TC 69, *Applications of statistical methods*, Subcommittee SC 3, *Application of statistical methods in standaridization*.

ISO 16269 consists of the following parts, under the general title *Statistical interpretation of data*:

— *Part 7: Median — Estimation and confidence intervals*

The following will be the subjects of future parts to ISO 16269:

— *Part 1: Guide to statistical interpretation of data*

— *Part 2: Presentation of statistical data*

— *Part 3: Tests for departure from normality*

— *Part 4: Detection and treatment of outliers*

— *Part 5: Estimation and tests of means and variances for the normal distribution, with power functions for tests*

— *Part 6: Determination of statistical tolerance intervals*

Annexes A and B of this part of ISO 16269 are for information only.

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Statistical interpretation of data —

Part 7:
Median — Estimation and confidence intervals

1 Scope

This part of ISO 16269 specifies the procedures for establishing a point estimate and confidence intervals for the median of any continuous probability distribution of a population, based on a random sample size from the population. These procedures are distribution-free, i.e. they do not require knowledge of the family of distributions to which the population distribution belongs. Similar procedures can be applied to estimate quartiles and percentiles.

NOTE   The median is the second quartile and the fiftieth percentile. Similar procedures for other quartiles or percentiles are not described in this part of ISO 16269.

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2 Normative references

The following normative documents contain provisions which, through reference in this text, constitute provisions of this part of ISO 16269. For dated references, subsequent amendments to, or revisions of, any of these publications do not apply. However, parties to agreements based on this part of ISO 16269 are encouraged to investigate the possibility of applying the most recent editions of the normative documents indicated below. For undated references, the latest edition of the normative document referred to applies. Members of ISO and IEC maintain registers of currently valid International Standards.

ISO 2602, *Statistical interpretation of test results — Estimation of the mean — Confidence interval.*

ISO 3534-1, *Statistics — Vocabulary and symbols — Part 1: Probability and general statistical terms.*

3 Terms, definitions and symbols

3.1 Terms and definitions

For the purposes of this part of ISO 16269, the terms and definitions given in ISO 2602 and ISO 3534-1 and the following apply.

3.1.1
k**th order statistic of a sample**
value of the kth element in a sample when the elements are arranged in non-decreasing order of their values

NOTE   For a sample of n elements arranged in non-decreasing order, the kth order statistics is $x_{[k]}$ where

$$x_{[1]} \leqslant x_{[2]} \leqslant \ldots \leqslant x_{[n]}$$

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3.1.2
median of a continuous probability distribution
value such that the proportions of the distribution lying on either side of it are both equal to one half

NOTE   In this part of ISO 16269, the median of a continuous probability distribution is called the population median and is denoted by M.

3.2   Symbols

a lower bound to the values of the variable in the population

b upper bound to the values of the variable in the population

C confidence level

c constant used for determining the value of k in equation (1)

k number of the order statistic used for the lower confidence limit

M population median

n sample size

T_1 lower confidence limit derived from a sample

T_2 upper confidence limit derived from a sample

u fractile of the standardized normal distribution

$x_{[i]}$ ith smallest element in a sample when the elements are arranged in a non-decreasing order of their values

$\tilde{x}$ sample median

y intermediate value calculated to determine k using equation (1)

4   Applicability

The method described in this part of ISO 16269 is valid for any continuous population, provided that the sample is drawn at random.

NOTE   If the distribution of the population can be assumed to be approximately normal, the population median is approximately equal to the population mean and the confidence limits should be calculated in accordance with ISO 2602.

5   Point estimation

A point estimate of the population median is given by the sample median, $\tilde{x}$. The sample median is obtained by numbering the sample elements in non-decreasing order of their values and taking the value of

⎯   the $[(n + 1)/2]$th order statistic, if n is odd, or

⎯   the arithmetic mean of the $(n/2)$th and $[(n/2) + 1]$th order statistics, if n is even.

NOTE   This estimator is in general biased for asymmetrical distributions, but an estimator that is unbiased for any population does not exist.

6 Confidence interval

6.1 General

A *two-sided confidence interval* for the population median is a closed interval of the form $[T_1, T_2]$, where $T_1 < T_2$; T_1 and T_2 are called the *lower* and *upper confidence limits*, respectively.

If a and b are respectively the lower and upper bounds of the variable in the population, a *one-sided confidence interval* will be of the form $[T_1, b)$ or of the form $(a, T_2]$.

NOTE   For practical purposes, a is often taken to be zero for variables that cannot be negative, and b is often taken to be infinity for variables with no natural upper bound.

The practical meaning of a confidence interval is that the experimenter claims that the unknown M lies within the interval, while admitting a small nominal probability that this assertion may be wrong. The probability that intervals calculated in such a way cover the population median is called the confidence level.

6.2 Classical method

The classical method is described in annex A. It involves solving a pair of inequalities. Alternatives to solving these inequalities are given below for a range of confidence levels.

6.3 Small samples ($5 \leqslant n \leqslant 100$)

The values of k satisfying the equations in annex A for eight of the most commonly used confidence levels for sample sizes varying from 5 to 100 sampling units are given in Table 1 for the one-sided case and in Table 2 for the two-sided case. The values of k are given such that the lower confidence limit is

$$T_1 = x_{[k]}$$

and the upper confidence limit is

$$T_2 = x_{[n-k+1]}$$

where $x_{[1]}, x_{[2]}, ..., x_{[n]}$ are the ordered observed values in the sample.

For small values of n, it can happen that confidence limits based on order statistics are unavailable at certain confidence levels.

An example of the calculation of the confidence limits for small samples is given in B.1 and shown in Form A of annex B.