



CYBER; Quantum-Safe Key Exchanges

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Contents

Intellectual Property Rights	6
Foreword.....	6
Modal verbs terminology.....	6
1 Scope	7
2 References	7
2.1 Normative references	7
2.2 Informative references.....	7
3 Abbreviations	13
4 Quantum-safe key exchanges	13
4.1 Introduction	13
4.2 Use cases	14
4.2.1 General comments	14
4.2.2 Network security.....	14
4.2.3 Internet of Things	14
4.3 Candidate primitives.....	14
5 Implementation considerations.....	15
5.1 Introduction	15
5.2 Active security.....	15
5.2.1 Invalid key attacks	15
5.2.2 Key validation.....	15
5.2.3 Performance impact	16
5.3 Side-channel protection.....	16
5.3.1 Side-channel vulnerabilities.....	16
5.3.2 Side-channel mitigations.....	16
5.3.3 Performance impact	16
6 Learning with Errors	17
6.1 Introduction	17
6.2 LWE key exchange	17
6.2.1 Overview	17
6.2.2 Public parameters.....	18
6.2.3 Key generation.....	18
6.2.4 Key extraction.....	18
6.2.5 Reconciliation.....	19
6.3 Ring-LWE key exchange	19
6.3.1 Overview	19
6.3.2 Public parameters.....	20
6.3.3 Key generation.....	21
6.3.4 Key extraction.....	21
6.3.5 Reconciliation.....	21
6.4 Implementation considerations.....	22
6.4.1 Active security	22
6.4.2 Side-channel protection	22
6.5 Parameter selection.....	22
6.5.1 LWE proposed parameters.....	22
6.5.2 Ring-LWE proposed parameters.....	23
6.5.3 Security estimates	23
6.6 Performance	23
6.6.1 Performance on a 64-bit processor	23
6.6.2 Performance on a 32-bit embedded processor	24
6.6.3 Performance on 32-bit microcontrollers	24
6.7 Summary	25
7 Supersingular isogenies.....	25

7.1	Introduction	25
7.2	SIDH key exchange	25
7.2.1	Overview	25
7.2.2	Public parameters	26
7.2.3	Key generation	26
7.2.4	Key exchange	27
7.3	Implementation considerations	27
7.3.1	Static key exchanges	27
7.3.2	Side-channel protection	28
7.4	Parameter selection	28
7.4.1	Proposed parameters	28
7.4.2	Security estimates	28
7.5	Performance	28
7.5.1	Performance on a 64-bit desktop processor	28
7.5.2	Performance on a 64-bit embedded processor	29
7.5.3	Performance on a 32-bit embedded processor	29
7.6	Summary	29
8	Key exchanges from key transport mechanisms	29
8.1	General construction	29
8.2	Niederreiter	30
8.2.1	Introduction	30
8.2.2	Niederreiter key exchange	30
8.2.2.1	Overview	30
8.2.2.2	Public parameters	31
8.2.2.3	Key generation	31
8.2.2.4	Decryption	32
8.2.3	Implementation considerations	32
8.2.3.1	Active attacks	32
8.2.3.2	Side-channel attacks	32
8.2.4	Parameter selection	32
8.2.4.1	Proposed parameters	32
8.2.4.2	Security estimates	33
8.2.5	Performance	33
8.2.5.1	Performance on a 64-bit server processor	33
8.2.5.2	Performance on a 64-bit desktop processor	33
8.2.5.3	Performance on an 8-bit microcontroller	33
8.2.6	Summary	34
8.3	NTRU	34
8.3.1	Introduction	34
8.3.2	NTRU key exchange	34
8.3.2.1	Overview	34
8.3.2.2	Public parameters	35
8.3.2.3	Decryption	35
8.3.3	Implementation considerations	35
8.3.3.1	Static key exchange	35
8.3.3.2	Side channel attacks	35
8.3.4	Parameter selection	36
8.3.4.1	Proposed parameters	36
8.3.4.2	Security estimates	36
8.3.5	Performance	36
8.3.5.1	Performance on a 64-bit desktop processor	36
8.3.5.2	Performance on a 32-bit embedded processor	36
8.3.5.3	Performance on a 32-bit microcontroller	37
8.3.6	Summary	37
9	Conclusions	37
Annex A:	LWE design and security considerations	39
A.1	LWE and Ring-LWE variants	39
A.1.1	Rings	39
A.1.2	Distributions	39

A.1.2.1	Discrete Gaussians	39
A.1.2.2	Approximate Gaussians	39
A.1.2.3	Small distributions	40
A.1.2.4	Learning with Rounding	40
A.1.3	Varying A	40
A.1.4	Reconciliation mechanisms	41
A.1.5	Key transport	41
A.2	Security considerations.....	42
A.2.1	Provable security	42
A.2.2	Passive security	42
A.2.3	Active security.....	43
Annex B:	SIDH background and security considerations.....	44
B.1	Mathematical background	44
B.1.1	Isogenies.....	44
B.1.2	Parameter generation	44
B.1.3	Public key compression.....	45
B.2	Security.....	45
B.2.1	Provable security	45
B.2.2	Passive security	46
B.2.3	Active security.....	46
Annex C:	Open Quantum-Safe benchmarks	48
C.1	Open Quantum-Safe	48
C.2	Benchmarks	48
C.2.1	Performance on a 64-bit desktop processor.....	48
C.2.2	Performance on a 64-bit laptop processor	49
C.2.3	Performance on a 32-bit embedded processor.....	49
C.3	Discussion	49
History	50

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Foreword

This Technical Report (TR) has been produced by ETSI Technical Committee Cyber Security (CYBER).

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1 Scope

The present document compares a selection of proposals for quantum-safe key exchanges taken from the academic literature. In particular, it includes key exchanges based on the Learning with Errors (LWE), Ring-LWE and Supersingular Isogeny Diffie-Hellman (SIDH) problems, as well as key exchanges constructed from the Niederreiter and NTRU key transport schemes.

The present document gives an overview of each key exchange, lists proposed parameters and gives software performance estimates on a range of processors. It also discusses various security and implementation considerations such as active attacks and side-channel vulnerabilities.

2 References

2.1 Normative references

Normative references are not applicable in the present document.

2.2 Informative references

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3 Abbreviations

For the purposes of the present document, the following abbreviations apply:

AES-NI	AES New Instructions
AMD	Advanced Micro Devices
ARM	Advanced RISC machine
AVX	Advanced Vector Extensions
BKZ	Block Korkine-Zolotarev algorithm
DH	Diffie-Hellman
DTLS	Datagram Transport Layer Security
ECDH	Elliptic Curve Diffie-Hellman
GF	Galois Field
IKE	Internet Key Exchange
IoT	Internet of Things
KDF	Key Derivation Function
KEM	Key Encapsulation Mechanism
LWE	Learning With Errors
LWR	Learning With Rounding
NTT	Number-Theoretic Transform
QKD	Quantum Key Distribution
QSC	Quantum-Safe Cryptography
RSA	Rivest-Shamir-Adleman protocol
SIDH	Supersingular Isogeny Diffie-Hellman
SSH	Secure Shell
TLS	Transport Layer Security
VoIP	Voice over Internet Protocol
VPN	Virtual Private Network

4 Quantum-safe key exchanges

4.1 Introduction

Key establishment is a public-key cryptographic primitive which allows two parties to set up a shared secret key. In a key exchange, the shared secret key is securely derived from information contributed by both parties; for example, by exchanging public keys with each other. The standard examples of a key exchange are Diffie-Hellman (DH) and Elliptic Curve Diffie-Hellman (ECDH). In a key transport mechanism one party generates the secret key and securely shares it with the second party; for example, by sending it encrypted under the second party's public key. The standard example of a key transport mechanism is RSA encryption.

DH, ECDH and RSA will all be made insecure by the development of large-scale fault-tolerant quantum computing. The present document discusses proposals in the academic literature for quantum-safe key exchange primitives that could be used directly to replace DH and ECDH. The present document also includes examples of key exchanges constructed from key transport mechanisms.

NOTE 1: Quantum-safe key transport mechanisms that could be used to replace RSA will be considered in a separate document.

NOTE 2: The present document only considers algorithmic key exchange mechanisms. Other mechanisms, based on Quantum Key Distribution (QKD), are considered in ETSI QKD GS 002 [i.1].

Key exchanges can either use short-term ephemeral keys or long-term static keys.

- In ephemeral key exchanges both parties generate new short-term public keys that are only used in a single exchange.