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**Statistical methods in process
management — Capability and
performance —**

Part 2:

**Process capability and performance of
time-dependent process models**

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*Méthodes statistiques dans la gestion de processus — Aptitude et
performance —*

*Partie 2: Aptitude de processus et performance des modèles de
processus dépendants du temps*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2. www.iso.org/directives

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received. www.iso.org/patents

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The committee responsible for this document is ISO/TC 96, *Applications of statistical methods*, Subcommittee SC 4, *Applications of statistical methods in process management*.

This first edition of ISO 22514-2 cancels and replaces ISO 21747:2006, of which it constitutes a technical revision.

ISO 22514 consists of the following parts, under the general title *Statistical methods in process management — Capability and performance*: <http://www.iso.org/standards/catalog/standards/sist/889979f1-5c59-4d70-b9ff-aeba998ef2a8/sist-iso-22514-2-2014>

- *Part 1: General principles and concepts*
- *Part 2: Process capability and performance of time-dependent process models*
- *Part 3: Machine performance studies for measured data on discrete parts*
- *Part 4: Process capability estimates and performance measures*
- *Part 5: Process capability statistics for attribute characteristics*
- *Part 6: Process capability statistics for characteristics following a multivariate normal distribution*
- *Part 7: Capability of measurement processes*
- *Part 8: Machine performance of a multi-state production process*

This corrected version of ISO 22514-2:2013 incorporates the following corrections: in Table 3, rows 3 and 4, the formulae have been corrected by replacing “ $k \cdot n$ ” with “ k ” in the denominators.

Introduction

Many standards have been created concerning the quality capability/performance of processes by international, regional and national standardization bodies and also by industry. All of them assume that the process is in a state of statistical control, with stationary, normally distributed processes. However, a comprehensive analysis of production processes shows that, over time, it is very rare for processes to remain in such a state.

In recognition of this fact, this part of ISO 22514 provides a framework for estimating the quality capability/performance of industrial processes for an array of standard circumstances. These circumstances are categorized based on the stability of the mean and variance, as to whether they are constant, changing systematically, or changing randomly. As such, the quality capability/performance can be assessed for very differently shaped distributions with respect to time.

In other parts of ISO 22514 more detailed information about calculations of indices can be found. It should be noted that where the capability indices given in this part of ISO 22514 are computed they only form point estimates of their true values. It is therefore recommended that wherever possible the indices' confidence intervals are computed and reported.

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Statistical methods in process management — Capability and performance —

Part 2: Process capability and performance of time-dependent process models

1 Scope

This part of ISO 22514 describes a procedure for the determination of statistics for estimating the quality capability or performance of product and process characteristics. The process results of these quality characteristics are categorized into eight possible distribution types. Calculation formulae for the statistical measures are placed with every distribution.

The statistical methods described in this part of ISO 22514 only relate to continuous quality characteristics. They are applicable to processes in any industrial or economical sector.

NOTE This method is usually applied in case of a great number of serial process results, but it can also be used for small series (a small number of process results).

2 Normative references

The following documents, in whole or in part, are normatively referenced in this document and are indispensable for its application. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 3534-2, *Statistics — Vocabulary and symbols — Part 2: Applied statistics*

ISO 5479, *Statistical interpretation of data — Tests for departure from the normal distribution*

ISO 22514-1, *Statistical methods in process management — Capability and performance — Part 1: General principles and concepts*

3 Terms, definitions, symbols and abbreviated terms

For the purposes of this document, the terms and definitions given in ISO 3534-2 and ISO 22514-1, and the following symbols and abbreviated terms, apply.

3.1 Symbols

C_p	process capability index
C_{pk}	minimum process capability index
C_{pkL}	lower process capability index
C_{pkU}	upper process capability index
c_4	constant based on subgroup size n
Δ	dispersion of the process

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Δ_L	difference between X_{mid} and $X_{0,135\%}$ of the distribution of the product characteristic
Δ_U	difference between $X_{99,865\%}$ and X_{mid} of the distribution of the product characteristic
d_2	constant based on subgroup size n
k	number of subgroups of the same size n
μ	average location of the process
L	lower specification limit
$M_{l,d}$	Calculation methods with location method label l and dispersion method label d
N	sample size
p_L	lower fraction nonconforming
p_t	total fraction nonconforming
p_U	upper fraction nonconforming
P_p	process performance index
P_{pk}	minimum process performance index
P_{pkL}	lower process performance index
P_{pkU}	upper process performance index
R_i	range of the i th subgroup
s	standard deviation, realized value
σ	standard deviation, population
S	standard deviation, sample statistic
S_i	observed sample standard deviation of the i th subgroup
S_t	standard deviation, with the subscript "t" indicating total standard deviation
U	upper specification limit
$X_{0,135\%}$	0,135 % distribution quantile
$X_{99,865\%}$	99,865 % distribution quantile
$X_{50\%}$	50 % distribution quantile
X_{mid}	distribution midpoint

3.2 Abbreviations

ANOVA	analysis of variance
SPC	statistical process control

4 Process analysis

The purpose of process analysis is to obtain knowledge of a process. This knowledge is necessary for controlling the process efficiently and effectively so that the products realized by the process fulfil the quality requirement. It is a general assumption of this part of ISO 22514 that a process analysis has been carried out and subsequent process improvements have been implemented.

The behaviour of a characteristic under consideration can be described by the distribution, the location, the dispersion and the shape, parameters of which are time-dependent functions, in general. Different models of such resulting distributions the parameters of which are time-dependent functions are discussed in [Clauses 6](#) and [7](#). To indicate whether a time-dependent distribution model fits, statistical methods [e.g. estimating parameters, analysis of variance (ANOVA)] including graphical tools (e.g. probability plots, control charts) are used.

The values of the characteristics under consideration are typically determined on the basis of samples taken from the process flow. The sample size and frequency should be chosen depending on the type of process and the type of product so that all important changes are detected in time. The samples should be representative for the characteristic under consideration. To assess the stability of the process a control chart should be used. Information on the use of control charts can be found in ISO 7870-2.

5 Time-dependent distribution models

The instantaneous distribution characterizes the behaviour of the characteristic under investigation during a short interval. Usually, it is the time interval during which the sample (e.g. the subgroup) can be taken from the process. Observing the process continuously in time for a longer time interval the output from the process is called the resulting process distribution and it is described by a corresponding time-dependent distribution model that reflects

- the instantaneous distribution of the characteristic under consideration, and
- the changes of its location, dispersion and shape parameters during the time interval of process observation.

In practice, the resulting distribution can be represented by the whole data set, e.g. when SPC is applied, by all subgroups gained during the interval of the process observation.

Time-dependent distribution models can be classified into four groups according to whether the location and dispersion moments are constant or changing (see [Table 1](#)).

- a) A process whose location and dispersion are constant is in time-dependent distribution model A. In this case only, all the means and variances of the instantaneous distributions are equal to each other and they are equal to the resulting distribution.
- b) If the dispersion of a process is changing with time, but the location stays constant, the process is said to be in time-dependent distribution model B.
- c) If the dispersion is constant, but the location is changing, we have time-dependent distribution model C.
- d) Otherwise, we have time-dependent distribution model D.

Table 1 — Classification of time-dependent distribution models

Process-standard deviation $s(t)$	Process average $\mu(t)$			
	Constant		Not constant	
Constant	A		C	
	A1	A2	C1	C2
			C3	C4
Short time distribution	Normal distributed	Not normal distributed - unimodal	Random	Random
Short time distribution			Normal distributed	Systematic (e.g. trend)
Resulting distribution			Normal distributed	Normal distributed
Resulting distribution			Not normal distributed - unimodal	Any shape
Resulting distribution				Any shape
Not constant	B		D	
	Any shape - unimodal		Any shape	

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For changing moments, the models can be classified according to whether the changes are random, systematic or both.

NOTE Model A2 is known as *stationary* in time-series analysis literature and model A1 is known as *second order stationary*.

Table 2 summarizes the basic features of individual time-dependent distribution models; their graphical representations are given in Figures 1 to 8. There are subclasses of time-dependent distribution models A and C which are introduced due to their practical importance. They differ in the shape of the resulting distribution and in the cause of the process being in an out-of-control state.

Table 2 — Basic features of time-dependent distribution models

Characteristic	Time-dependent distribution models ^a							
	A1	A2	B	C1	C2	C3	C4	D
Location	c	c	c	r	r	s	s	S
Dispersion	c	c	s/r	c	c	c	c	s/r
Instantaneous distribution	nd	1m	nd	nd	nd	as	as	as
Resulting distribution	nd	1m	1m	nd	1m	as	as	as
Figure	1	2	3	4	5	6	7	8
Location/dispersion:								
c parameter remains constant								
r parameter changes randomly only								
s parameter changes systematically only								
Instantaneous/resulting distribution:								
nd normally distributed								
1m not normally distributed, one mode only								
as any shape								
^a The choice of the model is a result of process analysis.								

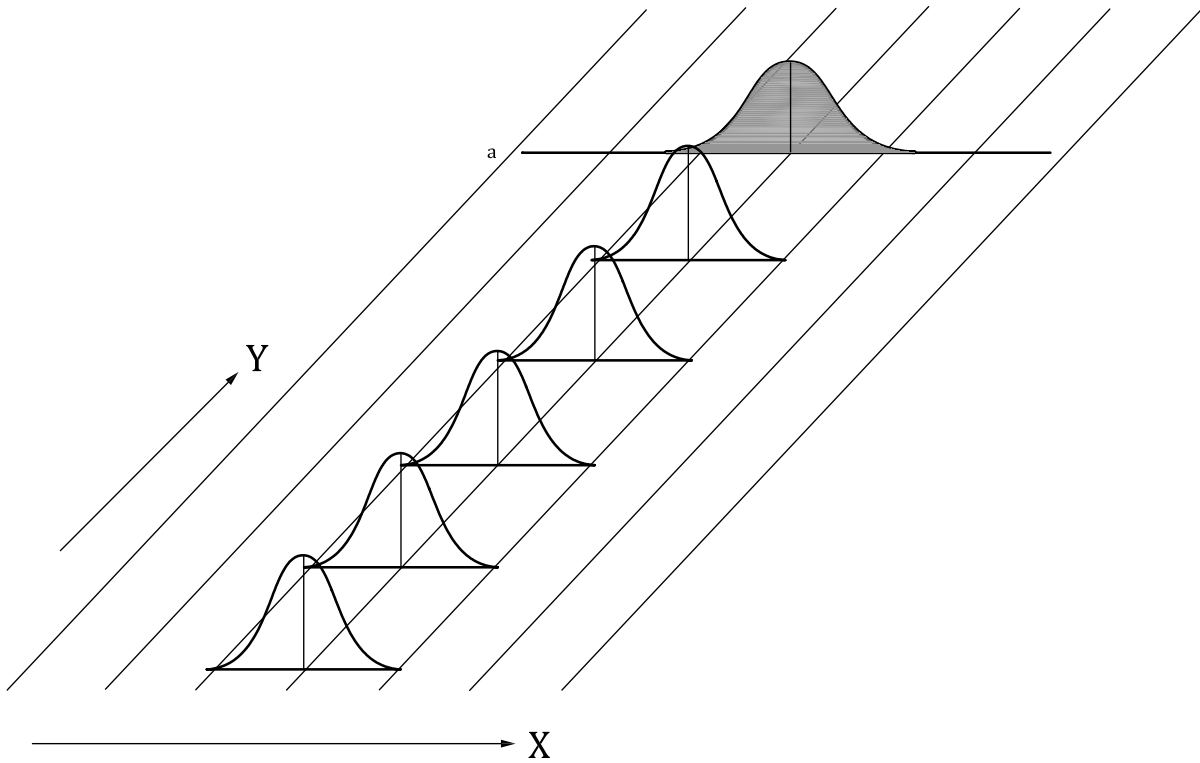
For each time-dependent distribution model, several instantaneous distributions are shown as a function of time; the related resulting distribution is shown as well. These distributions are not drawn to scale.

The choice of models and their verification requires extensive data analysis. This will usually require the use of statistical software.

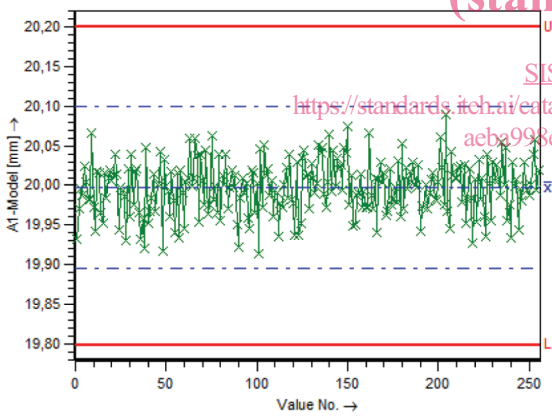
Time-dependent distribution model A1 (see Figure 1) has the following characteristics (e.g. the measured length of an item from a process in a state of statistical control):

- location: constant;
- dispersion: constant;
- instantaneous distribution: normally distributed;
- resulting distribution: normally distributed.

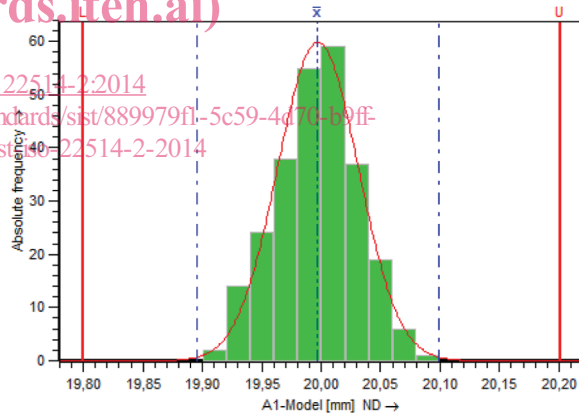
This process is under statistical control.



a) Time-dependent distribution model A1
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b) Example of run chart model A1



c) Example of histogram model A1

Key

X characteristic value

Y time

a Resulting distribution.

Figure 1 — Graphical representation of time-dependent distribution model A1

Time-dependent distribution model A2 (see [Figure 2](#)) has the following characteristics (e.g. the surface roughness of an item as an example for a physically limited characteristic):

- location: constant;
- dispersion: constant;
- instantaneous distribution: not normally distributed, unimodal;