



Standard Test Method for Detection and Measurement of Partial Discharge (Corona) Pulses in Evaluation of Insulation Systems¹

This standard is issued under the fixed designation D 1868; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

This standard has been approved for use by agencies of the Department of Defense.

1. Scope

1.1 This test method covers the detection and measurement of partial discharge (corona) pulses at the terminals of an insulation system under an applied test voltage, including the determination of partial discharge (corona) inception and extinction voltages as the test voltage is raised and lowered. The test method is also useful in determining quantities such as apparent charge and pulse repetition rate together with such integrated quantities as average current, quadratic rate and power. The test method is useful for test voltages ranging in frequency from zero (direct voltage) to approximately 2000 Hz.

1.2 The test method is directly applicable to a simple insulation system that can be represented as a two-terminal capacitor (1), (2).

1.3 The test method is also applicable to (distributed parameter) insulation systems such as high-voltage cable. Consideration must be given to attenuation and reflection phenomena in this type of system. Further information on distributed parameter systems will be found in Refs. (1), (2), (3), and (4).²

1.4 The test method can be applied to multi-terminal insulation systems, but at some loss in accuracy, especially where the insulation of inductive windings is involved.

1.5 *This standard does not purport to address all of the safety problems, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.* Specific precaution statements are given in Sections 8 and 14.

2. Referenced Documents

2.1 ASTM Standards:

¹ This test method is under the jurisdiction of ASTM Committee D-9 on Electrical and Electronic Insulating Materials and is the direct responsibility of Subcommittee D09.12 on Electrical Tests.

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² The boldface numbers in parentheses refer to the list of references at the end of this test method.

D 149 Test Method for Dielectric Breakdown Voltage and Dielectric Strength of Solid Electrical Insulating Materials at Commercial Power Frequencies³

D 618 Practice for Conditioning Plastics and Electrical Insulating Materials for Testing⁴

D 2275 Test Method for Voltage Endurance of Solid Electrical Insulating Materials Subjected to Partial Discharges (Corona) on the Surface³

D 3382 Test Methods for Measurement of Energy and Integrated Charge Transfer Due to Partial Discharges (Corona) Using Bridge Techniques⁵

2.2 Other Documents:

AEIC CS5-87 Specifications for Thermoplastic and Crosslinked Polyethylene Insulated Shielded Power Cables Rated 5 through 35 kV (9th Edition) October 1987⁶

ICEA T-24-380 Guide for Partial Discharge Procedure⁷

IEEE 48 Standard Test Procedures and Requirements for High Voltage Alternating Current Cable Terminations⁸

3. Terminology

3.1 *Definitions*—The following terms are presented in a developing sequence; it is best that they be read in their entirety:

3.1.1 *ionization*—the process by which electrons are lost from or transferred to neutral molecules or atoms to form positively or negatively charged particles.

3.1.2 *partial discharge (corona)*—an electrical discharge that only partially bridges the insulation between conductors. A transient gaseous ionization occurs in an insulation system if

³ Annual Book of ASTM Standards, Vol 10.01.

⁴ Annual Book of ASTM Standards, Vols 08.01 and 10.01.

⁵ Annual Book of ASTM Standards, Vol 10.02.

⁶ Available from the publication department of the Association of Edison Illuminating Companies, 600 N. 18th St., PO Box 2641, Birmingham, AL 35291-0992.

⁷ Available from the Insulated Cable Engineers Association, Inc., PO Box 440, South Yarmouth, MA 02664.

⁸ Available from the Institute of Electrical and Electronics Engineers Service Center, 445 Hoes Lane, Piscataway, NJ 08854.

the voltage stress exceeds a critical value, and this ionization produces partial discharges.

3.1.3 *corona*—visible partial discharges in gases adjacent to a conductor. This term has also been used to refer to partial discharges in general.

3.1.4 *continuous partial discharges (continuous corona)*—discharges that recur at rather regular intervals; for example on approximately every cycle of an alternating voltage or at least once per minute for an applied direct voltage.

3.1.5 *partial discharge (corona) inception voltage (PDIV [CIV])*—the lowest voltage at which continuous partial discharges above some stated magnitude (which may define the limit of permissible background noise) occur as the applied voltage is gradually increased (Note 1). Where the applied voltage is alternating, the PDIV is expressed as $1/\sqrt{2}$ of the peak voltage. Many test and specimen parameters can affect this value, and in some cases reproducibility may be difficult to achieve.

NOTE 1—Many factors may influence the value of the PDIV and PDEV including the rate at which the voltage is increased or decreased as well as the previous history of the voltage applied to the specimen. In many cases it may be difficult to obtain the same value with subsequent tests.

Moreover, the “continuous” character of the partial discharges is sometimes quite difficult to define, and an arbitrary judgment in this respect may lead to different values of the PDIV or PDEV.

3.1.6 *partial discharge (corona) extinction voltage (PDEV [CEV])*—the highest voltage at which partial discharges above some stated magnitude no longer occur as the applied voltage is gradually decreased from above the inception voltage (see Note 1). Where the applied voltage is alternating, the PDEV is expressed as $1/\sqrt{2}$ of the peak voltage. Many test and specimen parameters can affect this value, and in some cases reproducibility may be difficult to achieve.

3.1.7 *partial discharge pulse voltage (V_t)*—the terminal pulse voltage resulting from a partial discharge represented as a voltage source suddenly applied in series with the capacitance of the insulation system under test, and that would be detected at the terminals of the system under open-circuit conditions.

3.1.8 *partial discharge quantity (terminal corona charge) (Q_t)*—the magnitude of an individual discharge in an insulation system expressed in terms of the charge transfer measured at the system terminals. The measured charge is in general not equal to the charge transferred at the discharge site, and does have a relation to the discharge energy. For a small specimen that can be treated as a simple lumped capacitor, it is equal to the product of the capacitance of the insulation system and the partial discharge pulse voltage, that is:

$$Q_t = C_t V_t \quad (1)$$

where:

- Q_t = partial discharge quantity, C,
- C_t = capacitance of the specimen insulation system, F, and
- V_t = peak value of the partial discharge pulse voltage appearing across C_t , V.

3.1.9 *partial discharge (corona) level*—the magnitude of the greatest recurrent discharge during an observation of continuous discharges.

3.1.10 *average discharge (corona) current (I_t)*—the sum of the absolute magnitudes of the individual discharges during a certain time interval divided by that time interval. When the discharges are measured in coulombs and the time interval in seconds, the calculated current will be in amperes.

$$I_t = \frac{\sum_{t_0}^{t_1} Q_1 + Q_2 + \dots + Q_n}{t_1 - t_0} \quad (2)$$

where:

- I_t = average current, A,
- t_0 = starting time, s,
- t_1 = completion time, s, and
- Q_1, Q_2, Q_n = partial discharge quantity in a corona pulse 1 through n, C.

3.1.11 *quadratic rate*—the sum of the squares of the individual discharge magnitudes during a certain time interval divided by that time interval. The quadratic rate is expressed as (coulombs)² per second.

3.1.12 *partial discharge (corona) energy (W)*—the energy drawn from the test voltage source as the result of an individual discharge. It is the product of the magnitude Q of that discharge and the instantaneous value V of the voltage across the test specimen at the inception of the discharge (5). Thus the discharge energy of the i th pulse is:

$$W_i = Q_i V_i \quad (3)$$

where:

- W_i = the discharge energy, W-s (= J),
- Q_i = the partial discharge magnitude, (see 3.1.8), and
- V_i = the instantaneous value of the applied test voltage at the time of the discharge, V.

3.1.13 *partial discharge (corona) power loss (P)*—the summation of the energies drawn from the test voltage source by individual discharges occurring over a period of time, divided by that time period.

$$P = \frac{1}{T} \sum_{i=1}^{i=m} Q_i V_i \quad (4)$$

where:

- P = the discharge power, W,
- T = the time period, s,
- m = the number of the final pulse during T, and
- $Q_i V_i$ = the discharge energy of the i th pulse (see 3.1.12).

When pulse height analysis is used, the summation over a period of time of pulses above a preset level of corona usually determined by background noise multiplied by the instantaneous test voltage at the time of the pulses in the specimen is approximately equal to:

$$P = \sum_{j=1}^i n_j Q_{ij} V_j \quad (5)$$

where:

- P = pulse discharge power loss, W,
- n_j = recurrence rate of the j th discharge pulse in pulses/second.
- Q_{ij} = the corresponding value of the partial discharge quantity in coulombs for the particular pulse.

V_j = instantaneous value of the applied voltage in volts at which the j th discharge pulse takes place (6).

If the assumption (7) is made that $V_j \Delta C_j \approx C_i \Delta V_j$ (where ΔC_j is incremental capacitance rise in C_i due to the drop ΔV_j in V_j as a result of the j th discharge), then the above summation must be multiplied by $1/2$. However, this assumption is not usually borne out in practice.

3.1.14 *partial discharge apparent power loss (P_a)*—the summation over a period of time of all corona pulse amplitudes multiplied by the rms test voltage.

$$P_a = I_t V_s \quad (6)$$

where:

P_a = apparent power loss in time interval ($t_1 - t_0$), W,

I_t = average corona current, A, and

V_s = applied rms test voltage, V.

3.1.15 *partial discharge (corona) pulse rate (n)*—the average number of discharge pulses that occur per second or in some other specified time interval. The pulse count may be restricted to pulses above a preset threshold magnitude, or to those between stated lower and upper magnitude limits.

3.1.16 *partial discharge pulse*—a voltage or current pulse that occurs at some designated location in a circuit as a result of a partial discharge.

4. Summary of Test Method

4.1 A specimen insulation system is energized in a test circuit by a high-voltage source. A partial discharge (corona) in the specimen will cause a sudden charge transfer and a resulting voltage pulse at the specimen terminals. A measuring instrument coupled to the terminals may be calibrated to respond to the voltage pulse in terms of the charge transferred at the terminals.

5. Significance and Use

5.1 The presence of partial discharges (corona) at operating voltage in an insulation system may result in a significant reduction in the life of the insulating material. Some materials are more susceptible to such discharge damage than others. This characteristic can be investigated using Test Method D 2275 (6).

5.2 The presence of partial discharges (corona) in an apparently solid insulation may be an indication of the existence of internal cavities. Partial discharge tests have been useful in the design and inspection of molded, laminated, and composite insulation, as well as specimens in the form of cables, capacitors, transformers, and bushings.

5.3 Partial discharge (corona) inception and extinction voltages are used in the determination of the limiting voltage at which an insulation system will operate free of such discharges. The extinction voltage is often substantially lower than the inception voltage. Where the operating voltage is below the inception voltage but above the extinction voltage, a transient over-voltage may initiate discharges which then continue until the voltage is lowered below the extinction voltage. Inception and extinction voltages depend upon many factors, including temperature and the rate at which the voltage is changed. After a time at a voltage, discharges may start and

stop in a nonuniform and unpredictable fashion, especially for discharges within cavities in certain materials.

5.4 The magnitude (pulse height) of a partial discharge is an indication of the amount of energy that it dissipates in the insulation system. Partial discharge magnitude and pulse rate are useful in estimating the rate, or change of rate, at which deterioration is produced.

5.5 In general, the occurrence of partial discharges is not directly related to the basic properties of a solid insulating material, but usually results from overstressing of gaseous occlusions or similar imperfections or discontinuities in an insulating system. Partial discharges may originate at locations such as on the leads or terminals without resulting in any hazard within the main part of the insulation system.

6. Interference

6.1 Radiated or conducted electrical disturbances from sources other than the test specimen may interfere with the measurement of partial discharges. The magnitude of disturbances reaching the measuring instrument must be kept small relative to the most sensitive measurements to be made.

6.2 Interference from radiation may be reduced by shielding the test circuit or by conducting the test in a shielded room. Interference by conduction may be suppressed by means of a low-pass filter in the voltage supply circuit.

6.3 Corona on the connecting leads between the test voltage source and the specimen may interfere with the measurement. Such interference may be avoided if the leads are smooth-surfaced and of sufficient diameter, with spherical terminals.

6.4 Interference may often be identified from the display of an oscilloscope coupled to the measuring circuit, with its horizontal deflection relating to the instantaneous value of the test voltage. For example, pulses that appear only during the negative half-cycle of the alternating test voltage are often the result of corona originating on the connecting lead or terminal rather than the result of partial discharges within the specimen.

6.5 Interference may be controlled by the use of time window circuits that suppress the measuring device input during the portion of the test voltage wave when partial discharges do not occur, that is, at the voltage zero-crossing points. Using this technique take care to avoid the loss of wanted signals. Other more sophisticated interference suppression techniques of signal processing can be used (1).

7. Apparatus

7.1 Test Voltage Supply:

7.1.1 The voltage supply must be capable of energizing the test circuit, including the specimen, over a range of voltages to the maximum desired test value. The requirements in Test Method D 149 may be used. The frequency of the supply voltage should preferably be the frequency that will be used in service of the specimen.

7.1.2 The voltage supply must not introduce into the measuring circuit pulses of sufficient magnitude to interfere with the most sensitive measurement. The internal impedance including the shunt capacitance of the voltage supply must not significantly reduce the sensitivity of the measurement. To assist in meeting these two requirements, a supply impedance,

preferably in the form of a low-pass filter, may be inserted in the output circuit of the voltage supply.

7.1.3 The voltage supply shall include a voltmeter that responds to the peak voltage applied to the test circuit and permits measurements of the voltage directly across the insulation system.

7.2 *Coupling Capacitor (C_{cc})*—The capacitance value of this capacitor is selected in relation to other circuit components to realize the desired circuit sensitivity (see circuit sensitivity expressions in X1.1). A value of 100 pF is often satisfactory for low-capacitance specimens. In general, a higher capacitance value will improve circuit sensitivity but will require increased charging current from the test voltage supply. The coupling capacitor shall not introduce into the circuit pulses of sufficient magnitude to interfere with the most sensitive measurement.

7.3 *Measuring Impedance:*

7.3.1 The measuring impedance should have a value at test frequency that is low in comparison with other circuit elements to prevent the appearance of an excessive portion of the test voltage at the input terminals of the measuring device. The measuring impedance is usually inductive or resistive.

7.3.2 An inductive impedance, shunted by stray capacitance (consisting of connection cables and component mountings), produces an oscillatory response to a partial discharge pulse. The persistence of the oscillations facilitates pulse observation, but reduces resolution between pulses. Resolution can be changed by the use of a shunting resistor to damp the oscillation or by modifying the frequency response of the discharge measuring system.

7.3.3 A resistive impedance, shunted by stray capacitance, produces an exponentially decaying step response to a discharge pulse. A resistive impedance is used to provide maximum pulse resolution and where the impedance must be adjusted, as in a bridge circuit.

7.4 *Measuring Devices:*

7.4.1 A cathode-ray oscilloscope may be used to display and measure the discharge pulses that appear across the measuring impedance. The pulses are amplified by the vertical deflection amplifier, which must respond to the important frequency components of the pulses. Bandwidth in the range from 25 kHz to several hundred thousand Hz have been found satisfactory. The height of the vertical deflection caused by a partial discharge can be related to the discharge magnitude. In a common arrangement, the vertical deflections are superimposed on an elliptical oval trace synchronized with the test voltage. Thus the point on the voltage wave at which each discharge occurs can be visualized. The oscilloscope may be equipped with a beam-brightening or pulse-stretching circuit to facilitate the observation of peak deflections.

7.4.2 The partial discharge level may be measured by a peak-reading voltmeter connected across the measuring impedance. The meter must be able to respond accurately over a range of pulse rates between 1 and at least 1000 per second.

7.4.3 The average discharge current may be measured by an instrument that responds to the average value of the rectified discharge pulses that occur in a certain time interval. Precautions may be necessary to avoid oscillations in the measuring circuit that could reduce accuracy. Alternatively, the average

discharge current may be determined from a pulse height distribution curve (see 7.4.7).

7.4.4 The quadratic rate may be measured by an instrument that responds to the mean square value of the discharge pulses that occur in a certain time interval. A suitable rectifier or a thermal detector may be used to provide the squaring function.

7.4.5 The apparent discharge power loss may be determined from the area under a pulse height distribution curve (see 7.4.7). A useful approximation of the discharge power loss for an alternating test voltage may be obtained from an instrument that responds to the product of the average discharge current and the rMS value of the test voltage.

NOTE 2—Power loss due to continuous partial discharges under alternating voltage may be determined by Method A of Test Methods D 3382. Alternatively, Method B of Test Methods D 3382 may be used to obtain discharge energy per cycle in joules and then multiplying by the frequency to obtain the loss in watts.

7.4.6 A pulse counter responsive to either positive or negative pulses may be used to measure the partial discharge (corona) pulse rate, n . A rectifier bridge may be employed to obtain total pulse counts of the combined positive and negative pulse responses. Suitable pulse-shaping circuits applied across the measuring impedance must be employed to ensure that each discharge pulse is recorded as a single event. When oscillatory responses are involved, a demodulation circuit with proper active filtering constitutes an effective means for obtaining smooth pulses having a single polarity (6). When high pulse resolution is desired and the pulses are already unidirectional but contain superimposed high-frequency oscillations, pulse shaping may be carried out using multivibrator circuits (8). An amplifier with a suitable bandwidth may be inserted between the measuring impedance and the pulse-shaping circuit to provide adequate sensitivity. A controlled gating system may be employed to prevent the counting of pulses below selected magnitude levels. For example, in high ambient noise environments it may be useful to avoid counting pulses below a preset level.

7.4.7 Single- or multichannel pulse-height analyzers may be utilized to obtain curves of the partial discharge pulse rate, n , as a function of the discharge magnitude, Q . The area under such pulse height distribution curves is given by

$$A(n, Q) = \int_0^{\infty} n(Q)dQ \quad (7)$$

and is dimensionally equal to the corona current and is proportional to the partial discharge power loss. As in the case of pulse counters (7.4.6), the use of proper pulse shaping and amplification circuitry is of the utmost importance to ensure a meaningful pulse-height analysis.

7.5 *Calibration Capacitor (C_c)*—The calibration capacitor should preferably not exceed 200 pF. If its position in the test circuit subjects it to the test voltage, the capacitor shall not introduce into the measuring circuit discharge pulses of sufficient magnitude to interfere with the most sensitive measurement, and it must have a voltage rating equal to the highest test voltage.

7.6 *Calibration Pulse Generator*—The pulse generator must have an output impedance of not more than 100 Ω capable of withstanding the charging current at test voltage of

the calibration capacitor. When connected to the circuit the generator must produce pulses having a rise time of 0.1 μ s or less and a decay time to half crest of greater than 1 ms. Provision must be made for determining the crest value of the output pulse. A square-wave generator that meets these requirements is a satisfactory pulse source. The maximum repetition rate of the pulse generator should be 12.5 kHz.

8. Hazards

8.1 The portion of the test area that includes the test specimen and other components of the test circuit to be energized at high voltage shall be blocked from easy access and marked by warning signs. Doors or gates to this area shall be provided with switches interlocked with the test voltage supply system.

8.2 Provision shall be made for the remote (automatic) grounding of the high-voltage circuit. The high-voltage circuit shall not be approached unless a ground is applied. This precaution is especially important when direct-voltage tests are employed, since the circuit may remain charged at high voltage after the energizing source is interrupted.

8.3 Surge voltage protectors must be applied to those parts of a measuring circuit that must be accessible during the measurement, such as the measuring device and calibration pulse generator, to minimize danger from accidental high voltage which could result from the failure of the test specimen, high-voltage calibration capacitor, or other circuit element. The instrumentation must be enclosed in a grounded case.

8.4 It is recommended that the safety practices as outlined in paragraph 2.0 to 2.8 of Ref. (9) be followed.

9. Sampling

9.1 Because this test method is used on a variety of insulating materials and systems, no one sampling procedure can be specified. Material specification methods may provide guidance. For some insulation systems, each production unit is tested individually as a quality control measure.

10. Test Specimens

10.1 Specimens may be entire insulation systems with normally included electrodes. Discharge measurements may be

made between any two insulated sets of conductors or metallic parts. Other conductors or metallic parts may or may not be grounded, but their disposition should be noted in the report.

10.2 Where the test specimen does not have its own electrode system, temporary electrodes must be applied. There should be no cavities between an electrode and the surface of the specimen insulation, since discharges in such cavities cannot be distinguished from partial discharge within the specimen. A film of insulating paste or grease spread on the surface of the insulation before applying the electrode is helpful in preventing discharges at this location.

10.3 When the test specimen is energized in air, corona may occur in the air at the edges of the electrodes. If the measurement is to be confined to internal discharges, edge corona may be suppressed by immersing the test specimen in a suitable dielectric fluid, or by covering the edges with a thick coat of insulating paste or grease.

11. Arrangement of Apparatus

11.1 Some common circuit arrangements are shown in Figs. 1-3. In these figures the test specimen is represented by capacitor C_t , the calibration capacitor by capacitance C_c , and the coupling capacitor as capacitance C_{cc} . Optional connections for the calibration circuit are indicated by broken lines. The calibration circuit may be disconnected during the application of high voltage to the test specimen (see 12.4).

11.2 The circuit of Fig. 1 may be used when it is convenient to have one terminal of the specimen grounded. The circuit of Fig. 2 is suitable for specimens of small dimensions that can be easily isolated from ground. The circuit of Fig. 3 is advantageous for minimizing interference conducted from the test voltage supply. In this circuit the measuring impedance is composed of two adjustable resistance sections, one section in series with the test specimen and the other in series with the coupling capacitor. Proper balancing of the resistance values can substantially reduce the level of conducted interference appearing across the input terminals of the measuring device.

11.3 Precautions must be taken to avoid corona on the high-voltage connecting leads (see 6.3).

11.4 Stray capacitance between connecting leads and between leads and ground generally reduces the maximum

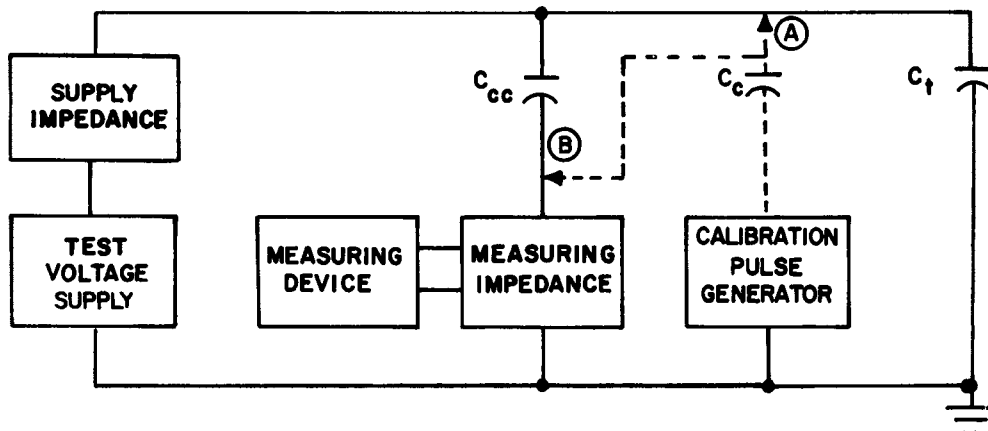


FIG. 1 Circuit No. 1

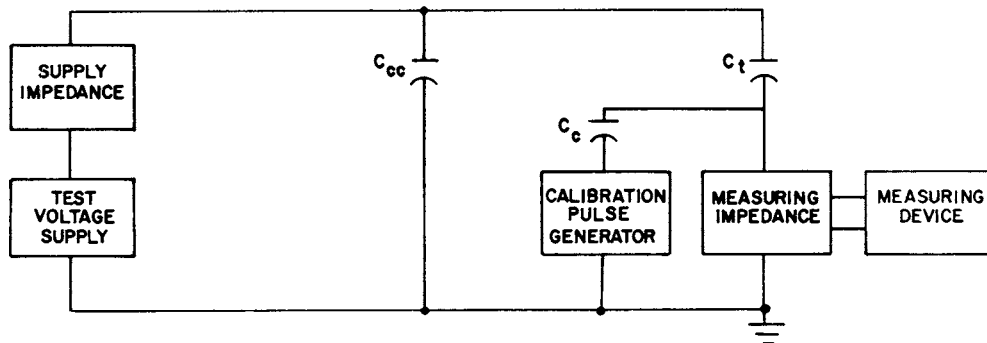


FIG. 2 Circuit No. 2

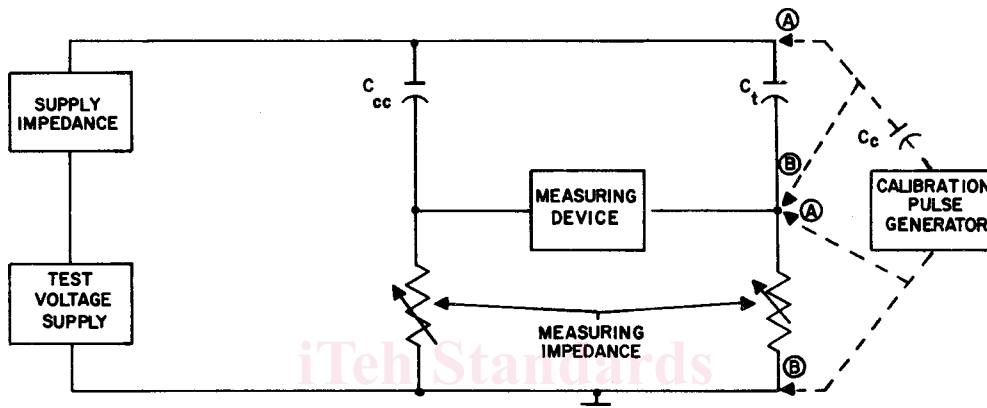


FIG. 3 Circuit No. 3

achievable sensitivity of the test circuit. Leads should be well spaced from each other and from ground.

12. Calibration

12.1 A calibration procedure is carried out to establish a scale factor relating the response of the measuring device to the magnitude of a discharge pulse. Since the response of the measuring device is affected by the value and location of the various test circuit components, the calibration must involve the entire test circuit. Recalibration is required for each test specimen (except for specimens of the same dimensions and capacitance) or when any other test circuit component is changed or relocated.

12.2 In the calibration procedure, a calibration circuit consisting of a calibration pulse generator in series with a calibration capacitor is connected to the test circuit. The calibration circuit produces a pulse resulting in equivalent response in the detection system to a partial discharge pulse. The value of charge (Q) in picocoulombs is equal to the product of the crest voltage (E) in volts of the pulse produced by the calibration generator, and the capacitance (C_c) in picofarads of the calibration capacitor. From the observed response of the measuring device, a scale factor relating the calibrating pulse response to the partial discharge response can be established. By adjustment of the sensitivity of the measuring device, its response may be made to correspond to a precalibrated magnitude scale. The scale factor as determined for a given calibration pulse magnitude may be applied to all magnitudes within the linear response range of the measuring device.

12.3 Two methods of calibration can be carried out, (1) direct, (2) indirect. In the direct method, the calibration is performed with the calibration signal being applied directly across the terminal of the test specimen as in Fig. 1 and Fig. 3 connection A. When the calibration capacitor is to remain in the circuit during test, the calibration capacitor must be able to withstand the highest test voltage and have partial discharge with a lower level than the specimen to be tested. When the calibration capacitor is not to remain connected to the specimen high-voltage terminal during application of test voltage, a correction of the system sensitivity must be made to compensate for its removal. See Appendix X1 for correction factor.

12.4 When the calibration capacitor is disconnected, it may be reconnected as in Fig. 1 and Fig. 3 connection B, and Fig. 2 to perform an indirect method of calibration and determine a correction factor. The ratio of the sensitivity determined by the direct to indirect method is called the correction factor. By maintaining the measuring device sensitivity constant when going from the direct to indirect methods and adjusting the calibration pulse generator output, the correction factor can be made to equal unity.

12.5 To calibrate a device for the measurement of pulse rate, average discharge current, or quadratic rate, the calibration pulses may be supplied by a square-wave generator. The frequency (f) of the generator may be in the 50 to 5000-Hz range. A pulse-rate measuring device should indicate a value of $2f$, since each wave generates one positive and one negative pulse. A device for measuring the average discharge current should indicate a value of $2fQ$ picoamperes, where Q is the