

Designation: E2555 – 07

### Standard Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection<sup>1</sup>

This standard is issued under the fixed designation E2555; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon ( $\varepsilon$ ) indicates an editorial change since the last revision or reapproval.

#### 1. Scope

1.1 This practice presents a procedure and related tables of factors for adapting Practice E2234 (equivalent to MIL-STD-105) sampling plans to acceptance sampling inspection when the item quality of interest is life length or reliability. Factors are provided for three alternative criteria for lot evaluation: mean life, hazard rate, and reliable life. Inspection of the sample is by attributes with testing truncated at the end of some prearranged period of time. The Weibull distribution, together with the exponential distribution as a special case, is used as the underlying statistical model.

1.2 A system of units is not specified by this practice.

1.3 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

#### 2. Referenced Documents

2.1 ASTM Standards:<sup>2</sup>

E456 Terminology Relating to Quality and Statistics E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

#### 3. Terminology

3.1 Definitions:

3.1.1 The terminology defined in Terminology E456 applies to this practice unless modified herein.

3.1.2 *acceptance quality level (AQL), n*—quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling. **E2234** 

3.1.2.1 *Discussion*—This term is often referred to as the "acceptance quality limit."

3.1.2.2 *Discussion*—This definition supersedes that given in MEL-STD-105E.

3.1.2.3 Discussion—A sampling plan and an AQL are chosen in accordance with the risk assumed. Use of a value of AQL for a certain defect or group of defects indicates that the sampling plan will accept the great majority of the lots or batches provided the process average level of percent defective (or defects per hundred units) in these lots or batches are no greater than the designated value of AQL. Thus, the AQL is a designated value of percent defective (or defects per hundred units) for which lots will be accepted most of the time by the sampling procedure being used. The sampling plans provided herein are so arranged that the probability of acceptance at the designated AQL value depends upon the sample size, being generally higher for large samples than for small ones, for a given AQL. The AQL alone does not identify the chances of accepting or rejecting individual lots or batches but more directly relates to what might be expected from a series of lots or batches, provided the steps indicated in this refer to the operating characteristic curve of the plan to determine the relative risks.

3.1.3 *consumer's risk*, *n*—probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan.

3.1.4 *double sampling plan*, *n*—a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot.

3.1.5 *limiting quality level (LQL), n*—quality level having a specified consumer's risk for a given sampling plan.

3.1.6 *lot*, *n*—a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes.

3.1.6.1 *Discussion*—The lot for sampling may differ from a collection of units designated as a batch for other purposes, for example, production, shipment, and so forth.

3.1.7 *multiple sampling plan*, *n*—a sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples.

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<sup>&</sup>lt;sup>1</sup> This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.30 on Statistical Quality Control.

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<sup>&</sup>lt;sup>2</sup> For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

3.1.7.1 *Discussion*—When the quality is much less or much more than the AQL, the decision can be made on the first sample, which is smaller than that of a single sampling plan with equivalent acceptance quality level. For samples that are close to the AQL in quality, additional samples are required and the total sample size will be larger than the corresponding single sampling plan.

3.1.8 *sample*, n—group of items, observations, test results, or portions of material taken from a large collection of items, observations, test results, or quantities of material that serves to provide information that may be used as a basis for making a decision concerning the larger collection. **E2234** 

3.2 Definitions of Terms Specific to This Standard:

3.2.1 *acceptance number*, *n*—the maximum number of failed items allowed in the sample for the lot to be accepted using a single or multiple sampling plan.

3.2.2 *hazard rate*, *n*—differential fraction of items failing at time *t* among those surviving up to time *t*, symbolized by h(t).

3.2.2.1 *Discussion*—h(t) is also referred to as the instantaneous failure rate at time *t*. It is related to the probability density and cumulative distribution functions by h(t) = f(t)/(1 - F(t)).

3.2.3 *mean life*, *n*—average time that items in the lot or population are expected to operate before failure.

3.2.3.1 *Discussion*—This metric is often referred to as mean time to failure (MTTF) or mean time before failure (MTBF).

3.2.4 *rejection number*, *n*—the minimum number of failed items in the sample that will cause the lot to be rejected under a given sampling plan.

3.2.5 *reliable life* ( $\rho_r$ ), *n*—life beyond which some specified proportion, *r*, of the items in the lot or population will survive.

3.2.6 *test truncation time* (t), *n*—amount of time sampled items are allowed to be tested.

3.2.7 *Weibull distribution*, *n*—probability distribution having cumulative distribution:

function 
$$F(t) = 1 - \exp\left(-\left(\frac{t-\gamma}{\eta}\right)^{\beta}\right), t > \gamma$$
 and probability density  
function  $f(t) = \frac{\beta}{\eta} \left(\frac{t-\gamma}{\eta}\right)^{\beta-1} \exp\left(-\left(\frac{t-\gamma}{\eta}\right)^{\beta}\right)$ 

3.2.7.1 *Discussion*—The Weibull distribution is widely used for modeling product life. It can take a wide variety of shapes and also the characteristics of other types of distributions based on the value of its parameters.  $\gamma$  is called the location, minimum life, or threshold parameter and defines the lower limit of the distribution (Fig. 1).  $\eta$  is called the scale or characteristic life parameter and is equal to the 63.2 percentile of the distribution, minus  $\gamma$  (Fig. 2).  $\beta$  is the shape parameter (Fig. 3). The exponential distribution is the special case where  $\gamma = 0$  and  $\beta = 1$ .

#### 4. Significance and Use

4.1 The procedure and tables presented in this practice are based on the use of the Weibull distribution in acceptance sampling inspection. Details of this work, together with tables of sampling plans of other forms, have been published previously. See Refs (1-3).<sup>3</sup> Since the basic computations required have already been made, it has been quite easy to provide these new factors. No changes in method or details of application have been made over those described in the publications referenced above. For this reason, the text portion of this report has been briefly written. Readers interested in further details

<sup>3</sup> The boldface numbers in parentheses refer to the list of references at the end of this standard.

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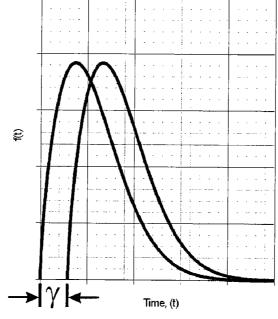


FIG. 1 Effect of the Parameter  $\gamma$  on the Weibull Probability Density Function, f(t)

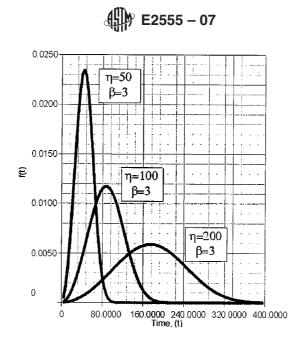
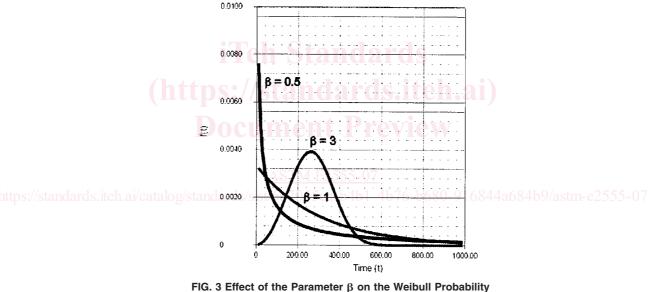


FIG. 2 Effect of the Parameter  $\eta$  on the Weibull Probability Density Function, *f*(*t*)



IG. 3 Effect of the Parameter  $\beta$  on the Weibull Probability Density Function, f(t)

are referred to these previous publications. Other sources of material on the underlying theory and approach are also available (4-7).

4.2 The procedure to be used is essentially the same as the one normally used for attribute sampling inspection. The only difference is that sample items are tested for life or survival instead of for some other property. For single sampling, the following are the required steps:

4.2.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234.

4.2.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.

4.2.3 Place the sample of items on life test for the specified period of time, t.

4.2.4 Determine the number of sample items that failed during the test period.

4.2.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.

4.2.6 If the number that failed is equal to or less than the acceptable number, accept the lot; if the number failing exceeds the acceptable number, reject the lot.

4.3 Both the sample sizes and the acceptance numbers used are those specified by Practice E2234 plans. It will be assumed in the section on examples that single sampling plans will be used. However, the matching double sampling and multiple sampling plans provided in MIL-STD-105 can be used if desired. The corresponding sample sizes and acceptance and rejection numbers are used in the usual way. The specified test truncation time, *t*, must be used for all samples.

4.4 The probability of acceptance for a lot under this procedure depends only on the probability of a sample item failing before the end of the test truncation time, *t*. For this reason, the actual life at failure need not be determined; only the number of items failing is of interest. Life requirements and test time specifications need not necessarily be measured in chronological terms such as minutes or hours. For example, the life measure may be cycles of operation, revolutions, or miles of travel.

4.5 The underlying life distribution assumed in this standard is the Weibull distribution (note that the exponential distribution is a special case of the Weibull). The Weibull model has three parameters. One parameter is a scale or characteristic life parameter. For these plans and procedures, the value for this parameter need not be known; the techniques used are independent of its magnitude. A second parameter is a location or "guaranteed life" parameter. In these plans and procedures, it is assumed that this parameter has a value of zero and that there is some risk of item failure right from the start of life. If this is not the case for some applications, a simple modification in procedure is available. The third parameter, and the one of importance, is the shape parameter,  $\beta$ .<sup>4</sup> The magnitude of the conversion factors used in the procedures described in this report depends directly on the value for this parameter. For this reason, the magnitude of the parameter shall be known through experience with the product or shall be estimated from past research, engineering, or inspection data. Estimation procedures are available and are outlined in Ref (1).

4.6 For the common case of random chance failures with the failure rate constant over time, rather than failures as a result of "infant mortality" or wearout, a value of 1 for the shape parameter shall be assumed. With this parameter value, the Weibull distribution reduces to the exponential. Tables of conversion factors are provided in Annex A1 for 15 selected shape parameter values ranging from  $\frac{1}{2}$  to 10, the range commonly encountered in industrial and technical practice. The value 1, used for the exponential case, is included. Factors for other required shape parameter values within this range may be obtained approximately by interpolation. A more complete discussion of the relationship between failure patterns and the Weibull parameters can be found in Refs (1-3).

4.7 One possible acceptance criterion is the mean life for items making up the lot ( $\mu$ ). Mean life conversion factors or values for the dimensionless ratio 100t/ $\mu$  have been determined to correspond to or replace all the *p*' or percent defective values associated with Practice E2234 plans. In this factor, *t* represents the specified test truncation time and  $\mu$  the mean item life for the lot. For reliability or life-length applications, these factors are used in place of the corresponding *p*' values normally used in the use of Practice E2234 plans for attribute inspection of other item qualities. The use of these factors will be demonstrated by several examples (see Sections 5, 7, and 9).

4.8 Annex Table 1A lists, for each selected shape parameter value,  $100t/\mu$  ratios for each of the Practice E2234 AQL [p'(%)] values. With acceptance inspection plans selected in

terms of these ratios, the probability of acceptance will be high for lots whose mean life meets the specified requirement. The actual probability of acceptance will vary from plan to plan and may be read from the associated operating characteristic curves supplied in MDL-STD-105. The curves are entered by using the corresponding p'(%) value. Annex Table 1B lists  $100t/\mu$ ratios at the LQL for the quality level at which the consumer's risk is 0.10. Annex Table 1C lists corresponding  $100t/\mu$  ratios for a consumer's risk of 0.05.

4.8.1 These ratios are to be used directly for the usual case for which the value for the Weibull location or threshold parameter ( $\gamma$ ) can be assumed as zero. If  $\gamma$  is not zero but has some other known value, all that shall be done is to subtract the value for  $\gamma$  from t to get  $t_0$  and from m to get  $m_0$ . These transformed values,  $t_0$  and  $m_0$ , are then employed in the use of the tables and for all other computations. A solution in terms of  $m_0$  and  $t_0$  can then be converted back to actual or absolute values by adding the value for  $\gamma$  to each.

#### 5. Examples, Mean Life Ratio

5.1 A Practice E2234 acceptance sampling inspection plan is to be applied to incoming lots of product for which the mean item life is the property of interest. An acceptable mean life of 2000 h has been specified, and under the plan, used lots with a mean life of this value or greater shall have a high probability of acceptance. A testing truncation time of t = 250 h has been specified. From past experience it has been determined that the Weibull distribution can be used as a life-length model and a shape parameter value of 2.5 and a location or threshold parameter value of 0 can be assumed. Single sampling is to be used. A sample of as many as 300 items or so can be tested at one time. An appropriate sampling inspection plan shall be selected. Also, the consumer's risk under use of the selected plan shall be determined.

5.1.1 Computation of the  $100t/\mu$  ratio at the AQL gives  $100t/\mu = 100 \times 250/2000 = 12.5$ . Examination of the ratios in the column for a shape parameter of 2.5 in Annex Table 1A discloses a value of 12.4 for an AQL of 0.40 in p'(%) terms. A plan with this AQL is accordingly to be used. Reference now to Practice E2234 indicates for Sample Size Code Letter M the sample size is 315; this value will accordingly be used. Examination of the Master Table for Normal Inspection (Single Sampling) in Practice E2234 shows for Sample Size Code Letter M and an AQL of 0.40, the acceptance number must be 3 and the rejection number 4.

5.1.2 The acceptance procedure will thus be to draw at random a sample of 315 items and submit them to life test for 250 h. At the end of that time, the number that has failed will be determined. If three items or less have failed, the lot will be accepted; if four or more have failed, it will be rejected.

5.1.3 The consumer's risk at a probability level of 0.10 can be determined by use of Annex Table 1B which gives  $100t/\mu$ ratios at the LQL for the 0.10 risk value. For a shape parameter value of 2.5, a Sample Size Code Letter M, and an AQL of 0.40, the  $100t/\mu$  ratio value is found to be 24. With t = 250,  $100t/\mu = 24$  or  $100 \times 250/\mu = 24$  which gives a value for  $\mu$  of 1040. Thus, if the mean life for the items in the lot is 1040 h or less, the probability of acceptance will be 0.10 or less. If the lot quality for which the consumer's risk was 0.05 was desired

 $<sup>^4</sup>$  In some disciplines, the Weibull shape  $\beta$  parameter is referred to as the "Weibull slope."

instead, Annex Table 1C might be used which gives ratios at the LQL for this risk value.

# 5.2 A Practice E2234 plan with Sample Size Code Letter F and an AQL of 4.0 has been specified for a product for which life length in terms of cycles of operation is the quality of interest. Acceptance is to be in terms of a mean life evaluation. The Weibull distribution can be assumed to apply with a shape parameter value and a location parameter value of 0. Testing of sample items is to be truncated at 5000 cycles. The operating characteristics in terms of mean life for this plan are required.

5.2.1 Annex Table 1A lists ratios of  $100t/\mu$  at selected AQLs and gives a  $100t/\mu$  value of 0.62 for an AQL of 4.0 and a shape parameter value of  $\frac{2}{3}$ . With t = 5000,  $100t/\mu = 0.62$  or  $100 \times 5000/\mu = 0.62$  which gives  $\mu = 810\ 000$ . Therefore, if the mean item life for the lot is 810 000 or more, the probability of acceptance will be high. Annex Table 1C gives ratios  $100t/\mu$  at the LQL for a consumer's risk of 0.05 and provides a  $100t/\mu$  value of 14 for Code Letter F, an AQL of 4.0, and a shape parameter value of  $\frac{2}{3}$ . Thus,  $100 \times 5000/\mu = 14$  or  $\mu = 36\ 000$ . If the mean item life for the lot is 36\ 000 cycles or less, the probability of acceptance will be 0.05 or less.

5.2.2 The sample size and acceptance number will be those specified by Practice E2234 for Code Letter F and an AQL of 4.0. For single sampling, the sample size will be 20 items and the acceptance number 2. For this example, as in all cases, the matched Practice E2234 double sampling and multiple sampling plans may be used instead. No additional changes in procedure are required. The specified test time, which in this case is 5000 cycles, shall be used for all samples.

5.3 Assume the Weibull distribution applies with a shape parameter value of  $\beta = 3.33$  and a location or threshold parameter value,  $\gamma$ , of 3000 h. A Practice E2234 acceptanceinspection plan shall be selected under which the probability of acceptance will be low (0.05 or less) if mean item life is 8000 h or less. The sample size will be kept large to reduce the testing period time but it cannot exceed 250 items. To reduce further testing time, an acceptance number of 0 will be used. The required test truncation time must be determined; also, the AQL.

5.3.1 Reference to Practice E2234 indicates the Code Letter L with a sample size of 200 items shall be used. With this code letter and an acceptance number of 0, the AQL in Practice E2234 terms must be 0.065. Subtraction of the threshold parameter value,  $\gamma$ , of 3000 h from the required mean value,  $\mu$ , of 8000 h gives as a converted value for the mean  $\mu_0 = 8000 - 3000 = 5000$  h. This converted value must now be used in working with the tables of factors. Use of Annex Table 1C for  $\beta = 3\frac{1}{3}$ . Code Letter L, and an AQL of 0.065 gives a 100 $t/\mu$  value of 31 at the LQL (for P(A) = 0.05). With  $\mu_0 = 5000$ ,  $100t_0/\mu_0 = 100 t_0/5000 = 31$  or  $t_0 = 1550$  h. Conversion of this to absolute terms gives  $t = t_0 + \gamma = 1550 + 3000 = 4550$  h as the required test truncation time.

5.3.2 From Annex Table 1A, the corresponding ratio at the AQL may be found. For an AQL of 0.065 and  $b = 3\frac{1}{3}$ , it is 12.3. Thus, 100  $t_0/\mu_0 = 12.3$  or  $100 \times 1550/\mu_0 = 12.3$  or  $\mu_0 = 12600$ . Converting this to absolute terms gives  $\mu = \mu_0 + \gamma = 12600 + 3000 = 15600$ . Thus, the mean item life for a lot shall be 15600 h or more for its probability of acceptance to be high.

#### 6. Hazard Rate Conversion Factors

6.1 Another measure of lot quality is the hazard rate or instantaneous failure rate, h(t), at some specified period of time, *t*. Hazard rate conversion factors or values for the dimensionless product  $100t\{h(t)\}$  have been determined for all of the *p*' values that characterize the collection of Practice E2234 plans. As for the mean life plans, these products may be used in place of the corresponding *p*' values when using the Practice E2234 plans for life-length and reliability applications.

6.2 Annex Table 2A lists for each selected value for the shape parameter  $100t\{h(t)\}$  products for each Practice E2234 AQL value. Annex Table 2B lists corresponding  $100t\{h(t)\}$  products at the LQL for a consumer's risk of 0.10. Annex Table 2C lists products at the LQL for a consumer's risk of 0.05. Use of these tables of factors is similar to the method of use for the mean life ratios including the variation in method required when some nonzero value for the location or threshold parameter shall be assumed.

6.2.1 Note one point of difference. The products are for direct application only in cases in which the time t at which the hazard rate is specified or is to be evaluated is the same as the time t at which the life testing of sample items is to be truncated. However, a table of hazard rate ratios has been prepared, Annex Table 2D, to use in a simple modification of method that allows the test truncation time to differ from the time at which the hazard rate is specified. All that shall be done is to determine the hazard rate at the test truncation time which corresponds to the hazard rate at the specification time. Annex Table 2D provides ratios for making this conversion. It gives for various values of  $t_2/t_1$  the corresponding values for the ratio  $h(t_2)/h(t_1)$  for all the shape parameter values for which conversion values have been provided. If the test truncation time is shorter than the time for hazard rate specification,  $t_1$  is used to represent the test truncation time and  $h(t_1)$  the corresponding hazard rate at that time. In this case,  $t_2$  represents the time of hazard rate specification and  $h(t_2)$  the specified hazard rate. If the test truncation is longer instead, the meanings given Subscripts 1 and 2 are simply reversed.

#### 7. Examples, Hazard Rate

7.1 An acceptance-inspection plan shall be selected from the Practice E2234 collection for an application for which the Weibull distribution applies and for which it may be assumed the shape parameter value is 1.67 and the location parameter value is 0. A hazard rate of no more than 0.0005/h at 1000 h of life can be tolerated so a plan under which the probability of acceptance will be low (0.10) if this rate will be exceeded at this life is required. The test truncation time is likewise to be 1000 h.

7.1.1 Computation of the  $100t\{h(t)\}$  product gives  $100 \times 1000 \times 0.0005 = 50$ . Thus, apian shall be used for which this product is found at the LQL for which the consumer's risk is 0.10. Examination of the column for  $\beta = 1.67$  in Annex Table 2B discloses several close possibilities. One is for a plan with Code Letter D and an AQL of 1.5 for which the product is 48; another is Code Letter F and an AQL of 4.0 for which the product is likewise 48; still another is Code Letter G and an

AQL of 6.5 for which the product is 53. Any of these will provide fairly closely the required consumer's protection.

7.1.2 The last plan mentioned with its relatively large sample size and acceptance number will discriminate most sharply between good and bad lots and hence provide the most reasonable AQL. This will be achieved at the expense of a relatively large number of item hours of inspection, of course. With this choice (Code Letter G and an AQL of 6.5) the AQL can be easily determined. Reference to Annex Table 2A gives a value for  $100t\{h(t)\}$  of 11.2 for an AQL of 6.5. Thus,  $100 \times 1000 \ h(t) = 11.2$  or  $h(t) = 0.000 \ 112$  at t = 1000; the "acceptable" hazard rate is therefore 0.000 112 (per hour). If, alternatively, Code Letter D and an AQL of 1.5 had been used, the "acceptable" hazard rate would be 0.000 025 2 (per hour) instead.

7.2 Suppose the selected sampling plan must have an acceptable hazard rate (a rate for which the probability of acceptance is high) of 0.0001 per hour at 500 h of life. However, the testing of sample items shall be truncated at 200 h. A value of  $\beta = 0.67$  and a location parameter of 0 can be assumed. A Practice E2234 plan shall be selected.

7.2.1 In this case, use Annex Table 2D. Letting  $t_2 = 500$  and  $t_1 = 200$ ,  $t_2/t_1 = 500/200 = 2.5$ . Referencing Annex Table 2D with this ratio using the value  $\beta = 0.67$  column shows  $h(t_2)/h(t_1)$  to be 0.734. With  $h(t_2) = 0.0001$ ,  $0.0001/h(t_1) = 0.734$  or  $h(t_1) = 0.000136$ . This failure rate number shall be used in selecting the plan. Thus,  $100t\{h(t)\} = 100 \times 200 \times 0.000136 = 2.72$  (note that the testing truncation time of 200 h is used as t at this point). Referencing Annex Table 2A examining the column for  $\beta = 0.67$  shows that a Practice E2234 plan with an AQL of 4.0 % precisely meets this need.

#### 8. Reliable Life Conversion Factors

8.1 A third possible reliability and life-length measure for the items in a lot or population is reliable life ( $\rho$ ). Reliable life can be defined as the life beyond which some specified proportion of the items in the lot or population will survive. The letter *r* represents this specified proportion.

8.1.1 Tables of conversion factors have been prepared for two different proportions, r = 0.90 and r = 0.99. As for the mean life case, these reliable life conversion factors have been prepared in the form of values for the dimensionless ratio 100t/p. Ratio values have been determined for all the p'(%)values associated with Practice E2234 plans. Annex Table 3A gives  $100t/\rho$  values at each of the AQLs for r = 0.90; Annex Table 4A gives corresponding values for r = 0.99. Annex Table 3B gives ratio values at the LQL for a consumer's risk of 0.10 for r = 0.90; Annex Table 4B gives corresponding values for a consumer's risk of 0.10 and r = 0.99. Annex Table 3C gives ratio values at the LQL for a consumer's risk of 0.05 and r = 0.90; Annex Table 4C gives similar ratio values at a consumer's risk of 0.05 and r = 0.99. These conversion ratios are used in the same manner in which mean life ratios are used, including the manner for application when the location parameter is not zero. See Section 9 for an example.

#### 9. Examples, Reliable Life

9.1 A sampling inspection plan shall be selected for a product for which item life in terms of feet of travel is the

quality of interest. Experience indicates the Weibull distribution will serve well as a statistical model with a shape parameter value of approximately  $1\frac{1}{3}$  and a location parameter of 0. A lot will be considered "acceptable" if the reliable life is 40 000 ft and the probability of acceptance for such lots shall be high. For lots in which reliable life is 10 000 ft or less, the probability of acceptance shall be low, namely 0.05 or less. Reliable life is defined as the life beyond which 90 % of the items will survive; that is, *r* is to be 0.90. Testing of sample items is to be truncated at 5000 ft.

9.1.1 At the AQL, the 100t/p factor is  $100 \times 5000/40\ 000 =$ 12.5. Examination of Annex Table 3A shows that for  $\beta = 1\frac{1}{3}$ , the 100t/p ratio for an AQL of 0.65 is 12.4 which is quite close to the desired ratio. Accordingly, a plan with this AQL is to be adopted. At the unacceptable or LQL, the  $100t/p_r$  factor is 100  $\times$  5000/10 000 = 50. Referencing Annex Table 3C, which gives ratios at the LQL for P(A) = 0.05, shows that, for Code Letter L, an AQL of 0.65 (which is required for this application, as indicated above) and  $\beta = 1\frac{1}{3}$  the corresponding ratio is 48, which is close to the desired value of 50. Thus, a Practice E2234 plan with Code Letter L and an AQL of 0.65 will meet the specified operating requirements. For single sampling, Practice E2234 shows the sample size to be 200 items and the acceptance number 3.

#### **10.** Summary

10.1 This practice preserves the structure of TR-7 for use in applications in which that standard is prescribed or its use is desirable.

10.2 This practice provides tables and procedures for applying three different measures of reliability in which testing is performed without replacement.

10.2.1 *Mean Life*,  $\mu$ —The expected life of the product.

10.2.2 Hazard Rate, h(t)—The instantaneous failure rate at some specified time, t.

10.2.3 *Reliable Life*,  $\rho_r$ —The life  $\rho$  beyond which some specified proportion *r* of the items in the population will survive.

10.3 Procedure for Application:

10.3.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234 for normal inspection.

10.3.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.

10.3.3 Place the sample of items on life test for the specified period of time, t.

10.3.4 Determine the number of sample items that failed during the test period.

10.3.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.

10.3.6 If the number that failed is equal to or less than the acceptance number, accept the lot; if the number failing exceeds the acceptance number, reject the lot.

10.4 Selection—Mean Life:

10.4.1 Specify:

10.4.1.1 Acceptable mean life,  $\mu_0$ .

10.4.1.2 Unacceptable mean life,  $\mu_1$ .

10.4.1.3 Test truncation time, t.

10.4.1.4 Weibull shape parameter,  $\beta$ .

10.4.2 Compute the dimensionless ratio  $100t/\mu_0$  from the specified  $\mu_0$  and *t* and enter Annex Table 1A under  $\beta$ . Locate the nearest value of  $100t/\mu_0$  to that calculated and read the corresponding AQL.

10.4.3 Compute the dimensionless ratio  $100t/\mu_1$  from the specified  $\mu_1$  and *t* and enter Annex Table 1B under  $\beta$ . Locate the nearest value of  $100t/\mu_1$  corresponding to the AQL obtained in 10.4.2 and read the sample size code letter (use Annex Table 1C if a limiting quality with 5 % probability of acceptance is desired).

10.4.4 Obtain the sample size and acceptance number for the test from the Practice E2234 normal inspection plan.

10.4.5 Mean Life Example:

10.4.5.1 Suppose  $\mu_0 = 50$ ,  $\mu_1 = 10$ , t = 5,  $\beta = 1$ , then  $100t/\mu_0 = 10$  giving an AQL of 10 from Annex Table 1A and  $100t/\mu_1 = 50$  giving Code F from Table 1B.

10.4.5.2 Practice E2234 gives sample size 20. Accept on 5 for Code F, AQL = 10.

10.5 Selection—Hazard Rate or Reliable Life:

10.5.1 The selection of plans for a specified hazard rate or reliable life follows the procedure for mean life described in 10.4 using appropriate dimensionless ratios and the associated tables from Annex A1.

10.5.2 Hazard rate uses the product  $100t\{h(t)\}$  with the Annex A1 tables of Section B.

10.5.3 Reliable life uses the dimensionless ratio  $100t/\rho$  with the Annex A1 tables of Section C.

#### 11. Keywords

11.1 exponential distribution; hazard rate; mean life; MIL-STD-105; reliability; reliable life; Weibull distribution

#### ANNEX

#### (Mandatory Information)

#### A1. TABLES OF CONVERSION FACTORS

#### TABLE 1A

100t/µ Ratios at the Acceptable Quality Level (normal inspection)

o for the ASTM E2234 Plans

NOTE 1—These plans assume the characteristic being measured has a Weibull distribution.

NOTE 2—Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

AQL	Shape Parameter, β														
p'(%)	0.333	0.500	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
0.010	1.67E-11	5.00E-07	7.52E-05	1.00E-02	0.109	0.239	0.446	1.128	2.831	5.198	7.031	7.999	11.033	17.262	41.847
0.015	5.63E-11	1.13E-06	1.38E-04	1.50E-02	0.147	0.313	0.568	1.382	3.330	5.950	7.940	8.981	12.210	18.720	43.578
0.025	2.61E-10	3.13E-06	2.97E-04	2.50E-02	0.216	0.440	0.772	1.784	4.085	7.055	9.255	10.393	13.873	20.734	45.863
0.040	1.07E-09	8.00E-06	6.02E-04	4.00E-02	0.308	0.601	1.024	2.257	4.930	8.252	10.657	11.887	15.603	22.778	48.070
0.065	4.58E-09	2.11E-05	1.25E-03	6.50E-02	0.443	0.831	1.370	2.877	5.986	9.702	12.328	13.656	17.617	25.101	50.462
0.100	1.67E-08	5.01E-05	2.38E-03	0.100	0.612	1.108	1.774	3.569	7.113	11.200	14.030	15.445	19.622	27.360	52.684
0.150	5.64E-08	1.13E-04	4.38E-03	0.150	0.830	1.452	2.263	4.372	8.366	12.822	15.845	17.344	21.716	29.673	54.866
0.250	2.61E-07	3.13E-04	9.42E-03	0.250	1.218	2.042	3.076	5.645	10.265	15.205	18.472	20.072	24.677	32.868	57.744
0.400	1.07E-06	8.03E-04	1.91E-02	0.401	1.733	2.795	4.080	7.144	12.391	17.788	21.274	22.962	27.759	36.113	60.527
0.650	4.62E-06	2.13E-03	3.96E-02	0.652	2.497	3.867	5.464	9.112	15.055	20.922	24.619	26.388	31.352	39.806	63.547
1.000	1.69E-05	5.05E-03	7.58E-02	1.005	3.454	5.159	7.083	11.312	17.899	24.167	28.031	29.859	34.932	43.402	66.356
1.500	5.75E-05	1.14E-02	0.140	1.511	4.690	6.771	9.047	13.872	21.071	27.687	31.680	33.551	38.683	47.092	69.119
2.500	2.70E-04	3.20E-02	0.303	2.532	6.906	9.551	12.330	17.954	25.901	32.883	36.983	38.879	44.008	52.211	72.778
4.000	1.13E-03	8.33E-02	0.620	4.082	9.882	13.133	16.422	22.798	31.355	38.559	42.682	44.565	49.591	57.446	76.339
6.500	5.06E-03	0.226	1.311	6.721	14.362	18.311	22.149	29.253	38.275	45.530	49.569	51.388	56.174	63.469	80.242
10.000	1.95E-02	0.555	2.573	10.536	20.122	24.711	29.007	36.626	45.816	52.891	56.726	58.431	62.856	69.441	83.932

## **E2555 – 07**

#### TABLE 1B

#### 100t/ $\mu$ Ratios at the Limiting Quality Level for the ASTM E2234 Plans, Consumer's Risk = 0.10

NOTE 1-These plans assume the characteristic being measured has a Weibull distribution.

Note 2—Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL															
Letter	(p%)	0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
A	6.500	25.433	66.274	92.927	115.129	120.933	121.682	121.789	121.073		117.369		115.707		112.025	
В	4.000	7.536	29.455	50.583	76.753	89.223 60.826	92.861	95.489	98.856 76.573	101.388	102.531	102.922	103.050	103.265	103.299	102.369
C C	2.500 10.000	1.628 11.235	10.604 38.440	23.509 61.762	46.052 87.681	98.590	66.059 101.478	70.282 103.429	105.659	82.650 106.932	86.478 107.183	88.298 107.115	89.056 107.045	90.885 106.759	93.267 106.086	97.271 103.741
D	1.500	0.397	4.142	11.616	28.782	42.756	48.289	53.012	60.537	68.485	73.938	76.686	77.865	80.809	84.899	92.805
D	6.500	2.361	13.587	28.313	52.129	66.752	71.750	75.709	81.469	86.852	90.126	91.644	92.267	93.745	95.608	98.484
D	10.000	7.688	29.850	51.091	77.265	89.669	93.274	95.871	99.185	101.658	102.759	103.128	103.247	103.437	103.437	102.437
Е	1.000	9.26E-02	1.569	5.608	17.712	29.707	34.937	39.615	47.489	56.397	62.890	66.292	67.780	71.573	77.043	88.407
Е	4.000	0.505	4.859	13.094	31.175	45.395	50.930	55.614	63.003	70.708	75.933	78.546	79.662	82.439	86.266	93.549
E	6.500	1.478	9.943	22.401	44.594	59.376	64.657	68.939	75.352	81.594	85.556	87.450	88.241	90.157	92.669	96.959
E	10.000	3.379	17.255	33.871	58.746	73.011	77.700	81.336	86.486	91.104	93.789	94.989	95.471	96.588	97.920	99.668
F F	0.650 2.500	2.54E-02 0.133	0.663 1.992	2.939 6.709	11.513 19.962	21.505 32.495	26.215 37.836	30.592 42.562	38.287 50.415	47.470 59.160	54.478 65.448	58.255 68.714	59.930 70.136	64.265 73.745	70.683 78.908	84.679 89.471
F	4.000	0.133	3.940	11.189	28.073	32.495 41.963	47.492	42.502 52.224	50.415 59.786	67.805	73.325	76.114	70.130	80.306	78.908 84.476	92.574
F	6.500	0.795	6.577	16.430	36.267	50.850	56.335	60.899	67.954	75.120	79.860	82.193	83.182	85.617	88.916	94.975
F	10.000	2.566	14.362	29.516	53.596	68.156	73.089	76.980	82.608	87.821	90.964	92.410	93.001	94.398	96.140	98.758
G	0.400	6.21E-03	0.259	1.452	7.196	15.117	19.164	23.075	30.268	39.334	46.578	50.594	52.399	57.141	64.341	80.792
G	1.500	3.14E-02	0.763	3.266	12.352	22.670	27.474	31.911	39.657	48.825	55.770	59.498	61.147	65.405	71.684	85.277
G	2.500	8.46E-02	1.476	5.358	17.183	29.038	34.237	38.900	46.773	55.716	62.257	65.691	67.194	71.032	76.576	88.139
G	4.000	0.176	2.407	7.730	21.939	34.879	40.294	45.043	52.852	61.437	67.540	70.688	72.053	75.506	80.412	90.319
G G	6.500 10.000	0.524 1.201	4.981 8.658	13.339 20.194	31.5 <mark>6</mark> 3 41.613	45.818 56.374	51.351 61.743	56.028 66.136	63.393 72.790	71.059 79.367	76.246 83.606	78.837 85.654	79.944 86.514	82.694 88.611	86.479 91.395	93.665 96.290
Н	0.250	1.63E-03	0.106	0.743	4.605	10.817	14.232	17.654	24.215	32.904	40.140	44.254	46.126	51.108	58.847	90.290 77.265
н	1.000	8.09E-03	0.309	1.657	7.859	16.150	20.324	24.329	31.633	40.747	47.967	51.950	53.737	58.414	65.486	81.507
Н	1.500	2.14E-02	0.590	2.694	10.865	20.592	25.223	29.548	37.194	46.384	53.437	57.252	58.947	63.342	69.869	84.191
н	2.500	4.36E-02	0.950	3.849	13.783	24.613	29.558	34.081	41.892	51.014	57.846	61.487	63.093	67.223	73.274	86.217
Н	4.000	0.125	1.912	6.505	19.555	31.996	37.320	42.039	49.898	58.675	65.000	68.290	69.724	73.366	78.583	89.286
Н	6.500	0.273	3.222	9.621	25.385	38.912	44.411	49.164	56.852	65.130	70.906	73.850	75.121	78.311	82.793	91.647
н	10.000	0.680	5.928	15.199	34.432	48.908	54.418	59.030	66.212	73.575	78.490	80.922	81.956	84.512	87.997	94.483
J J	0.150 0.650	3.97E-04 1.95E-03	4.14E-02 0.120	0.367 0.814	2.878 4.893	7.603 11.320	10.404 14.819	13.316 18.308	19.143 24.960	27.264 33.711	34.319 40.959	38.434 45.066	40.330 46.932	45.442 51.889	53.568 59.565	73.718 77.735
J	1.000	5.10E-03	0.120	1.316	4.893 6.738	14.390	18.342	22.183	29.290	38.314	40.959	49.606	40.932 51.425	56.210	63.501	80.262
hums	1.500	1.03E-02	0.362	1.868	8.513	17.147	21.436	25.523	32.9227	42.070	49.262	53.211	54.977	59.593	66.5417	82.161
J	2.500	2.86E-02	0.717	3.117	11.974	22.148	26.911	31.322	39.046	48.222	55.196	58.946	60.607	64.899	71.240	85.013
J	4.000	6.09E-02	1.186	4.547	15.403	26.752	31.830	36.430	44.285	53.332	60.029	63.571	65.128	69.116	74.920	87.180
J	6.500	0.145	2.119	7.025	20.584	33.251	38.618	43.353	51.194	59.891	66.120	69.349	70.753	74.312	79.393	89.745
J	10.000	0.354	3.832	10.956	27.682	41.525	47.051	51.787	59.369	67.426	72.984	75.795	77.003	80.026	84.240	92.444
K K	0.100 0.400	1.04E-04 5.08E-04	1.70E-02 4.88E-02	0.188 0.415	1.842	5.440	7.726	10.188	15.315	22.807 28.174	29.575	33.618	35.502	40.645	48.994 54.454	70.500
ĸ	0.400		4.88E-02 9.21E-02	0.415	3.124 4.292	8.086 10.261	10.989 13.580	13.988 16.925	19.945 23.378	28.174 31.991	35.270 39.210	39.392 43.330	41.287 45.209	46.384 50.217	54.454 58.025	74.325 76.724
ĸ	1.000	2.64E-03	0.146	0.947	5.410	12.206	15.845	19.445	26.246	35.094	42.354	46.445	48.299	53.208	60.774	78.520
К	1.500	7.24E-03	0.287	1.568	7.573	15.707	19.828	23.793	31.052	40.147	47.378	51.376	53.170	57.875	65.002	81.205
K	2.500	1.52E-02	0.470	2.270	9.692	18.900	23.373	27.590	35.129	44.311	51.439	55.323	57.054	61.558	68.290	83.234
К	4.000	3.54E-02	0.825	3.465	12.849	23.351	28.206	32.675	40.447	49.602	56.509	60.206	61.840	66.054	72.252	85.614
K	6.500	8.31E-02	1.459	5.312	17.084	28.913	34.105	38.765	46.638	55.588	62.137	65.577	67.084	70.929	76.488	88.088
K L	10.000 0.065	2.51E-01 2.54E-05	3.050 6.63E-03	9.234 9.29E-02	24.700 1.151	38.122 3.824	43.608 5.648	48.363 7.684	56.079 12.107	64.420 18.898	70.262 25.286	73.247 29.197	74.535 31.041	11.111 36.139	82.341 44.598	91.396 67.263
L		2.54E-05 1.24E-04		9.29E-02 0.205	1.950	5.677	5.048 8.025	10.541	15.756	23.331	30.141	29.197 34.196	36.083	41.226	44.598 49.553	70.902
L	0.400		3.58E-02	0.329	2.675	7.196	9.907	12.742	18.454	26.476	33.490	37.597	39.493	44.616	52.787	73.179
L	0.650		5.66E-02	0.465	3.366	8.550	11.548	14.627	20.701	29.026	36.156	40.281	42.174	47.255	55.271	74.880
L		1.73E-03	0.110	0.766	4.696	10.977	14.419	17.863	24.453	33.163	40.403	44.515	46.386	51.360	59.079	77.417
L	1.500	3.58E-03	0.179	1.103	5.991	13.176	16.961	20.673	27.619	36.556	43.819	47.889	49.728	54.583	62.027	79.325
L	2.500	8.23E-03	0.312	1.671	7.903	16.218	20.400	24.411	31.722	40.838	48.057	52.038	53.823	58.497	65.560	81.553
L	4.000	1.89E-02	0.544	2.536	10.435	19.977	24.552	28.840	36.450	45.640	52.722	56.562	58.270	62.705	69.307 74.416	83.851
L M	6.500 0.040	5.50E-02	1.109 2.67E-03	4.323 4.70E-02	14.892 0.731	26.083 2.720	31.122 4.172	35.699 5.851	43.544 9.647	52.617 15.758	59.357 21.733	62.931 25.477	64.503 27.263	68.535 32.259	74.416 40.725	86.887 64.276
M	0.040		2.67E-03 7.65E-03	4.70E-02 0.103	1.237	4.035	4.172 5.924	8.022	9.647 12.549	19.448	25.897	29.831	31.683	36.792	40.725	67.747
M	0.250		1.44E-02	0.166	1.695	5.111	7.309	9.692	14.691	22.061	28.766	32.789	34.668	39.808	48.185	69.916
М		1.61E-04		0.234	2.131	6.069	8.515	11.119	16.472	24.176	31.047	35.120	37.011	42.153	50.443	71.535
Μ	0.650	4.36E-04	4.40E-02	0.385	2.968	7.780	10.619	13.564	19.440	27.601	34.672	38.790	40.686	45.793	53.898	73.944
М	1.000		7.14E-02	0.553	3.779	9.326	12.474	15.679	21.935	30.402	37.580	41.706	43.593	48.643	56.566	75.753
М		2.05E-03	0.124	0.834	4.970	11.454	14.975	18.481	25.157	33.924	41.174	45.279	47.143	52.093	59.753	77.857
M	2.500	4.65E-03	0.214 0.429	1.257 2.120	6.537 9.260	14.066	17.975	21.782 26.846	28.849 34.338	37.852 43.511	45.110 50.664	49.157 54 572	50.981 56.316	55.785 60.861	63.117 67.671	80.019 82.856
М	4.000	1.32E-02	0.429	2.120	9.260	18.265	22.674	20.040	04.000	40.011	50.004	54.572	50.510	00.001	67.671	02.000

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TABLE Continued

Code	le AQL Shape Parameter, β															
Letter	(p%)	0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
N	0.025	1.63E-06	1.06E-03	2 35E-02	0.461	1.923	3.066	4.435	7.657	13.099	18.631	22.180	23.891	28.740	37.130	61.374
N	0.100		3.03E-03		0.779	2.852	4.352	6.078	9.957	16.162	22.197	25.965	27.760	32.774	41.243	64.684
N	0.150		5.69E-03		1.067	3.611	5.367	7.340	11.654	18.329	24.651	28.535	30.370	35.455	43.922	66.751
N	0.250	4.01E-05		0.117	1.340	4.286	6.250	8.418	13.063	20.082	26.600	30.558	32.418	37.538	45.974	68.293
N	0.400	1.08E-04		0.191	1.864	5.490	7.788	10.261	15.407	22.917	29.694	33.739	35.624	40.767	49.111	70.585
N	0.650	2.22E-04		0.275	2.371	6.574	9.142	11.853	17.374	25.229	32.171	36.262	38.156	43.292	51.530	72.302
N	1.000	5.03E-04		0.413	3.113	8.063	10.961	13.956	19.908	28.132	35.226	39.347	41.242	46.340	54.413	74.297
Ν	1.500		8.34E-02	0.621	4.083	9.883	13.135	16.425	22.801	31.358	38.562	42.685	44.568	49.594	57.448	76.341
Ν	2.500	3.18E-03	0.166	1.040	5.759	12.791	16.519	20.188	27.078	35.982	43.245	47.324	49.169	54.046	61.538	79.012
Р	0.015	3.97E-07	4.14E-04	1.16E-02	0.288	1.352	2.241	3.345	6.054	10.854	15.929	19.263	20.889	25.554	33.799	58.556
Р	0.065	1.92E-06	1.18E-03	2.55E-02	0.487	2.004	3.181	4.583	7.871	13.390	18.975	22.548	24.269	29.138	37.540	61.712
Р	0.100	4.93E-06	2.22E-03	4.09E-02	0.666	2.537	3.922	5.534	9.209	15.183	21.071	24.777	26.548	31.519	39.975	63.682
Р	0.150	9.76E-06	3.50E-03	5.76E-02	0.837	3.010	4.565	6.345	10.321	16.633	22.734	26.530	28.335	33.367	41.840	65.150
Р	0.250	2.62E-05	6.76E-03	9.43E-02	1.163	3.853	5.686	7.731	12.169	18.975	25.372	29.285	31.130	36.230	44.688	67.331
Р	0.400	5.38E-05	1.09E-02	0.135	1.478	4.612	6.671	8.926	13.717	20.883	27.481	31.468	33.336	38.467	46.882	68.964
Р	0.650	1.21E-04	1.88E-02	0.203	1.938	5.652	7.992	10.503	15.708	23.275	30.080	34.134	36.021	41.164	49.493	70.859
Р	1.000	2.73E-04	3.22E-02	0.304	2.538	6.919	9.567	12.349	17.977	25.928	32.911	37.012	38.908	44.037	52.238	72.797
Р	1.500	7.58E-04	6.37E-02	0.507	3.570	8.937	12.010	15.153	21.321	29.718	36.874	41.000	42.891	47.957	55.926	75.323
Q	0.010	1.04E-07	1.70E-04	5.95E-03	0.184	0.967	1.665	2.559	4.843	9.080	13.728	16.849	18.388	22.856	30.913	56.000
Q	0.040	5.03E-07	4.85E-04	1.31E-02	0.311	1.434	2.362	3.506	6.296	11.200	16.351	19.721	21.362	26.060	34.333	59.017
Q	0.065		9.08E-04		0.426	1.815	2.912	4.233	7.366	12.699	18.155	21.669	23.367	28.188	36.558	60.899
Q	0.100		1.43E-03		0.535	2.153	3.389	4.852	8.254	13.910	19.587	23.201	24.938	29.839	38.262	62.302
Q	0.150		2.76E-03		0.743	2.755	4.220	5.911	9.729	15.865	21.856	25.607	27.395	32.396	40.863	64.385
Q	0.250		4.46E-03	6.90E-02	0.944	3.296	4.949	6.823	10.965	17.458	23.670	27.512	29.332	34.392	42.865	65.943
Q	0.400	3.16E-05		0.104	1.237	4.037	5.926	8.025	12.552	19.452	25.902	29.836	31.688	36.797	45.247	67.751
Q	0.650	7.08E-05		0.155	1.619	4.939	7.090	9.430	14.359	21.661	28.332	32.343	34.219	39.356	47.747	69.597
Q	1.000	1.96E-04		0.258	2.274	6.371	8.891	11.560	17.015	24.812	31.726	35.811	37.704	42.842	51.101	72.001
R	0.025		1.89E-04		0.195	1.008	1.726	2.644	4.977	9.280	13.979	17.127	18.677	23.170	31.252	56.307
R	0.040		3.54E-04		0.266	1.275	2.128	3.192	5.822	10.521	15.521	18.818	20.429	25.061	33.276	58.102
R	0.065		5.59E-04		0.334	1.513	2.477	3.659	6.524	11.524	16.744	20.147	21.801	26.528	34.826	59.439
R	0.100				0.464	1.935	3.083	4.456	7.689	13.142	18.682	22.234	23.947	28.799	37.191	61.424
R	0.150		1.74E-03		0.590	2.315	3.615	<b>5</b> .143	8.664	14.460	20.230	23.886	25.638	30.571	39.011	62.909
R	0.250		2.98E-03		0.772	2.835	4.328	6.047	9.916	16.108	22.135	25.901	27.694	32.705	41.175	64.630
R	0.400		5.10E-03		1.010	3.466	5.176	7.104	11.340	17.934	24.206	28.072	29.901	34.975	43.445	66.388
R	0.650	4.74E-05	1.00E-02	0.127	1.417	4.468	6.486	8.703	13.430	20.533	27.097	31.071	32.936	38.062	46.487	68.673
						CIII	nen	τP	rat	ZIAV	V					

# Documer Fevrew TABLE 1C

## 100t/µ Ratios at the Limiting Quality Level for the MIL-STD-105D Plans, Consumer's Risk = 0.05

NOTE 1-These plans assume the characteristic being measured has a Weibull distribution.

NOTE 2—Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803).

Code	AQL (p%)		Shape Parameter, β														
Letter		0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000	
А	6.500	56.010	112.180	137.903	149.787	147.319	145.016	142.620	138.099	132.476	128.130	125.783	124.743	122.053	118.079	109.448	
В	4.000	16.596	49.858	75.065	99.858	108.690	110.668	111.822	112.758	112.642	111.932	111.377	111.097	110.287	108.881	105.099	
С	2.500	3.585	17.949	34.887	59.915	74.098	78.727	82.303	87.342	91.825	94.407	95.552	96.010	97.065	98.307	99.865	
С	10.000	20.487	57.375	83.403	107.122	114.568	115.972	116.634	116.787	115.851	114.582	113.748	113.349	112.240	110.421	105.839	
D	1.500	0.875	7.011	17.238	37.447	52.085	57.550	62.079	69.050	76.087	80.717	82.986	83.946	86.304	89.487	95.280	
D	6.500	4.291	20.235	38.169	63.616	77.505	81.937	85.317	89.999	94.053	96.312	97.286	97.669	98.530	99.493	100.465	
D	10.000	12.789	41.908	65.896	91.551	101.836	104.443	106.144	107.966	108.796	108.738	108.512	108.374	107.918	107.007	104.190	
E	1.000	0.204	2.655	8.322	23.044	36.189	41.637	46.391	54.167	62.657	68.656	71.738	73.072	76.440	81.206	90.764	
E	4.000	0.917	7.231	17.642	38.029	52.692	58.145	62.657	69.585	76.559	81.133	83.371	84.317	86.638	89.764	95.427	
E	6.500	2.450	13.929	28.845	52.780	67.376	72.346	76.274	81.976	87.284	90.500	91.986	92.594	94.036	95.845	98.607	
E	10.000	5.299	23.290	42.415	68.250	81.702	85.869	88.994	93.220	96.736	98.596	99.360	99.651	100.278	100.902	101.174	
F	0.650	5.60E-02	1.122	4.361	14.979	26.197	31.243	35.825	43.671	52.740	59.472	63.041	64.610	68.635	74.503	86.937	
F	2.500	0.241	2.964	9.038	24.348	37.714	43.193	47.949	55.679	64.052	69.927	72.932	74.231	77.499	82.105	91.265	
F	4.000	0.611	5.516	14.400	33.215	47.605	53.128	57.769	65.031	72.524	77.554	80.053	81.118	83.755	87.366	94.144	
F	6.500	1.244	8.866	20.555	42.108	56.876	62.232	66.607	73.221	79.743	83.936	85.959	86.807	88.873	91.612	96.404	
F	10.000	3.747	18.486	35.667	60.804	74.921	79.504	83.034	87.987	92.368	94.871	95.975	96.415	97.423	98.597	100.012	
G	0.400	1.37E-02	0.438	2.155	9.362	18.415	22.839	27.022	34.525	43.701	50.848	54.750	56.491	61.026	67.818	82.946	
G	1.500	5.70E-02	1.135	4.399	15.065	26.310	31.363	35.948	43.796	52.861	59.586	63.149	64.716	68.734	74.588	86.987	
G	2.500	0.140	2.066	6.894	20.327	32.939	38.296	43.027	50.874	59.591	65.844	69.088	70.500	74.079	79.194	89.633	
G	4.000	0.275	3.242	9.667	25.466	39.005	44.504	49.257	56.942	65.212	70.981	73.921	75.189	78.373	82.845	91.676	
G	6.500	0.764	6.404	16.105	35.788	50.345	55.837	60.414	67.503	74.721	79.507	81.865	82.866	85.332	88.680	94.849	
G	10.000	1.676	10.814	23.857	46.505	61.275	66.492	70.697	76.950	82.975	86.761	88.559	89.306	91.108	93.450	97.367	
Н	0.250	3.58E-03	0.179	1.103	5.991	13.177	16.961	20.674	27.620	36.556	43.820	47.889	49.728	54.584	62.027	79.325	

# €2555 – 07

TABLE Continued

Codo	101							Shape	Paramete	er. ß						
Code Letter	AQL (p%)	0 222	0.50	0.667	1 000	1 222	1 500	•			2 000	2 2 2 2 2	2 500	4 000	E 000	10.000
	(0, 0)	0.333	0.50	0.667	1.000	1.333	1.500	1.667	2.000	2.500	3.000	3.333	3.500	4.000	5.000	10.000
Н	1.000	1.47E-02	0.459	2.232	9.585	18.743	23.200	27.406	34.934	44.114	51.249	55.138	56.873	61.387	68.139	83.141
Н	1.500	3.54E-02 6.82E-02	0.826	3.466	12.853	23.357 27.523	28.212 32.644	32.682	40.454	49.608	56.515	60.212	61.846	66.059	72.257	85.617
H H	2.500 4.000	0.182	1.280 2.457	4.813 7.852	15.998 22.169	35.153	32.644 40.575	37.268 45.325	45.132 53.128	54.147 61.694	60.792 67.775	64.298 70.909	65.837 72.268	69.774 75.703	75.490 80.580	87.512 90.413
Н	6.500	0.380	4.022	11.361	28.360	42.285	47.816	43.323 52.544	60.091	68.082	73.575	76.347	77.537	80.511	84.649	92.668
Н	10.000	0.909	7.190	17.566	37.921	52.579	58.034	62.550	69.485	76.471	81.056	83.300	84.248	86.576	89.712	95.400
J	0.150	8.75E-04	7.01E-02	0.545	3.745	9.262	12.399	15.594	21.835	30.291	37.465	41.591	43.479	48.532	56.462	75.683
J	0.650	3.54E-03	0.178	1.097	5.967	13.137	16.916	20.624	27.564	36.497	43.761	47.832	49.671	54.529	61.978	79.294
J	1.000	8.44E-03	0.318	1.693	7.970	16.322	20.516	24.535	31.856	40.977	48.193	52.170	53.953	58.621	65.671	81.622
J J	1.500 2.500	1.61E-02 4.17E-02	0.488 0.921	2.336 3.762	9.880 13.573	19.174 24.332	23.674 29.257	27.909 33.769	35.467 41.572	44.653 50.702	51.770 57.551	55.642 61.205	57.367 62.817	61.854 66.966	68.553 73.049	83.394 86.085
J	2.500 4.000	4.17E-02 8.49E-02	1.480	5.369	17.206	29.068	29.257 34.268	38.932	46.805	55.747	62.285	65.718	67.221	71.056	76.597	88.151
J	6.500	0.194	2.569	8.117	22.665	35.741	41.179	45.932	53.720	62.243	68.277	71.382	72.727	76.123	80.937	90.614
J	10.000	0.455	4.532	12.427	30.107	44.223	49.760	54.462	61.914	69.729	75.055	77.728	78.873	81.723	85.666	93.224
К	0.100	2.29E-04		0.279	2.397	6.627	9.208	11.930	17.468	25.339	32.287	36.380	38.274	43.409	51.641	72.380
K	0.400	9.22E-04		0.560	3.810	9.384	12.543	15.757	22.026	30.503	37.683	41.809	43.696	48.744	56.659	75.815
K	0.650	2.18E-03	0.129	0.861	5.078	11.638	15.189	18.719	25.426	34.214	41.468	45.570	47.431	52.371	60.008	78.023
K K	1.000 1.500	4.13E-03 1.05E-02	0.197 0.368	1.184 1.892	6.279 8.584	13.648 17.256	17.499 21.556	21.263 25.652	28.275 33.060	37.248 42.211	44.510 49.400	48.567 53.344	50.399 55.109	55.227 59.718	62.612 66.653	79.698 82.230
ĸ	2.500	2.11E-02	0.586	2.680	10.826	20.536	25.162	29.484	37.127	46.317	53.373	57.190	58.887	63.285	69.819	84.160
ĸ	4.000	4.72E-02	1.001	4.003	14.147	25.099	30.075	34.618	42.441	51.548	58.351	61.970	63.564	67.662	73.656	86.442
K	6.500	1.07E-01	1.726	6.023	18.577	30.789	36.065	40.765	48.635	57.483	63.898	67.247	68.710	72.431	77.781	88.830
K		3.10E-01	3.513	10.265	26.505	40.193	45.708	50.454	58.093	66.264	71.934	74.813	76.053	79.161	83.511	92.043
L	0.065	5.60E-05		0.138	1.498	4.659	6.731	8.999	13.810	20.996	27.605	31.595	33.465	38.596	47.008	69.057
L	0.250 0.400	2.24E-04 5.28E-04		0.276	2.378	6.589	9.160	11.874 14.094	17.400	25.259	32.203	36.294	38.189 41.435	43.324	51.560	72.323
L	0.400	9.93E-04		0.423 0.581	3.164 3.906	8.162 9.560	11.081 12.753	14.094 15.994	20.071 22.302	28.316 30.807	35.418 37.997	39.540 42.122	41.435 44.007	46.530 49.048	54.591 56.942	74.418 76.004
L	1.000	2.51E-03	0.142	0.924	5.324	12.059	15.676	19.258	26.035	34.868	42.127	46.221	48.077	52.994	60.578	78.393
L	1.500	5.00E-03	0.224	1.302	6.692	14.316	18.259	22.092	29.191	38.210	45.466	49.505	51.325	56.114	63.415	80.208
L	2.500	1.10E-02	0.379	1.931	8.701	17.432	21.752	25.861	33.285	42.441	49.623	53.562	55.323	59.920	66.834	82.341
L	4.000	2.43E-02	0.644	2.875	11.347	21.272	25.963	30.327	38.010	47.195	54.215	58.002	59.682	64.032	70.478	84.556
L	6.500	6.80E-02	1.277	4.805	15.979	27.499	32.618	37.241	45.105	54.121	60.768	64.275	65.814	69.753	75.472	87.501
M M	0.040 0.150		4.52E-03 1.14E-02	6.98E-02 0.139	0.951	3.314 4.683	4.972 6.763	6.852 9.037	11.004 13.858	17.508 21.055	23.726 27.669	27.570 31.662	29.391 33.532	34.453 38.664	42.926 47.074	65.990 69.105
M	0.250	1.34E-04		0.139	2.005	5.798	8.176	10.719	15.978	23.594	30.423	34.484	36.372	41.515	49.831	71.100
M	0.400	2.52E-04		0.293	2.473	6.786	9.403	12.158	17.746	25.660	32.628	36.725	38.620	43.752	51.968	72.608
М	0.650	6.35E-04	5.66E-02	0.464	3.364	8.547	11.544	14.623	20.697	29.021	36.151	40.276	42.169	47.250	55.266	74.877
Μ	1.000	1.25E-03		0.652	4.221	10.133	13.429	16.756	23.183	31.778	38.991	43.113	44.993	50.008	57.831	76.595
M	1.500	2.73E-03	0.150	0.963	5.472	12.311	15.967	19.580	26.396	35.255	42.516	46.605	48.457	53.361	60.913	78.610
M	2.500 4.000	5.98E-03	0.253	1.425	7.108	14.978	19.007	22.905	30.083	39.142	46.387	50.408	52.216	56.965	64.183	80.692
M	4.000 0.025	1.63E-02	0.494 1.79E-03	2.356 3.49E-02	9.936 0.599	19.256	23.764 3.654	28.005 5.193	35.568 8.734	44.754	51.868 20.339	55.737 24.002	57.461 25.757	61.942 30.695	68.631 39.137	83.441 63.010
N	0.100		4.51E-03		0.950	3.310	4.968	6.846	10.996	17.498	23.715	27.559	29.380	34.441	42.914	65.981
Ν	0.150	3.35E-05		0.107	1.262	4.096	6.003	8.118	12.674	19.603	26.070	30.010	31.864	36.976	45.422	67.882
N	0.250		1.21E-02	0.146	1.555	4.792	6.902	9.205	14.073	21.315	27.954	31.955	33.827	38.962	47.364	69.318
N	0.400	1.57E-04		0.231	2.113	6.031	8.467	11.063	16.403	24.095	30.960	35.032	36.923	42.064	50.358	71.475
N	0.650		3.51E-02	0.324	2.648	7.143	9.842	12.667	18.363	26.371	33.379	37.486	39.382	44.506 47.468	52.683	73.106
N N		6.71E-04 1.46E-03		0.477 0.704	3.427 4.440	8.666 10.524	11.687 13.889	14.786 17.271	20.888 23.776	29.235 32.426	36.374 39.653	40.499 43.771	42.392 45.647	47.468 50.643	55.470 58.419	75.015 76.983
N		3.93E-03		1.155	6.179	13.485	17.313	21.060	28.049	37.010	44.272	48.334	50.168	55.006	62.411	79.570
P		8.75E-07			0.374	1.647	2.671	3.917	6.905	12.059	17.390	20.845	22.520	27.292	35.625	60.117
Р		3.48E-06			0.593	2.326	3.631	5.163	8.692	14.497	20.274	23.932	25.685	30.620	39.061	62.949
Р		8.15E-06			0.788	2.878	4.386	6.121	10.016	16.239	22.284	26.057	27.854	32.870	41.341	64.760
P		1.53E-05			0.971	3.366	5.042	6.938	11.119	17.654	23.891	27.743	29.567	34.633	43.105	66.128
P	0.250	3.82E-05		0.114	1.318	4.233	6.182	8.335	12.956	19.950	26.454	30.407	32.265	37.383	45.822	68.180
P P	0.400 0.650	7.50E-05 1.62E-04		0.160 0.234	1.651 2.134	5.011 6.074	7.182 8.522	9.539 11.127	14.498 16.482	21.828 24.188	28.514 31.060	32.530 35.133	34.407 37.024	39.546 42.166	47.931 50.455	69.731 71.544
P		3.50E-04		0.234	2.134	7.368	0.522 10.117	12.985	18.746	26.811	33.843	37.954	39.850	44.968	50.455 53.120	73.409
P		9.37E-04		0.564	3.831	9.421	12.588	15.807	22.085	30.567	37.750	41.876	43.762	48.809	56.719	75.855
Q		2.29E-07			0.240	1.179	1.984	2.997	5.524	10.088	14.986	18.233	19.824	24.411	32.583	57.493
Q		9.12E-07			0.380	1.664	2.696	3.949	6.953	12.126	17.470	20.931	22.609	27.386	35.724	60.200
Q		2.13E-06			0.504	2.058	3.257	4.682	8.011	13.581	19.201	22.789	24.516	29.397	37.807	61.931
Q	0.100		1.93E-03		0.621	2.407	3.743	5.306	8.892	14.764	20.584	24.261	26.022	30.971	39.419	63.237
Q Q	0.150 0.250	9.98E-06 1.96E-05	3.55E-03		0.843 1.055	3.026 3.581	4.587 5.328	6.373 7.291	10.359 11.589	16.681 18.248	22.789 24.559	26.588 28.440	28.394 30.274	33.427 35.357	41.900 43.824	65.197 66.677
Q		4.22E-05		0.120	1.362	4.339	5.328 6.319	8.501	13.171	20.215	24.559	28.440 30.710	30.274	37.693	45.624	68.406
Q		9.10E-05		0.120	1.761	5.259	7.497	9.916	14.973	22.399	29.134	33.166	35.047	40.189	48.553	70.183
Q		2.42E-04		0.287	2.440	6.717	9.318	12.059	17.625	25.520	32.480	36.575	38.470	43.603	51.826	72.509
R	0.025	2.23E-07	2.81E-04	8.69E-03	0.237	1.170	1.970	2.979	5.496	10.047	14.936	18.178	19.767	24.349	32.518	57.435
R		5.21E-07			0.315	1.447	2.380	3.531	6.332	11.252	16.415	19.790	21.433	26.136	34.413	59.086
R		9.73E-07			0.388	1.691	2.735	4.001	7.028	12.231	17.596	21.068	22.749	27.535	35.879	60.331
R		2.43E-06			0.526	2.126	3.352	4.804	8.186	13.818	19.479	23.086	24.820	29.716	38.135	62.199
R	0.150	4.76E-06	2.1/E-03	4.02E-02	0.659	2.515	3.892	5.496	9.157	15.114	20.991	24.692	26.462	31.429	39.884	63.609