TECHNICAL SPECIFICATION

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Geometrical product specifications (GPS) — Filtration —

Part 22: Linear profile filters: Spline filters

iTeh ST Partie 22: Filtres de profil linéaires: Filtres splines (standards.iteh.ai)

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of technical committees is to prepare International Standards. Draft International Standards adopted by the technical committees are circulated to the member bodies for voting. Publication as an International Standard requires approval by at least 75 % of the member bodies casting a vote.

In other circumstances, particularly when there is an urgent market requirement for such documents, a technical committee may decide to publish other types of normative document:

- an ISO Publicly Available Specification (ISO/PAS) represents an agreement between technical experts in an ISO working group and is accepted for publication if it is approved by more than 50 % of the members of the parent committee casting avote; TANDARD PREVIEW
- an ISO Technical Specification (ISO/TS) represents an agreement between the members of a technical committee and is accepted for publication if it is approved by 2/3 of the members of the committee casting a vote.

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An ISO/PAS or ISO/TS is reviewed after three years in order to decide whether it will be confirmed for a further three years, revised to become an International Standard, or withdrawn. If the ISO/PAS or ISO/TS is confirmed, it is reviewed again after a further three years, at which time it must either be transformed into an International Standard or be withdrawn.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights.

ISO/TS 16610-22 was prepared by Technical Committee ISO/TC 213, *Dimensional and geometrical product specifications and verification*.

ISO/TS 16610 consists of the following parts, under the general title *Geometrical product specifications* (*GPS*) — *Filtration*:

- Part 1: Overview and basic concepts
- Part 20: Linear profile filters: Basic concepts
- Part 22: Linear profile filters: Spline filters
- Part 29: Linear profile filters: Spline wavelets
- Part 31: Robust profile filters: Gaussian regression filters
- Part 32: Robust profile filters: Spline filters
- Part 40: Morphological profile filters: Basic concepts

- Part 41: Morphological profile filters: Disk and horizontal line-segment filters
- Part 49: Morphological profile filters: Scale space techniques

The following parts are under preparation:

- Part 21: Linear profile filters: Gaussian filters
- Part 26: Linear profile filters: Filtration on nominally orthogonal grid planar data sets
- Part 27: Linear profile filters: Filtration on nominally orthogonal grid cylindrical data sets
- Part 30: Robust profile filters: Basic concepts
- Part 42: Morphological profile filters: Motif filters
- Part 60: Linear areal filters: Basic concepts
- Part 61: Linear areal filters: Gaussian filters
- Part 62: Linear areal filters: Spline filters
- Part 69: Linear areal filters: Spline wavelets
- Part 70: Robust areal filters: Basic concepts A RD PREVIEW
- Part 71: Robust areal filters: Gaussian regression filtersh.ai)
- Part 72: Robust areal filters: Spline filters 16610-22:2006
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- Part 80: Morphological areal filters: Basic concepts 610-22-2006
- Part 81: Morphological areal filters: Sphere and horizontal planar segment filters
- Part 82: Morphological areal filters: Motif filters
- Part 89: Morphological areal filters: Scale space techniques

Introduction

This part of ISO/TS 16610 is a geometrical product specification (GPS) Technical Specification and is to be regarded as a global GPS Technical Report (see ISO/TR 14638). It influences the chain links 3 and 5 of all chains of standards.

For more detailed information about the relation of this part of ISO/TS 16610 to the GPS matrix model, see Annex F.

This part of ISO/TS 16610 develops the terminology and concepts of spline filters.

The spline filter has an advantage over a conventional phase correct filter in that for open profiles, the ends of the measured profile are still usable.

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Geometrical product specifications (GPS) — Filtration —

Part 22: Linear profile filters: Spline filters

1 Scope

This part of ISO/TS 16610 specifies spline filters for the filtration of profiles. It specifies in particular how to separate the long and short wave component of a profile.

2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies A RD PREVIEW

ISO/TS 16610-1:2006, Geometrical product specifications (GPS) - Filtration — Part 1: Overview and basic terminology

ISO/TS 16610-20:2006, Geometrical product specifications (GPS) — Filtration — Part 20: Linear profile filters: Basic concepts https://standards.iteh.a/catalog/standards/sist/a0074dd0-024e-4025-92fb-1a01df0fc8dd/iso-ts-16610-22-2006

International vocabulary of basic and general terms in metrology (VIM). BIPM, IEC, IFCC, ISO, IUPAC, IUPAP, OIML, 2nd ed., 1993

3 Terms and definitions

For the purposes of this document, the terms and definitions given in VIM, ISO/TS 16610-1 and ISO/TS 16610-20, and the following apply.

3.1

spline

linear combination of piecewise polynomials, with a smooth fit between the pieces

NOTE The degree of the spline is equal to the degree of the polynomial of the highest degree used, e.g. a cubic spline is made of cubic polynomials.

3.2

cardinal spline

basic function of the space of **splines** (3.1) with infinite support

3.3

natural spline

spline (3.1) which is a straight line beyond the end points

3.4 spline profile filter

linear profile filter based on **splines** (3.1)

NOTE For the purposes of this part of ISO/TS 16610, the result of the low-pass filtering is a spline.

4 Spline profile filters

4.1 General

For a spline filter to conform with this part of ISO/TS 16610, it shall satisfy the filter equations given in 4.3.2, for open profiles, and 4.3.3, for closed profiles.

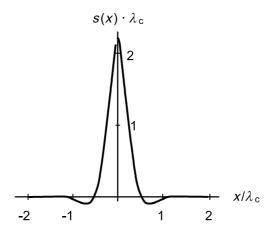
NOTE A comparison with Gaussian filters is given in Annex B, and illustrative examples are given in Annex C. A concept diagram for the concepts of spline filters is given in Annex D, and the relationship to the filtration matrix model is given in Annex E.

4.2 Weighting function

The weighting function of a spline profile filter cannot be given by a simple closed formula. Filter equations are therefore used instead of weighting functions to describe the spline profile filters. However, where necessary, a numerical calculation of the weighting function for a spline profile filter is always possible. If the sampling interval Δx is small enough, and the spline profile filter is based on cardinal cubic splines, the weighting function s(x), with a default value of $\beta = 0$, can be approximated by the continuous function

$$s(x) = \frac{\pi}{\lambda_{c}} \sin\left(\sqrt{2} \frac{\pi}{\lambda_{c}} |x| + \frac{\pi}{4}\right) \exp\left(-\sqrt{2} \frac{\pi}{\lambda_{c}} |x|\right) \frac{\pi}{\lambda_{c}} \log\left(-\sqrt{2} \frac{\pi}{\lambda_{c}} |x|\right) \frac{\pi}{150/15} \frac{\pi}{16610-22:2006}$$
(1)

NOTE This is the weighting function of the ideal splige profile filter, based ion cardinal cubic splines. A graph of this function is shown in Figure 1. 1a01df0fc8dd/iso-ts-16610-22-2006





4.3 Filter equations

4.3.1 General

The following filter equations for spline profile filters are based on cardinal cubic splines (for more details, see [1] and [2]).

4.3.2 Filter equation for the non-periodic spline profile filter

Non-periodic spline profile filters should be used in cases of filtering open profiles. The filter equation for the non-periodic spline profile filter is given by

$$\left[1+\beta\alpha^2 P+(1-\beta)\alpha^4 Q\right]w=z$$
(2)

with the matrix

with *n* rows, *n* columns and the parameters (standards.iteh.ai)

$$\alpha = \frac{1}{2\sin\frac{\pi\Delta x}{\lambda_{c}}} \quad \text{and } 0 \le \beta \le 1 \underbrace{\frac{\text{ISO/TS 16610-22:2006}}{\text{IsO/TS 16610-22:2006}}}_{\text{1a01df0fc8dd/iso-ts-16610-22-2006}}$$

where

- *n* is the number of extracted data values of the profile;
- z is the vector of dimension n of the profile values before filtering;
- w is the vector of dimension n of the profile values in the filtered profile;
- λ_{c} is the cut-off wavelength of the profile filter;
- Δx is the sampling interval.

NOTE 1 The vector w gives the profile values of the long wave component. The short wave component r can be obtained by the difference vector r = z - w, i.e. by subtracting the long wave component values obtained by the filtering process from the extracted data values of the profile.

NOTE 2 β is called the tension parameter, and controls how tightly the spline curve fits through the data points.

NOTE 3 Algorithms to solve matrix equations can be found in [6].

(4)

4.3.3 Filter equation for the periodic spline profile filter

Periodic spline profile filters should be used in cases of filtering closed profiles. The filter equation for the periodic spline profile filter is given by

$$\left[1+\beta\alpha^{2}\tilde{P}+(1-\beta)\alpha^{4}\tilde{Q}\right]\tilde{w}=\tilde{z}$$
(5)

with the matrix

$$\tilde{P} = \begin{pmatrix} 2 & -1 & & -1 \\ -1 & 2 & -1 & & \\ & -1 & 2 & -1 & & \\ & & \ddots & \ddots & \ddots & \ddots & \\ & & -1 & 2 & -1 & \\ & & & -1 & 2 & -1 \\ & & & & -1 & 2 \end{pmatrix} \qquad \tilde{Q} = \begin{pmatrix} 6 & -4 & 1 & & 1 & 1 & -4 \\ -4 & 6 & -4 & 1 & & 1 \\ 1 & -4 & 6 & -4 & 1 & \\ & & \ddots & \ddots & \ddots & \ddots & \ddots & \\ & & 1 & -4 & 6 & -4 & 1 \\ 1 & & & 1 & -4 & 6 & -4 \\ -4 & 1 & & 1 & -4 & 6 \end{pmatrix}$$
(6)

with *n* rows, *n* columns and the parameters

$$\alpha = \frac{1}{2\sin\frac{\pi\Delta x}{\lambda_{\rm c}}} \text{ and } 0 \le \beta \le 1$$
(7)

where

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- *n* is the number of extracted data values of the profiles.iteh.ai)
- \tilde{z} is the vector of dimension *n* of the profile values before filtering;

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- \tilde{w} is the vector of dimension *n* of the profile values in the filtered profile;
- λ_{c} is the cut-off wavelength of the profile filter;
- Δx is the sampling interval.

NOTE 1 The vector \tilde{w} gives the profile values of the long wave component. The short wave component \tilde{r} can be obtained by the difference vector $\tilde{r} = \tilde{z} - \tilde{w}$, i.e. by subtracting the long wave component values obtained by the filtering process from the extracted data values of the profile.

NOTE 2 β is called the tension parameter, and controls how tightly the spline curve fits through the data points.

NOTE 3 Algorithms to solve matrix equations can be found in [6].

4.4 Transmission characteristics

4.4.1 General

The following transmission characteristics for spline profile filters are based on cardinal cubic splines. For more details, see [3]. For the influence of the sampling interval, see Annex A.

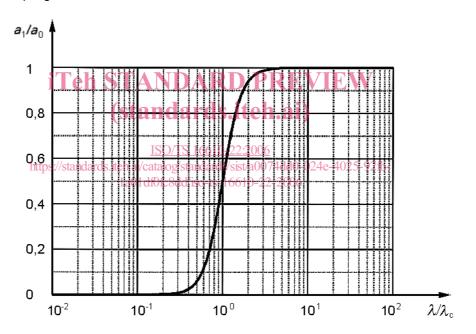
4.4.2 Transmission characteristic of the long wave profile component

The filter characteristic (see Figure 2) is determined from the filter equations of the spline profile filter by means of the Fourier transformation. The filter characteristic for the long wave component is approximated (for very small Δx) by the following equation:

$$\frac{a_1}{a_0} = \left[1 + \beta \alpha^2 \sin^2 \frac{\pi \Delta x}{\lambda} + 16(1 - \beta) \alpha^4 \sin^4 \frac{\pi \Delta x}{\lambda}\right]^{-1}$$
(8)

where

- a_0 is the amplitude of the sinusoidal profile before filtering;
- a_1 is the amplitude of the sinusoidal profile in the long wave component;
- λ is the wavelength of the sine profile $(\lambda \ge 2\Delta x)$;
- Δx is the sampling interval.





4.4.3 Transmission characteristic of the short wave profile component

The transmission characteristic of the short wave profile component is complementary to the transmission characteristic of the long wave profile component. The short wave profile component is the difference between the surface profile and the long wave profile component. The filter characteristic for the short wave profile component (see Figure 3) has the following equation:

$$\frac{a_2}{a_0} = 1 - \frac{a_1}{a_0} = \left[4\beta\alpha^2 \sin^2\frac{\pi\Delta x}{\lambda} + 16(1-\beta)\alpha^4 \sin^4\frac{\pi\Delta x}{\lambda} \right] \left[1 + \beta\alpha^2 \sin^2\frac{\pi\Delta x}{\lambda} + 16(1-\beta)\alpha^4 \sin^4\frac{\pi\Delta x}{\lambda} \right]^{-1}$$
(9)

where

 a_2 is the amplitude of the sinusoidal profile short wave component.