# Standard Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection ${ }^{1}$ 


#### Abstract

This standard is issued under the fixed designation E2555; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon $(\varepsilon)$ indicates an editorial change since the last revision or reapproval.


## 1. Scope

1.1 This practice presents a procedure and related tables of factors for adapting Practice E2234 (equivalent to MIL-STD105) sampling plans to acceptance sampling inspection when the item quality of interest is life length or reliability. Factors are provided for three alternative criteria for lot evaluation: mean life, hazard rate, and reliable life. Inspection of the sample is by attributes with testing truncated at the end of some prearranged period of time. The Weibull distribution, together with the exponential distribution as a special case, is used as the underlying statistical model.
1.2 A system of units is not specified by this practice.
1.3 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

## 2. Referenced Documents

### 2.1 ASTM Standards: ${ }^{2}$

E456 Terminology Relating to Quality and Statistics
E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

## 3. Terminology

### 3.1 Definitions:

3.1.1 The terminology defined in Terminology E456 applies to this practice unless modified herein.
3.1.2 acceptance quality level ( $A Q L$ ), $n$-quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling.

E2234
3.1.2.1 Discussion-This term is often referred to as the "acceptance quality limit."

[^0]3.1.2.2 Discussion-This definition supersedes that given in MEL-STD-105E.
3.1.2.3 Discussion-A sampling plan and an AQL are chosen in accordance with the risk assumed. Use of a value of AQL for a certain defect or group of defects indicates that the sampling plan will accept the great majority of the lots or batches provided the process average level of percent defective (or defects per hundred units) in these lots or batches are no greater than the designated value of AQL. Thus, the AQL is a designated value of percent defective (or defects per hundred units) for which lots will be accepted most of the time by the sampling procedure being used. The sampling plans provided herein are so arranged that the probability of acceptance at the designated AQL value depends upon the sample size, being generally higher for large samples than for small ones, for a given AQL. The AQL alone does not identify the chances of accepting or rejecting individual lots or batches but more directly relates to what might be expected from a series of lots or batches, provided the steps indicated in this refer to the operating characteristic curve of the plan to determine the relative risks.
3.1.3 consumer's risk, n-probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan.
3.1.4 double sampling plan, $n$-a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot.
3.1.5 limiting quality level ( $L Q L$ ), $n$-quality level having a specified consumer's risk for a given sampling plan.
3.1.6 lot, $n$-a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes.
3.1.6.1 Discussion-The lot for sampling may differ from a collection of units designated as a batch for other purposes, for example, production, shipment, and so forth.
3.1.7 multiple sampling plan, $n-a$ sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples.
3.1.7.1 Discussion-When the quality is much less or much more than the AQL, the decision can be made on the first sample, which is smaller than that of a single sampling plan with equivalent acceptance quality level. For samples that are close to the AQL in quality, additional samples are required and the total sample size will be larger than the corresponding single sampling plan.
3.1.8 sample, $n$-group of items, observations, test results, or portions of material taken from a large collection of items, observations, test results, or quantities of material that serves to provide information that may be used as a basis for making a decision concerning the larger collection.

E2234

### 3.2 Definitions of Terms Specific to This Standard:

3.2.1 acceptance number, $n$-the maximum number of failed items allowed in the sample for the lot to be accepted using a single or multiple sampling plan.
3.2.2 hazard rate, $n$-differential fraction of items failing at time $t$ among those surviving up to time $t$, symbolized by $h(t)$.
3.2.2.1 Discussion- $h(t)$ is also referred to as the instantaneous failure rate at time $t$. It is related to the probability density and cumulative distribution functions by $h(t)=f(t)$ / $(1-F(t))$.
3.2.3 mean life, $n$-average time that items in the lot or population are expected to operate before failure.
3.2.3.1 Discussion-This metric is often referred to as mean time to failure (MTTF) or mean time before failure (MTBF).
3.2.4 rejection number, $n$-the minimum number of failed items in the sample that will cause the lot to be rejected under a given sampling plan.
3.2.5 reliable life $\left(\rho_{r}\right)$, $n$-life beyond which some specified proportion, $r$, of the items in the lot or population will survive.
3.2.6 test truncation time ( $t$ ), $n$-amount of time sampled items are allowed to be tested.
3.2.7 Weibull distribution, $n$-probability distribution having cumulative distribution:
function $F(t)=1-\exp \left(-\left(\frac{t-\gamma}{\eta}\right)^{\beta}\right), t>\gamma$ and probability density

$$
\text { function } f(t)=\frac{\beta}{\eta}\left(\frac{t-\gamma}{\eta}\right)^{\beta-1} \exp \left(-\left(\frac{t-\gamma}{\eta}\right)^{\beta}\right)
$$

3.2.7.1 Discussion-The Weibull distribution is widely used for modeling product life. It can take a wide variety of shapes and also the characteristics of other types of distributions based on the value of its parameters. $\gamma$ is called the location, minimum life, or threshold parameter and defines the lower limit of the distribution (Fig. 1). $\eta$ is called the scale or characteristic life parameter and is equal to the 63.2 percentile of the distribution, minus $\gamma$ (Fig. 2). $\beta$ is the shape parameter (Fig. 3). The exponential distribution is the special case where $\gamma=0$ and $\beta=1$.

## 4. Significance and Use

4.1 The procedure and tables presented in this practice are based on the use of the Weibull distribution in acceptance sampling inspection. Details of this work, together with tables of sampling plans of other forms, have been published previously. See Refs (1-3). ${ }^{3}$ Since the basic computations required have already been made, it has been quite easy to provide these new factors. No changes in method or details of application have been made over those described in the publications referenced above. For this reason, the text portion of this report has been briefly written. Readers interested in further details

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FIG. 1 Effect of the Parameter $\gamma$ on the Weibull Probability Density Function, $f(t)$


FIG. 2 Effect of the Parameter $\eta$ on the Weibull Probability Density Function, $f(t)$


FIG. 3 Effect of the Parameter $\beta$ on the Weibull Probability Density Function, $f(t)$
are referred to these previous publications. Other sources of material on the underlying theory and approach are also available (4-7).
4.2 The procedure to be used is essentially the same as the one normally used for attribute sampling inspection. The only difference is that sample items are tested for life or survival instead of for some other property. For single sampling, the following are the required steps:
4.2.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234.
4.2.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.
4.2.3 Place the sample of items on life test for the specified period of time, $t$.
4.2.4 Determine the number of sample items that failed during the test period.
4.2.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.
4.2.6 If the number that failed is equal to or less than the acceptable number, accept the lot; if the number failing exceeds the acceptable number, reject the lot.
4.3 Both the sample sizes and the acceptance numbers used are those specified by Practice E2234 plans. It will be assumed in the section on examples that single sampling plans will be used. However, the matching double sampling and multiple sampling plans provided in MIL-STD-105 can be used if desired. The corresponding sample sizes and acceptance and rejection numbers are used in the usual way. The specified test truncation time, $t$, must be used for all samples.
4.4 The probability of acceptance for a lot under this procedure depends only on the probability of a sample item failing before the end of the test truncation time, $t$. For this reason, the actual life at failure need not be determined; only the number of items failing is of interest. Life requirements and test time specifications need not necessarily be measured in chronological terms such as minutes or hours. For example, the life measure may be cycles of operation, revolutions, or miles of travel.
4.5 The underlying life distribution assumed in this standard is the Weibull distribution (note that the exponential distribution is a special case of the Weibull). The Weibull model has three parameters. One parameter is a scale or characteristic life parameter. For these plans and procedures, the value for this parameter need not be known; the techniques used are independent of its magnitude. A second parameter is a location or "guaranteed life" parameter. In these plans and procedures, it is assumed that this parameter has a value of zero and that there is some risk of item failure right from the start of life. If this is not the case for some applications, a simple modification in procedure is available. The third parameter, and the one of importance, is the shape parameter, $\beta .{ }^{4}$ The magnitude of the conversion factors used in the procedures described in this report depends directly on the value for this parameter. For this reason, the magnitude of the parameter shall be known through experience with the product or shall be estimated from past research, engineering, or inspection data. Estimation procedures are available and are outlined in Ref (1).
4.6 For the common case of random chance failures with the failure rate constant over time, rather than failures as a result of "infant mortality" or wearout, a value of 1 for the shape parameter shall be assumed. With this parameter value, the Weibull distribution reduces to the exponential. Tables of conversion factors are provided in Annex A1 for 15 selected shape parameter values ranging from $1 / 2$ to 10 , the range commonly encountered in industrial and technical practice. The value 1, used for the exponential case, is included. Factors for other required shape parameter values within this range may be obtained approximately by interpolation. A more complete discussion of the relationship between failure patterns and the Weibull parameters can be found in Refs (1-3).
4.7 One possible acceptance criterion is the mean life for items making up the lot $(\mu)$. Mean life conversion factors or values for the dimensionless ratio $100 t / \mu$ have been determined to correspond to or replace all the $p$ ' or percent defective values associated with Practice E2234 plans. In this factor, $t$ represents the specified test truncation time and $\mu$ the mean item life for the lot. For reliability or life-length applications, these factors are used in place of the corresponding $p^{\prime}$ values normally used in the use of Practice E2234 plans for attribute inspection of other item qualities. The use of these factors will be demonstrated by several examples (see Sections 5, 7, and 9).
4.8 Annex Table 1A lists, for each selected shape parameter value, $100 t / \mu$ ratios for each of the Practice E2234 AQL [ $p$ '(\%)] values. With acceptance inspection plans selected in

[^2]terms of these ratios, the probability of acceptance will be high for lots whose mean life meets the specified requirement. The actual probability of acceptance will vary from plan to plan and may be read from the associated operating characteristic curves supplied in MDL-STD-105. The curves are entered by using the corresponding $p^{\prime}(\%)$ value. Annex Table 1B lists $100 t / \mu$ ratios at the LQL for the quality level at which the consumer's risk is 0.10 . Annex Table 1C lists corresponding $100 t / \mu$ ratios for a consumer's risk of 0.05 .
4.8.1 These ratios are to be used directly for the usual case for which the value for the Weibull location or threshold parameter $(\gamma)$ can be assumed as zero. If $\gamma$ is not zero but has some other known value, all that shall be done is to subtract the value for $\gamma$ from $t$ to get $t_{0}$ and from $m$ to get $m_{0}$. These transformed values, $t_{0}$ and $m_{0}$, are then employed in the use of the tables and for all other computations. A solution in terms of $m_{0}$ and $t_{0}$ can then be converted back to actual or absolute values by adding the value for $\gamma$ to each.

## 5. Examples, Mean Life Ratio

5.1 A Practice E2234 acceptance sampling inspection plan is to be applied to incoming lots of product for which the mean item life is the property of interest. An acceptable mean life of 2000 h has been specified, and under the plan, used lots with a mean life of this value or greater shall have a high probability of acceptance. A testing truncation time of $t=250 \mathrm{~h}$ has been specified. From past experience it has been determined that the Weibull distribution can be used as a life-length model and a shape parameter value of 2.5 and a location or threshold parameter value of 0 can be assumed. Single sampling is to be used. A sample of as many as 300 items or so can be tested at one time. An appropriate sampling inspection plan shall be selected. Also, the consumer's risk under use of the selected plan shall be determined.
5.1.1 Computation of the $100 t / \mu$ ratio at the AQL gives $100 t / \mu=100 \times 250 / 2000=12.5$. Examination of the ratios in the column for a shape parameter of 2.5 in Annex Table 1A discloses a value of 12.4 for an AQL of 0.40 in $p^{\prime}(\%)$ terms. A plan with this AQL is accordingly to be used. Reference now to Practice E2234 indicates for Sample Size Code Letter M the sample size is 315 ; this value will accordingly be used. Examination of the Master Table for Normal Inspection (Single Sampling) in Practice E2234 shows for Sample Size Code Letter M and an AQL of 0.40, the acceptance number must be 3 and the rejection number 4.
5.1.2 The acceptance procedure will thus be to draw at random a sample of 315 items and submit them to life test for 250 h . At the end of that time, the number that has failed will be determined. If three items or less have failed, the lot will be accepted; if four or more have failed, it will be rejected.
5.1.3 The consumer's risk at a probability level of 0.10 can be determined by use of Annex Table 1B which gives $100 t / \mu$ ratios at the LQL for the 0.10 risk value. For a shape parameter value of 2.5, a Sample Size Code Letter M, and an AQL of 0.40 , the $100 t / \mu$ ratio value is found to be 24 . With $t=250$, $100 t / \mu=24$ or $100 \times 250 / \mu=24$ which gives a value for $\mu$ of 1040. Thus, if the mean life for the items in the lot is 1040 h or less, the probability of acceptance will be 0.10 or less. If the lot quality for which the consumer's risk was 0.05 was desired
instead, Annex Table 1C might be used which gives ratios at the LQL for this risk value.
5.2 A Practice E2234 plan with Sample Size Code Letter F and an AQL of 4.0 has been specified for a product for which life length in terms of cycles of operation is the quality of interest. Acceptance is to be in terms of a mean life evaluation. The Weibull distribution can be assumed to apply with a shape parameter value and a location parameter value of 0 . Testing of sample items is to be truncated at 5000 cycles. The operating characteristics in terms of mean life for this plan are required.
5.2.1 Annex Table 1A lists ratios of $100 t / \mu$ at selected AQLs and gives a $100 t / \mu$ value of 0.62 for an AQL of 4.0 and a shape parameter value of $2 / 3$. With $t=5000,100 t / \mu=0.62$ or $100 \times$ $5000 / \mu=0.62$ which gives $\mu=810000$. Therefore, if the mean item life for the lot is 810000 or more, the probability of acceptance will be high. Annex Table 1C gives ratios $100 t / \mu$ at the LQL for a consumer's risk of 0.05 and provides a $100 t / \mu$ value of 14 for Code Letter F, an AQL of 4.0, and a shape parameter value of $2 / 3$. Thus, $100 \times 5000 / \mu=14$ or $\mu=36000$. If the mean item life for the lot is 36000 cycles or less, the probability of acceptance will be 0.05 or less.
5.2.2 The sample size and acceptance number will be those specified by Practice E2234 for Code Letter F and an AQL of 4.0. For single sampling, the sample size will be 20 items and the acceptance number 2. For this example, as in all cases, the matched Practice E2234 double sampling and multiple sampling plans may be used instead. No additional changes in procedure are required. The specified test time, which in this case is 5000 cycles, shall be used for all samples.
5.3 Assume the Weibull distribution applies with a shape parameter value of $\beta=3.33$ and a location or threshold parameter value, $\gamma$, of 3000 h . A Practice E2234 acceptanceinspection plan shall be selected under which the probability of acceptance will be low ( 0.05 or less) if mean item life is 8000 $h$ or less. The sample size will be kept large to reduce the testing period time but it cannot exceed 250 items. To reduce further testing time, an acceptance number of 0 will be used. The required test truncation time must be determined; also, the AQL.
5.3.1 Reference to Practice E2234 indicates the Code Letter L with a sample size of 200 items shall be used. With this code letter and an acceptance number of 0 , the $A Q L$ in Practice E2234 terms must be 0.065 . Subtraction of the threshold parameter value, $\gamma$, of 3000 h from the required mean value, $\mu$, of 8000 h gives as a converted value for the mean $\mu_{0}=8000-$ $3000=5000 \mathrm{~h}$. This converted value must now be used in working with the tables of factors. Use of Annex Table 1C for $\beta=31 / 3$, Code Letter L, and an AQL of 0.065 gives a $100 t / \mu$ value of 31 at the LQL (for $P(A)=0.05$ ). With $\mu_{0}=5000$, $100 t_{0} / \mu_{0}=100 t_{0} / 5000=31$ or $t_{0}=1550 \mathrm{~h}$. Conversion of this to absolute terms gives $t=t_{0}+\gamma=1550+3000=4550 \mathrm{~h}$ as the required test truncation time.
5.3.2 From Annex Table 1A, the corresponding ratio at the AQL may be found. For an AQL of 0.065 and $b=31 / 3$, it is 12.3. Thus, $100 t_{0} / \mu_{0}=12.3$ or $100 \times 1550 / \mu_{0}=12.3$ or $\mu_{0}=$ 12 600. Converting this to absolute terms gives $\mu=\mu_{0}+\gamma=$ $12600+3000=15600$. Thus, the mean item life for a lot shall be 15600 h or more for its probability of acceptance to be high.

## 6. Hazard Rate Conversion Factors

6.1 Another measure of lot quality is the hazard rate or instantaneous failure rate, $h(t)$, at some specified period of time, $t$. Hazard rate conversion factors or values for the dimensionless product $100 t\{h(t)\}$ have been determined for all of the $p$ ' values that characterize the collection of Practice E2234 plans. As for the mean life plans, these products may be used in place of the corresponding $p^{\prime}$ values when using the Practice E2234 plans for life-length and reliability applications.
6.2 Annex Table 2A lists for each selected value for the shape parameter $100 t\{h(t)\}$ products for each Practice E2234 AQL value. Annex Table 2B lists corresponding $100 t\{h(t)\}$ products at the LQL for a consumer's risk of 0.10 . Annex Table 2C lists products at the LQL for a consumer's risk of 0.05 . Use of these tables of factors is similar to the method of use for the mean life ratios including the variation in method required when some nonzero value for the location or threshold parameter shall be assumed.
6.2.1 Note one point of difference. The products are for direct application only in cases in which the time $t$ at which the hazard rate is specified or is to be evaluated is the same as the time $t$ at which the life testing of sample items is to be truncated. However, a table of hazard rate ratios has been prepared, Annex Table 2D, to use in a simple modification of method that allows the test truncation time to differ from the time at which the hazard rate is specified. All that shall be done is to determine the hazard rate at the test truncation time which corresponds to the hazard rate at the specification time. Annex Table 2D provides ratios for making this conversion. It gives for various values of $t_{2} / t_{1}$ the corresponding values for the ratio $h\left(t_{2}\right) / h\left(t_{1}\right)$ for all the shape parameter values for which conversion values have been provided. If the test truncation time is shorter than the time for hazard rate specification, $t_{1}$ is used to represent the test truncation time and $h\left(t_{1}\right)$ the corresponding hazard rate at that time. In this case, $t_{2}$ represents the time of hazard rate specification and $h\left(t_{2}\right)$ the specified hazard rate. If the test truncation is longer instead, the meanings given Subscripts 1 and 2 are simply reversed.

## 7. Examples, Hazard Rate

7.1 An acceptance-inspection plan shall be selected from the Practice E2234 collection for an application for which the Weibull distribution applies and for which it may be assumed the shape parameter value is 1.67 and the location parameter value is 0 . A hazard rate of no more than $0.0005 / \mathrm{h}$ at 1000 h of life can be tolerated so a plan under which the probability of acceptance will be low ( 0.10 ) if this rate will be exceeded at this life is required. The test truncation time is likewise to be 1000 h .
7.1.1 Computation of the $100 t\{h(t)\}$ product gives $100 \times$ $1000 \times 0.0005=50$. Thus, apian shall be used for which this product is found at the LQL for which the consumer's risk is 0.10. Examination of the column for $\beta=1.67$ in Annex Table 2B discloses several close possibilities. One is for a plan with Code Letter D and an AQL of 1.5 for which the product is 48 ; another is Code Letter F and an AQL of 4.0 for which the product is likewise 48; still another is Code Letter G and an

AQL of 6.5 for which the product is 53 . Any of these will provide fairly closely the required consumer's protection.
7.1.2 The last plan mentioned with its relatively large sample size and acceptance number will discriminate most sharply between good and bad lots and hence provide the most reasonable AQL. This will be achieved at the expense of a relatively large number of item hours of inspection, of course. With this choice (Code Letter G and an AQL of 6.5) the AQL can be easily determined. Reference to Annex Table 2A gives a value for $100 t\{h(t)\}$ of 11.2 for an AQL of 6.5. Thus, $100 \times$ $1000 h(t)=11.2$ or $h(t)=0.000112$ at $t=1000$; the "acceptable" hazard rate is therefore 0.000112 (per hour). If, alternatively, Code Letter D and an AQL of 1.5 had been used, the "acceptable" hazard rate would be 0.0000252 (per hour) instead.
7.2 Suppose the selected sampling plan must have an acceptable hazard rate (a rate for which the probability of acceptance is high) of 0.0001 per hour at 500 h of life. However, the testing of sample items shall be truncated at 200 h . A value of $\beta=0.67$ and a location parameter of 0 can be assumed. A Practice E2234 plan shall be selected.
7.2.1 In this case, use Annex Table 2D. Letting $t_{2}=500$ and $t_{1}=200, t_{2} / t_{1}=500 / 200=2.5$. Referencing Annex Table 2D with this ratio using the value $\beta=0.67$ column shows $h\left(t_{2}\right) / h\left(t_{1}\right)$ to be 0.734 . With $h\left(t_{2}\right)=0.0001,0.0001 / h\left(t_{1}\right)=$ 0.734 or $h\left(t_{1}\right)=0.000136$. This failure rate number shall be used in selecting the plan. Thus, $100 t\{h(t)\}=100 \times 200 \times$ $0.000136=2.72$ (note that the testing truncation time of 200 h is used as $t$ at this point). Referencing Annex Table 2A examining the column for $\beta=0.67$ shows that a Practice E2234 plan with an AQL of $4.0 \%$ precisely meets this need.

## 8. Reliable Life Conversion Factors

8.1 A third possible reliability and life-length measure for the items in a lot or population is reliable life ( $\rho$ ). Reliable life can be defined as the life beyond which some specified proportion of the items in the lot or population will survive. The letter $r$ represents this specified proportion.
8.1.1 Tables of conversion factors have been prepared for two different proportions, $r=0.90$ and $r=0.99$. As for the mean life case, these reliable life conversion factors have been prepared in the form of values for the dimensionless ratio $100 t / \rho$. Ratio values have been determined for all the $p^{\prime}(\%)$ values associated with Practice E2234 plans. Annex Table 3A gives $100 t / \rho$ values at each of the AQLs for $r=0.90$; Annex Table 4A gives corresponding values for $r=0.99$. Annex Table 3B gives ratio values at the LQL for a consumer's risk of 0.10 for $r=0.90$; Annex Table 4B gives corresponding values for a consumer's risk of 0.10 and $r=0.99$. Annex Table 3C gives ratio values at the LQL for a consumer's risk of 0.05 and $r=0.90$; Annex Table 4C gives similar ratio values at a consumer's risk of 0.05 and $r=0.99$. These conversion ratios are used in the same manner in which mean life ratios are used, including the manner for application when the location parameter is not zero. See Section 9 for an example.

## 9. Examples, Reliable Life

9.1 A sampling inspection plan shall be selected for a product for which item life in terms of feet of travel is the
quality of interest. Experience indicates the Weibull distribution will serve well as a statistical model with a shape parameter value of approximately $11 / 3$ and a location parameter of 0 . A lot will be considered "acceptable" if the reliable life is 40000 ft and the probability of acceptance for such lots shall be high. For lots in which reliable life is 10000 ft or less, the probability of acceptance shall be low, namely 0.05 or less. Reliable life is defined as the life beyond which $90 \%$ of the items will survive; that is, $r$ is to be 0.90 . Testing of sample items is to be truncated at 5000 ft .
9.1.1 At the AQL , the $100 t / \rho$ factor is $100 \times 5000 / 40000=$ 12.5. Examination of Annex Table 3A shows that for $\beta=1 \frac{1}{3}$, the $100 t / \rho$ ratio for an AQL of 0.65 is 12.4 which is quite close to the desired ratio. Accordingly, a plan with this AQL is to be adopted. At the unacceptable or LQL, the $100 t / \rho_{r}$ factor is 100 $\times 5000 / 10000=50$. Referencing Annex Table 3C, which gives ratios at the LQL for $P(A)=0.05$, shows that, for Code Letter L, an AQL of 0.65 (which is required for this application, as indicated above) and $\beta=11 / 3$ the corresponding ratio is 48 , which is close to the desired value of 50 . Thus, a Practice E2234 plan with Code Letter L and an AQL of 0.65 will meet the specified operating requirements. For single sampling, Practice E2234 shows the sample size to be 200 items and the acceptance number 3 .

## 10. Summary

10.1 This practice preserves the structure of TR-7 for use in applications in which that standard is prescribed or its use is desirable.
10.2 This practice provides tables and procedures for applying three different measures of reliability in which testing is performed without replacement.
10.2.1 Mean Life, $\mu$-The expected life of the product.
10.2.2 Hazard Rate, $h(t)$-The instantaneous failure rate at some specified time, $t$.
10.2.3 Reliable Life, $\rho_{r}$-The life $\rho$ beyond which some specified proportion $r$ of the items in the population will survive.

### 10.3 Procedure for Application:

10.3.1 Using the tables of factors provided in Annex A1, select a suitable sampling inspection plan from those tabulated in Practice E2234 for normal inspection.
10.3.2 Draw at random a sample of items of the size specified by the selected Practice E2234 plan.
10.3.3 Place the sample of items on life test for the specified period of time, $t$.
10.3.4 Determine the number of sample items that failed during the test period.
10.3.5 Compare the number of items that failed with the number allowed under the selected Practice E2234 plan.
10.3.6 If the number that failed is equal to or less than the acceptance number, accept the lot; if the number failing exceeds the acceptance number, reject the lot.
10.4 Selection-Mean Life:
10.4.1 Specify:
10.4.1.1 Acceptable mean life, $\mu_{0}$.
10.4.1.2 Unacceptable mean life, $\mu_{1}$.
10.4.1.3 Test truncation time, $t$.
10.4.1.4 Weibull shape parameter, $\beta$.
10.4.2 Compute the dimensionless ratio $100 t / \mu_{0}$ from the specified $\mu_{0}$ and $t$ and enter Annex Table 1A under $\beta$. Locate the nearest value of $100 t / \mu_{0}$ to that calculated and read the corresponding AQL.
10.4.3 Compute the dimensionless ratio $100 t / \mu_{1}$ from the specified $\mu_{1}$ and $t$ and enter Annex Table 1B under $\beta$. Locate the nearest value of $100 t / \mu_{1}$ corresponding to the AQL obtained in 10.4.2 and read the sample size code letter (use Annex Table 1C if a limiting quality with $5 \%$ probability of acceptance is desired).
10.4.4 Obtain the sample size and acceptance number for the test from the Practice E2234 normal inspection plan.

### 10.4.5 Mean Life Example:

10.4.5.1 Suppose $\mu_{0}=50, \mu_{1}=10, t=5, \beta=1$, then $100 t / \mu_{0}=10$ giving an AQL of 10 from Annex Table 1A and $100 t / \mu_{1}=50$ giving Code F from Table 1B.
10.4.5.2 Practice E2234 gives sample size 20. Accept on 5 for Code $\mathrm{F}, \mathrm{AQL}=10$.

### 10.5 Selection-Hazard Rate or Reliable Life:

10.5.1 The selection of plans for a specified hazard rate or reliable life follows the procedure for mean life described in 10.4 using appropriate dimensionless ratios and the associated tables from Annex A1.
10.5.2 Hazard rate uses the product $100 t\{h(t)\}$ with the Annex A1 tables of Section B.
10.5.3 Reliable life uses the dimensionless ratio $100 t / \rho$ with the Annex A1 tables of Section C.

## 11. Keywords

11.1 exponential distribution; hazard rate; mean life; MIL-STD-105; reliability; reliable life; Weibull distribution

## ANNEX

## (Mandatory Information)

## A1. TABLES OF CONVERSION FACTORS

## TABLE 1A <br> $100 \mathrm{t} / \mu$ Ratios at the Acceptable Quality Level (normal inspection) for the ASTM E2234 Plans

Note 1-These plans assume the characteristic being measured has a Weibull distribution.
Note 2-Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is 8.03E-04, then the decimal is moved to the left four places. The number in decimal notation is 0.000803 ).

| AQL | Shape Parameter, $\beta$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{p}^{\prime}(\%)$ | 0.333 | 0.500 | 0.667 | 1.000 | 1.333 | 1.500 | 1.667 | 2.000 | 2.500 | 3.000 | 3.333 | 3.500 | 4.000 | 5.000 | 10.000 |
| 0.010 | $1.67 \mathrm{E}-11$ | 5.00E-07 | 7.52E-05 | $1.00 \mathrm{E}-02$ | 0.109 | 0.239 | 0.446 | 1.128 | 2.831 | 5.198 | 7.031 | 7.999 | 11.033 | 17.262 | 41.847 |
| 0.015 | 5.63E-11 | 1.13E-06 | 1.38E-04 | $1.50 \mathrm{E}-02$ | 0.147 | 0.313 | 0.568 | 1.382 | 3.330 | 5.950 | 7.940 | 8.981 | 12.210 | 18.720 | 43.578 |
| 0.025 | $2.61 \mathrm{E}-10$ | 3.13E-06 | 2.97E-04 | 2.50E-02 | 0.216 | 0.440 | 0.772 | 1.784 | 4.085 | 7.055 | 9.255 | 10.393 | 13.873 | 20.734 | 45.863 |
| 0.040 | $1.07 \mathrm{E}-09$ | 8.00E-06 | 6.02E-04 | $4.00 \mathrm{E}-02$ | 0.308 | 0.601 | 1.024 | 2.257 | 4.930 | 8.252 | 10.657 | 11.887 | 15.603 | 22.778 | 48.070 |
| 0.065 | $4.58 \mathrm{E}-09$ | $2.11 \mathrm{E}-05$ | $1.25 \mathrm{E}-03$ | 6.50E-02 | 0.443 | 0.831 | 1.370 | 2.877 | 5.986 | 9.702 | 12.328 | 13.656 | 17.617 | 25.101 | 50.462 |
| 0.100 | $1.67 \mathrm{E}-08$ | 5.01E-05 | $2.38 \mathrm{E}-03$ | 0.100 | 0.612 | 1.108 | 1.774 | 3.569 | 7.113 | 11.200 | 14.030 | 15.445 | 19.622 | 27.360 | 52.684 |
| 0.150 | $5.64 \mathrm{E}-08$ | 1.13E-04 | $4.38 \mathrm{E}-03$ | 0.150 | 0.830 | 1.452 | 2.263 | 4.372 | 8.366 | 12.822 | 15.845 | 17.344 | 21.716 | 29.673 | 54.866 |
| 0.250 | $2.61 \mathrm{E}-07$ | 3.13E-04 | $9.42 \mathrm{E}-03$ | 0.250 | 1.218 | 2.042 | 3.076 | 5.645 | 10.265 | 15.205 | 18.472 | 20.072 | 24.677 | 32.868 | 57.744 |
| 0.400 | $1.07 \mathrm{E}-06$ | 8.03E-04 | 1.91E-02 | 0.401 | 1.733 | 2.795 | 4.080 | 7.144 | 12.391 | 17.788 | 21.274 | 22.962 | 27.759 | 36.113 | 60.527 |
| 0.650 | $4.62 \mathrm{E}-06$ | $2.13 \mathrm{E}-03$ | 3.96E-02 | 0.652 | 2.497 | 3.867 | 5.464 | 9.112 | 15.055 | 20.922 | 24.619 | 26.388 | 31.352 | 39.806 | 63.547 |
| 1.000 | $1.69 \mathrm{E}-05$ | 5.05E-03 | 7.58E-02 | 1.005 | 3.454 | 5.159 | 7.083 | 11.312 | 17.899 | 24.167 | 28.031 | 29.859 | 34.932 | 43.402 | 66.356 |
| 1.500 | 5.75E-05 | 1.14E-02 | 0.140 | 1.511 | 4.690 | 6.771 | 9.047 | 13.872 | 21.071 | 27.687 | 31.680 | 33.551 | 38.683 | 47.092 | 69.119 |
| 2.500 | 2.70E-04 | 3.20E-02 | 0.303 | 2.532 | 6.906 | 9.551 | 12.330 | 17.954 | 25.901 | 32.883 | 36.983 | 38.879 | 44.008 | 52.211 | 72.778 |
| 4.000 | $1.13 \mathrm{E}-03$ | 8.33E-02 | 0.620 | 4.082 | 9.882 | 13.133 | 16.422 | 22.798 | 31.355 | 38.559 | 42.682 | 44.565 | 49.591 | 57.446 | 76.339 |
| 6.500 | $5.06 \mathrm{E}-03$ | 0.226 | 1.311 | 6.721 | 14.362 | 18.311 | 22.149 | 29.253 | 38.275 | 45.530 | 49.569 | 51.388 | 56.174 | 63.469 | 80.242 |
| 10.000 | $1.95 \mathrm{E}-02$ | 0.555 | 2.573 | 10.536 | 20.122 | 24.711 | 29.007 | 36.626 | 45.816 | 52.891 | 56.726 | 58.431 | 62.856 | 69.441 | 83.932 |

## TABLE 1B

100t/ $\mu$ Ratios at the Limiting Quality Level
for the ASTM E2234 Plans, Consumer's Risk $=0.10$
Note 1-These plans assume the characteristic being measured has a Weibull distribution.
Note 2-Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is $8.03 \mathrm{E}-04$, then the decimal is moved to the left four places. The number in decimal notation is 0.000803 ).

| ode | AQL | Shape Parameter, $\beta$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Letter | (p\%) | 0.333 | 0.50 | 0.667 | 1.000 | 1.333 | 1.500 | 1.667 | 2.000 | 2.500 | 3.000 | 3.333 | 3.500 | 4.000 | 5.000 | 10.000 |
| A | 6.500 | 25.433 | 66.274 | 92.927 | 115.129 | 120.933 | 121.682 | 121.789 | 121.073 | 119.240 | 117.369 | 116.235 | 115.707 | 114.281 | 112.025 | 106.605 |
| B | 4.000 | 7.536 | 29.455 | 50.583 | 76.753 | 89.223 | 92.861 | 95.489 | 98.856 | 101.388 | 102.531 | 102.922 | 103.050 | 103.265 | 103.299 | 102.369 |
| C | 2.500 | 1.628 | 10.604 | 23.509 | 46.052 | 60.826 | 66.059 | 70.282 | 76.573 | 82.650 | 86.478 | 88.298 | 89.056 | 90.885 | 93.267 | 97.271 |
| C | 10.000 | 11.235 | 38.440 | 61.762 | 87.681 | 98.590 | 101.478 | 103.429 | 105.659 | 106.932 | 107.183 | 107.115 | 107.045 | 106.759 | 106.086 | 103.741 |
| D | 1.500 | 0.397 | 4.142 | 11.616 | 28.782 | 42.756 | 48.289 | 53.012 | 60.537 | 68.485 | 73.938 | 76.686 | 77.865 | 80.809 | 84.899 | 92.805 |
| D | 6.500 | 2.361 | 13.587 | 28.313 | 52.129 | 66.752 | 71.750 | 75.709 | 81.469 | 86.852 | 90.126 | 91.644 | 92.267 | 93.745 | 95.608 | 98.484 |
| D | 10.000 | 7.688 | 29.850 | 51.091 | 77.265 | 89.669 | 93.274 | 95.871 | 99.185 | 101.658 | 102.759 | 103.128 | 103.247 | 103.437 | 103.437 | 102.437 |
| E | 1.000 | 9.26E-02 | 1.569 | 5.608 | 17.712 | 29.707 | 34.937 | 39.615 | 47.489 | 56.397 | 62.890 | 66.292 | 67.780 | 71.573 | 77.043 | 88.407 |
| E | 4.000 | 0.505 | 4.859 | 13.094 | 31.175 | 45.395 | 50.930 | 55.614 | 63.003 | 70.708 | 75.933 | 78.546 | 79.662 | 82.439 | 86.266 | 93.549 |
| E | 6.500 | 1.478 | 9.943 | 22.401 | 44.594 | 59.376 | 64.657 | 68.939 | 75.352 | 81.594 | 85.556 | 87.450 | 88.241 | 90.157 | 92.669 | 96.959 |
| E | 10.000 | 3.379 | 17.255 | 33.871 | 58.746 | 73.011 | 77.700 | 81.336 | 86.486 | 91.104 | 93.789 | 94.989 | 95.471 | 96.588 | 97.920 | 99.668 |
| F | 0.650 | $2.54 \mathrm{E}-02$ | 0.663 | 2.939 | 11.513 | 21.505 | 26.215 | 30.592 | 38.287 | 47.470 | 54.478 | 58.255 | 59.930 | 64.265 | 70.683 | 84.679 |
| F | 2.500 | 0.133 | 1.992 | 6.709 | 19.962 | 32.495 | 37.836 | 42.562 | 50.415 | 59.160 | 65.448 | 68.714 | 70.136 | 73.745 | 78.908 | 89.471 |
| F | 4.000 | 0.369 | 3.940 | 11.189 | 28.073 | 41.963 | 47.492 | 52.224 | 59.786 | 67.805 | 73.325 | 76.114 | 77.312 | 80.306 | 84.476 | 92.574 |
| F | 6.500 | 0.795 | 6.577 | 16.430 | 36.267 | 50.850 | 56.335 | 60.899 | 67.954 | 75.120 | 79.860 | 82.193 | 83.182 | 85.617 | 88.916 | 94.975 |
| F | 10.000 | 2.566 | 14.362 | 29.516 | 53.596 | 68.156 | 73.089 | 76.980 | 82.608 | 87.821 | 90.964 | 92.410 | 93.001 | 94.398 | 96.140 | 98.758 |
| G | 0.400 | 6.21E-03 | 0.259 | 1.452 | 7.196 | 15.117 | 19.164 | 23.075 | 30.268 | 39.334 | 46.578 | 50.594 | 52.399 | 57.141 | 64.341 | 80.792 |
| G | 1.500 | 3.14E-02 | 0.763 | 3.266 | 12.352 | 22.670 | 27.474 | 31.911 | 39.657 | 48.825 | 55.770 | 59.498 | 61.147 | 65.405 | 71.684 | 85.277 |
| G | 2.500 | 8.46E-02 | 1.476 | 5.358 | 17.183 | 29.038 | 34.237 | 38.900 | 46.773 | 55.716 | 62.257 | 65.691 | 67.194 | 71.032 | 76.576 | 88.139 |
| G | 4.000 | 0.176 | 2.407 | 7.730 | 21.939 | 34.879 | 40.294 | 45.043 | 52.852 | 61.437 | 67.540 | 70.688 | 72.053 | 75.506 | 80.412 | 90.319 |
| G | 6.500 | 0.524 | 4.981 | 13.339 | 31.563 | 45.818 | 51.351 | 56.028 | 63.393 | 71.059 | 76.246 | 78.837 | 79.944 | 82.694 | 86.479 | 93.665 |
| G | 10.000 | 1.201 | 8.658 | 20.194 | 41.613 | 56.374 | 61.743 | 66.136 | 72.790 | 79.367 | 83.606 | 85.654 | 86.514 | 88.611 | 91.395 | 96.290 |
| H | 0.250 | 1.63E-03 | 0.106 | 0.743 | 4.605 | 10.817 | 14.232 | 17.654 | 24.215 | 32.904 | 40.140 | 44.254 | 46.126 | 51.108 | 58.847 | 77.265 |
| H | 1.000 | 8.09E-03 | 0.309 | 1.657 | 7.859 | 16.150 | 20.324 | 24.329 | 31.633 | 40.747 | 47.967 | 51.950 | 53.737 | 58.414 | 65.486 | 81.507 |
| H | 1.500 | $2.14 \mathrm{E}-02$ | 0.590 | 2.694 | 10.865 | 20.592 | 25.223 | 29.548 | 37.194 | 46.384 | 53.437 | 57.252 | 58.947 | 63.342 | 69.869 | 84.191 |
| H | 2.500 | 4.36E-02 | 0.950 | 3.849 | 13.783 | 24.613 | 29.558 | 34.081 | 41.892 | 51.014 | 57.846 | 61.487 | 63.093 | 67.223 | 73.274 | 86.217 |
| H | 4.000 | 0.125 | 1.912 | 6.505 | 19.555 | 31.996 | 37.320 | 42.039 | 49.898 | 58.675 | 65.000 | 68.290 | 69.724 | 73.366 | 78.583 | 89.286 |
| H | 6.500 | 0.273 | 3.222 | 9.621 | 25.385 | 38.912 | 44.411 | 49.164 | 56.852 | 65.130 | 70.906 | 73.850 | 75.121 | 78.311 | 82.793 | 91.647 |
| H | 10.000 | 0.680 | 5.928 | 15.199 | 34.432 | 48.908 | 54.418 | 59.030 | 66.212 | 73.575 | 78.490 | 80.922 | 81.956 | 84.512 | 87.997 | 94.483 |
| J | 0.150 | 3.97E-04 | 4.14E-02 | 0.367 | 2.878 | 7.603 | 10.404 | 13.316 | 19.143 | 27.264 | 34.319 | 38.434 | 40.330 | 45.442 | 53.568 | 73.718 |
| J | 0.650 | 1.95E-03 | 0.120 | 0.814 | 4.893 | 11.320 | 14.819 | 18.308 | 24.960 | 33.711 | 40.959 | 45.066 | 46.932 | 51.889 | 59.565 | 77.735 |
| J | 1.000 | 5.10E-03 | 0.227 | 1.316 | 6.738 | 14.390 | 18.342 | 22.183 | 29.290 | 38.314 | 45.569 | 49.606 | 51.425 | 56.210 | 63.501 | 80.262 |
| $J$ | 1.500 | 1.03E-02 | 0.362 | 1.868 | 8.513 | 17.147 | 21.436 | 25.523 | 32.922 | 42.070 | 49.262 | 53.211 | 54.977 | 59.593 | 66.541 | 82.161 |
| J | 2.500 | 2.86E-02 | 0.717 | 3.117 | 11.974 | 22.148 | 26.911 | 31.322 | 39.046 | 48.222 | 55.196 | 58.946 | 60.607 | 64.899 | 71.240 | 85.013 |
| J | 4.000 | 6.09E-02 | 1.186 | 4.547 | 15.403 | 26.752 | 31.830 | 36.430 | 44.285 | 53.332 | 60.029 | 63.571 | 65.128 | 69.116 | 74.920 | 87.180 |
| $J$ | 6.500 | 0.145 | 2.119 | 7.025 | 20.584 | 33.251 | 38.618 | 43.353 | 51.194 | 59.891 | 66.120 | 69.349 | 70.753 | 74.312 | 79.393 | 89.745 |
| J | 10.000 | 0.354 | 3.832 | 10.956 | 27.682 | 41.525 | 47.051 | 51.787 | 59.369 | 67.426 | 72.984 | 75.795 | 77.003 | 80.026 | 84.240 | 92.444 |
| K | 0.100 | $1.04 \mathrm{E}-04$ | $1.70 \mathrm{E}-02$ | 0.188 | 1.842 | 5.440 | 7.726 | 10.188 | 15.315 | 22.807 | 29.575 | 33.618 | 35.502 | 40.645 | 48.994 | 70.500 |
| K | 0.400 | 5.08E-04 | 4.88E-02 | 0.415 | 3.124 | 8.086 | 10.989 | 13.988 | 19.945 | 28.174 | 35.270 | 39.392 | 41.287 | 46.384 | 54.454 | 74.325 |
| K | 0.650 | 1.32E-03 | 9.21E-02 | 0.669 | 4.292 | 10.261 | 13.580 | 16.925 | 23.378 | 31.991 | 39.210 | 43.330 | 45.209 | 50.217 | 58.025 | 76.724 |
| K | 1.000 | $2.64 \mathrm{E}-03$ | 0.146 | 0.947 | 5.410 | 12.206 | 15.845 | 19.445 | 26.246 | 35.094 | 42.354 | 46.445 | 48.299 | 53.208 | 60.774 | 78.520 |
| K | 1.500 | 7.24E-03 | 0.287 | 1.568 | 7.573 | 15.707 | 19.828 | 23.793 | 31.052 | 40.147 | 47.378 | 51.376 | 53.170 | 57.875 | 65.002 | 81.205 |
| K | 2.500 | $1.52 \mathrm{E}-02$ | 0.470 | 2.270 | 9.692 | 18.900 | 23.373 | 27.590 | 35.129 | 44.311 | 51.439 | 55.323 | 57.054 | 61.558 | 68.290 | 83.234 |
| K | 4.000 | 3.54E-02 | 0.825 | 3.465 | 12.849 | 23.351 | 28.206 | 32.675 | 40.447 | 49.602 | 56.509 | 60.206 | 61.840 | 66.054 | 72.252 | 85.614 |
| K | 6.500 | 8.31E-02 | 1.459 | 5.312 | 17.084 | 28.913 | 34.105 | 38.765 | 46.638 | 55.588 | 62.137 | 65.577 | 67.084 | 70.929 | 76.488 | 88.088 |
| K | 10.000 | 2.51E-01 | 3.050 | 9.234 | 24.700 | 38.122 | 43.608 | 48.363 | 56.079 | 64.420 | 70.262 | 73.247 | 74.535 | 11.111 | 82.341 | 91.396 |
| L | 0.065 | $2.54 \mathrm{E}-05$ | 6.63E-03 | 9.29E-02 | 1.151 | 3.824 | 5.648 | 7.684 | 12.107 | 18.898 | 25.286 | 29.197 | 31.041 | 36.139 | 44.598 | 67.263 |
| L | 0.250 | $1.24 \mathrm{E}-04$ | 1.90E-02 | 0.205 | 1.950 | 5.677 | 8.025 | 10.541 | 15.756 | 23.331 | 30.141 | 34.196 | 36.083 | 41.226 | 49.553 | 70.902 |
| L | 0.400 | 3.19E-04 | 3.58E-02 | 0.329 | 2.675 | 7.196 | 9.907 | 12.742 | 18.454 | 26.476 | 33.490 | 37.597 | 39.493 | 44.616 | 52.787 | 73.179 |
| L | 0.650 | 6.35E-04 | 5.66E-02 | 0.465 | 3.366 | 8.550 | 11.548 | 14.627 | 20.701 | 29.026 | 36.156 | 40.281 | 42.174 | 47.255 | 55.271 | 74.880 |
| L | 1.000 | $1.73 \mathrm{E}-03$ | 0.110 | 0.766 | 4.696 | 10.977 | 14.419 | 17.863 | 24.453 | 33.163 | 40.403 | 44.515 | 46.386 | 51.360 | 59.079 | 77.417 |
| L | 1.500 | 3.58E-03 | 0.179 | 1.103 | 5.991 | 13.176 | 16.961 | 20.673 | 27.619 | 36.556 | 43.819 | 47.889 | 49.728 | 54.583 | 62.027 | 79.325 |
| L | 2.500 | 8.23E-03 | 0.312 | 1.671 | 7.903 | 16.218 | 20.400 | 24.411 | 31.722 | 40.838 | 48.057 | 52.038 | 53.823 | 58.497 | 65.560 | 81.553 |
| L | 4.000 | 1.89E-02 | 0.544 | 2.536 | 10.435 | 19.977 | 24.552 | 28.840 | 36.450 | 45.640 | 52.722 | 56.562 | 58.270 | 62.705 | 69.307 | 83.851 |
| L | 6.500 | 5.50E-02 | 1.109 | 4.323 | 14.892 | 26.083 | 31.122 | 35.699 | 43.544 | 52.617 | 59.357 | 62.931 | 64.503 | 68.535 | 74.416 | 86.887 |
| M | 0.040 | 6.51E-06 | $2.67 \mathrm{E}-03$ | 4.70E-02 | 0.731 | 2.720 | 4.172 | 5.851 | 9.647 | 15.758 | 21.733 | 25.477 | 27.263 | 32.259 | 40.725 | 64.276 |
| M | 0.150 | 3.15E-05 | 7.65E-03 | 0.103 | 1.237 | 4.035 | 5.924 | 8.022 | 12.549 | 19.448 | 25.897 | 29.831 | 31.683 | 36.792 | 45.242 | 67.747 |
| M | 0.250 | 8.12E-05 | $1.44 \mathrm{E}-02$ | 0.166 | 1.695 | 5.111 | 7.309 | 9.692 | 14.691 | 22.061 | 28.766 | 32.789 | 34.668 | 39.808 | 48.185 | 69.916 |
| M | 0.400 | 1.61E-04 | 2.27E-02 | 0.234 | 2.131 | 6.069 | 8.515 | 11.119 | 16.472 | 24.176 | 31.047 | 35.120 | 37.011 | 42.153 | 50.443 | 71.535 |
| M | 0.650 | 4.36E-04 | 4.40E-02 | 0.385 | 2.968 | 7.780 | 10.619 | 13.564 | 19.440 | 27.601 | 34.672 | 38.790 | 40.686 | 45.793 | 53.898 | 73.944 |
| M | 1.000 | 8.99E-04 | 7.14E-02 | 0.553 | 3.779 | 9.326 | 12.474 | 15.679 | 21.935 | 30.402 | 37.580 | 41.706 | 43.593 | 48.643 | 56.566 | 75.753 |
| M | 1.500 | 2.05E-03 | 0.124 | 0.834 | 4.970 | 11.454 | 14.975 | 18.481 | 25.157 | 33.924 | 41.174 | 45.279 | 47.143 | 52.093 | 59.753 | 77.857 |
| M | 2.500 | $4.65 \mathrm{E}-03$ | 0.214 | 1.257 | 6.537 | 14.066 | 17.975 | 21.782 | 28.849 | 37.852 | 45.110 | 49.157 | 50.981 | 55.785 | 63.117 | 80.019 |
| M | 4.000 | 1.32E-02 | 0.429 | 2.120 | 9.260 | 18.265 | 22.674 | 26.846 | 34.338 | 43.511 | 50.664 | 54.572 | 56.316 | 60.861 | 67.671 | 82.856 |

TABLE

| Code | A | Shape Parameter, $\beta$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Letter | (p\%) | 0.333 | 0.50 | 0.667 | 1.000 | 1.333 | 1.500 | 1.667 | 2.000 | 2.500 | 3.000 | 3.333 | 3.500 | 4.000 | 5.000 | 10.000 |
| N | 0.025 | 1.63E-06 | $1.06 \mathrm{E}-03$ | $2.35 \mathrm{E}-02$ | 0.461 | 1.923 | 3.066 | 4.435 | 7.657 | 13.099 | 18.631 | 22.180 | 23.891 | 28.740 | 37.130 | 61.374 |
| N | 0.100 | 7.87E-06 | 3.03E-03 | 5.17E-02 | 0.779 | 2.852 | 4.352 | 6.078 | 9.957 | 16.162 | 22.197 | 25.965 | 27.760 | 32.774 | 41.243 | 64.684 |
| N | 0.150 | 2.02E-05 | 5.69E-03 | 8.29E-02 | 1.067 | 3.611 | 5.367 | 7.340 | 11.654 | 18.329 | 24.651 | 28.535 | 30.370 | 35.455 | 43.922 | 66.751 |
| N | 0.250 | 4.01E-05 | 8.98E-03 | 0.117 | 1.340 | 4.286 | 6.250 | 8.418 | 13.063 | 20.082 | 26.600 | 30.558 | 32.418 | 37.538 | 45.974 | 68.293 |
| N | 0.400 | $1.08 \mathrm{E}-04$ | $1.74 \mathrm{E}-02$ | 0.191 | 1.864 | 5.490 | 7.788 | 10.261 | 15.407 | 22.917 | 29.694 | 33.739 | 35.624 | 40.767 | 49.111 | 70.585 |
| N | 0.650 | 2.22E-04 | 2.81E-02 | 0.275 | 2.371 | 6.574 | 9.142 | 11.853 | 17.374 | 25.229 | 32.171 | 36.262 | 38.156 | 43.292 | 51.530 | 72.302 |
| N | 1.000 | 5.03E-04 | 4.84E-02 | 0.413 | 3.113 | 8.063 | 10.961 | 13.956 | 19.908 | 28.132 | 35.226 | 39.347 | 41.242 | 46.340 | 54.413 | 74.297 |
| N | 1.500 | 1.13E-03 | 8.34E-02 | 0.621 | 4.083 | 9.883 | 13.135 | 16.425 | 22.801 | 31.358 | 38.562 | 42.685 | 44.568 | 49.594 | 57.448 | 76.341 |
| N | 2.500 | $3.18 \mathrm{E}-03$ | 0.166 | 1.040 | 5.759 | 12.791 | 16.519 | 20.188 | 27.078 | 35.982 | 43.245 | 47.324 | 49.169 | 54.046 | 61.538 | 79.012 |
| P | 0.015 | 3.97E-07 | 4.14E-04 | 1.16E-02 | 0.288 | 1.352 | 2.241 | 3.345 | 6.054 | 10.854 | 15.929 | 19.263 | 20.889 | 25.554 | 33.799 | 58.556 |
| P | 0.065 | 1.92E-06 | 1.18E-03 | $2.55 \mathrm{E}-02$ | 0.487 | 2.004 | 3.181 | 4.583 | 7.871 | 13.390 | 18.975 | 22.548 | 24.269 | 29.138 | 37.540 | 61.712 |
| P | 0.100 | 4.93E-06 | $2.22 \mathrm{E}-03$ | 4.09E-02 | 0.666 | 2.537 | 3.922 | 5.534 | 9.209 | 15.183 | 21.071 | 24.777 | 26.548 | 31.519 | 39.975 | 63.682 |
| P | 0.150 | 9.76E-06 | $3.50 \mathrm{E}-03$ | $5.76 \mathrm{E}-02$ | 0.837 | 3.010 | 4.565 | 6.345 | 10.321 | 16.633 | 22.734 | 26.530 | 28.335 | 33.367 | 41.840 | 65.150 |
| P | 0.250 | 2.62E-05 | 6.76E-03 | 9.43E-02 | 1.163 | 3.853 | 5.686 | 7.731 | 12.169 | 18.975 | 25.372 | 29.285 | 31.130 | 36.230 | 44.688 | 67.331 |
| P | 0.400 | 5.38E-05 | $1.09 \mathrm{E}-02$ | 0.135 | 1.478 | 4.612 | 6.671 | 8.926 | 13.717 | 20.883 | 27.481 | 31.468 | 33.336 | 38.467 | 46.882 | 68.964 |
| P | 0.650 | 1.21E-04 | 1.88E-02 | 0.203 | 1.938 | 5.652 | 7.992 | 10.503 | 15.708 | 23.275 | 30.080 | 34.134 | 36.021 | 41.164 | 49.493 | 70.859 |
| P | 1.000 | $2.73 \mathrm{E}-04$ | 3.22E-02 | 0.304 | 2.538 | 6.919 | 9.567 | 12.349 | 17.977 | 25.928 | 32.911 | 37.012 | 38.908 | 44.037 | 52.238 | 72.797 |
| P | 1.500 | 7.58E-04 | 6.37E-02 | 0.507 | 3.570 | 8.937 | 12.010 | 15.153 | 21.321 | 29.718 | 36.874 | 41.000 | 42.891 | 47.957 | 55.926 | 75.323 |
| Q | 0.010 | $1.04 \mathrm{E}-07$ | 1.70E-04 | 5.95E-03 | 0.184 | 0.967 | 1.665 | 2.559 | 4.843 | 9.080 | 13.728 | 16.849 | 18.388 | 22.856 | 30.913 | 56.000 |
| Q | 0.040 | 5.03E-07 | 4.85E-04 | 1.31E-02 | 0.311 | 1.434 | 2.362 | 3.506 | 6.296 | 11.200 | 16.351 | 19.721 | 21.362 | 26.060 | 34.333 | 59.017 |
| Q | 0.065 | 1.29E-06 | 9.08E-04 | 2.09E-02 | 0.426 | 1.815 | 2.912 | 4.233 | 7.366 | 12.699 | 18.155 | 21.669 | 23.367 | 28.188 | 36.558 | 60.899 |
| Q | 0.100 | $2.55 \mathrm{E}-06$ | $1.43 \mathrm{E}-03$ | $2.94 \mathrm{E}-02$ | 0.535 | 2.153 | 3.389 | 4.852 | 8.254 | 13.910 | 19.587 | 23.201 | 24.938 | 29.839 | 38.262 | 62.302 |
| Q | 0.150 | 6.85E-06 | $2.76 \mathrm{E}-03$ | $4.82 \mathrm{E}-02$ | 0.743 | 2.755 | 4.220 | 5.911 | 9.729 | 15.865 | 21.856 | 25.607 | 27.395 | 32.396 | 40.863 | 64.385 |
| Q | 0.250 | $1.40 \mathrm{E}-05$ | 4.46E-03 | 6.90E-02 | 0.944 | 3.296 | 4.949 | 6.823 | 10.965 | 17.458 | 23.670 | 27.512 | 29.332 | 34.392 | 42.865 | 65.943 |
| Q | 0.400 | 3.16E-05 | 7.66E-03 | 0.104 | 1.237 | 4.037 | 5.926 | 8.025 | 12.552 | 19.452 | 25.902 | 29.836 | 31.688 | 36.797 | 45.247 | 67.751 |
| Q | 0.650 | 7.08E-05 | $1.31 \mathrm{E}-02$ | 0.155 | 1.619 | 4.939 | 7.090 | 9.430 | 14.359 | 21.661 | 28.332 | 32.343 | 34.219 | 39.356 | 47.747 | 69.597 |
| Q | 1.000 | 1.96E-04 | $2.59 \mathrm{E}-02$ | 0.258 | 2.274 | 6.371 | 8.891 | 11.560 | 17.015 | 24.812 | 31.726 | 35.811 | 37.704 | 42.842 | 51.101 | 72.001 |
| R | 0.025 | 1.23E-07 | 1.89E-04 | 6.45E-03 | 0.195 | 1.008 | 1.726 | 2.644 | 4.977 | 9.280 | 13.979 | 17.127 | 18.677 | 23.170 | 31.252 | 56.307 |
| R | 0.040 | 3.15E-07 | $3.54 \mathrm{E}-04$ | 1.03E-02 | 0.266 | 1.275 | 2.128 | 3.192 | 5.822 | 10.521 | 15.521 | 18.818 | 20.429 | 25.061 | 33.276 | 58.102 |
| R | 0.065 | 6.23E-07 | 5.59E-04 | $1.45 \mathrm{E}-02$ | 0.334 | 1.513 | 2.477 | 3.659 | 6.524 | 11.524 | 16.744 | 20.147 | 21.801 | 26.528 | 34.826 | 59.439 |
| R | 0.100 | 1.67E-06 | 1.08E-03 | $2.38 \mathrm{E}-02$ | 0.464 | 1.935 | 3.083 | 4.456 | 7.689 | 13.142 | 18.682 | 22.234 | 23.947 | 28.799 | 37.191 | 61.424 |
| R | 0.150 | 3.42E-06 | $1.74 \mathrm{E}-03$ | $3.41 \mathrm{E}-02$ | 0.590 | 2.315 | 3.615 | 5.143 | 8.664 | 14.460 | 20.230 | 23.886 | 25.638 | 30.571 | 39.011 | 62.909 |
| R | 0.250 | 7.68E-06 | $2.98 \mathrm{E}-03$ | $5.11 \mathrm{E}-02$ | 0.772 | 2.835 | 4.328 | 6.047 | 9.916 | 16.108 | 22.135 | 25.901 | 27.694 | 32.705 | 41.175 | 64.630 |
| R | 0.400 | 1.72E-05 | 5.10E-03 | 7.63E-02 | 1.010 | 3.466 | 5.176 | 7.104 | 11.340 | 17.934 | 24.206 | 28.072 | 29.901 | 34.975 | 43.445 | 66.388 |
| R | 0.650 | $4.74 \mathrm{E}-05$ | $1.00 \mathrm{E}-02$ | 0.127 | 1.417 | 4.468 | 6.486 | 8.703 | 13.430 | 20.533 | 27.097 | 31.071 | 32.936 | 38.062 | 46.487 | 68.673 |

## TABLE 1C

$100 t / \mu$ Ratios at the Limiting Quality Level
for the MIL-STD-105D Plans, Consumer's Risk $=0.05$
Note 1—These plans assume the characteristic being measured has a Weibull distribution.
Note 2—Where scientific notation is used (i.e. E-x), the decimal point is moved to the left x places (e.g. if the number in scientific notation is $8.03 \mathrm{E}-04$, then the decimal is moved to the left four places. The number in decimal notation is 0.000803 ).

| Code | A | Shape Parameter, $\beta$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Letter | (p\%) | 0.333 | 0.50 | 0.667 | 1.000 | 1.333 | 1.500 | 1.667 | 2.000 | 2.500 | 3.000 | 3.333 | 3.500 | 4.000 | 5.000 | 10.000 |
| A | 6.500 | 56.010 | 112.180 | 137.903 | 149.787 | 147.319 | 145.016 | 142.620 | 138.099 | 132.476 | 128.130 | 125.783 | 124.743 | 122.053 | 118.079 | 109.448 |
| B | 4.000 | 16.596 | 49.858 | 75.065 | 99.858 | 108.690 | 110.668 | 111.822 | 112.758 | 112.642 | 111.932 | 111.377 | 111.097 | 110.287 | 108.881 | 105.099 |
| C | 2.500 | 3.585 | 17.949 | 34.887 | 59.915 | 74.098 | 78.727 | 82.303 | 87.342 | 91.825 | 94.407 | 95.552 | 96.010 | 97.065 | 98.307 | 99.865 |
| C | 10.000 | 20.487 | 57.375 | 83.403 | 107.122 | 114.568 | 115.972 | 116.634 | 116.787 | 115.851 | 114.582 | 113.748 | 113.349 | 112.240 | 110.421 | 105.839 |
| D | 1.500 | 0.875 | 7.011 | 17.238 | 37.447 | 52.085 | 57.550 | 62.079 | 69.050 | 76.087 | 80.717 | 82.986 | 83.946 | 86.304 | 89.487 | 95.280 |
| D | 6.500 | 4.291 | 20.235 | 38.169 | 63.616 | 77.505 | 81.937 | 85.317 | 89.999 | 94.053 | 96.312 | 97.286 | 97.669 | 98.530 | 99.493 | 100.465 |
| D | 10.000 | 12.789 | 41.908 | 65.896 | 91.551 | 101.836 | 104.443 | 106.144 | 107.966 | 108.796 | 108.738 | 108.512 | 108.374 | 107.918 | 107.007 | 104.190 |
| E | 1.000 | 0.204 | 2.655 | 8.322 | 23.044 | 36.189 | 41.637 | 46.391 | 54.167 | 62.657 | 68.656 | 71.738 | 73.072 | 76.440 | 81.206 | 90.764 |
| E | 4.000 | 0.917 | 7.231 | 17.642 | 38.029 | 52.692 | 58.145 | 62.657 | 69.585 | 76.559 | 81.133 | 83.371 | 84.317 | 86.638 | 89.764 | 95.427 |
| E | 6.500 | 2.450 | 13.929 | 28.845 | 52.780 | 67.376 | 72.346 | 76.274 | 81.976 | 87.284 | 90.500 | 91.986 | 92.594 | 94.036 | 95.845 | 98.607 |
| E | 10.000 | 5.299 | 23.290 | 42.415 | 68.250 | 81.702 | 85.869 | 88.994 | 93.220 | 96.736 | 98.596 | 99.360 | 99.651 | 100.278 | 100.902 | 101.174 |
| F | 0.650 | 5.60E-02 | 1.122 | 4.361 | 14.979 | 26.197 | 31.243 | 35.825 | 43.671 | 52.740 | 59.472 | 63.041 | 64.610 | 68.635 | 74.503 | 86.937 |
| F | 2.500 | 0.241 | 2.964 | 9.038 | 24.348 | 37.714 | 43.193 | 47.949 | 55.679 | 64.052 | 69.927 | 72.932 | 74.231 | 77.499 | 82.105 | 91.265 |
| F | 4.000 | 0.611 | 5.516 | 14.400 | 33.215 | 47.605 | 53.128 | 57.769 | 65.031 | 72.524 | 77.554 | 80.053 | 81.118 | 83.755 | 87.366 | 94.144 |
| F | 6.500 | 1.244 | 8.866 | 20.555 | 42.108 | 56.876 | 62.232 | 66.607 | 73.221 | 79.743 | 83.936 | 85.959 | 86.807 | 88.873 | 91.612 | 96.404 |
| F | 10.000 | 3.747 | 18.486 | 35.667 | 60.804 | 74.921 | 79.504 | 83.034 | 87.987 | 92.368 | 94.871 | 95.975 | 96.415 | 97.423 | 98.597 | 100.012 |
| G | 0.400 | $1.37 \mathrm{E}-02$ | 0.438 | 2.155 | 9.362 | 18.415 | 22.839 | 27.022 | 34.525 | 43.701 | 50.848 | 54.750 | 56.491 | 61.026 | 67.818 | 82.946 |
| G | 1.500 | 5.70E-02 | 1.135 | 4.399 | 15.065 | 26.310 | 31.363 | 35.948 | 43.796 | 52.861 | 59.586 | 63.149 | 64.716 | 68.734 | 74.588 | 86.987 |
| G | 2.500 | 0.140 | 2.066 | 6.894 | 20.327 | 32.939 | 38.296 | 43.027 | 50.874 | 59.591 | 65.844 | 69.088 | 70.500 | 74.079 | 79.194 | 89.633 |
| G | 4.000 | 0.275 | 3.242 | 9.667 | 25.466 | 39.005 | 44.504 | 49.257 | 56.942 | 65.212 | 70.981 | 73.921 | 75.189 | 78.373 | 82.845 | 91.676 |
| G | 6.500 | 0.764 | 6.404 | 16.105 | 35.788 | 50.345 | 55.837 | 60.414 | 67.503 | 74.721 | 79.507 | 81.865 | 82.866 | 85.332 | 88.680 | 94.849 |
| G | 10.000 | 1.676 | 10.814 | 23.857 | 46.505 | 61.275 | 66.492 | 70.697 | 76.950 | 82.975 | 86.761 | 88.559 | 89.306 | 91.108 | 93.450 | 97.367 |
| H | 0.250 | $3.58 \mathrm{E}-03$ | 0.179 | 1.103 | 5.991 | 13.177 | 16.961 | 20.674 | 27.620 | 36.556 | 43.820 | 47.889 | 49.728 | 54.584 | 62.027 | 79.325 |

TABLE Continued

| Code |  | Shape Parameter, $\beta$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Letter | \%) | 0.333 | 0.50 | 0.667 | 1.000 | 1.333 | 1.500 | 1.667 | 2.000 | 2.500 | 3.000 | 3.333 | 3.500 | 4.000 | 5.000 | 10.000 |
| H | 1.000 | 1.47E-02 | 0.459 | 2.232 | . 585 | 18.743 | 23.200 | 27.406 | 34.934 | 44.114 | 51.249 | 55.138 | 56.873 | 61.387 | 68.139 | 83.141 |
| H | 1.500 | 3.54E-02 | 0.826 | 3.466 | 12.853 | 23.357 | 28.212 | 32.682 | 40.454 | 49.608 | 56.515 | 60.212 | 61.846 | 66.059 | 72.257 | 85.617 |
| H | 2.500 | 6.82E-02 | 1.280 | 4.813 | 15.998 | 27.523 | 32.644 | 37.268 | 45.132 | 54.147 | 60.792 | 64.298 | 65.837 | 69.774 | 75.490 | 87.512 |
| H | 4.000 | 0.182 | 2.457 | 7.852 | 22.169 | 35.153 | 40.575 | 45.325 | 53.128 | 61.694 | 67.775 | 70.909 | 72.268 | 75.703 | 80.580 | 90.413 |
| H | 6.500 | 0.380 | 4.022 | 11.361 | 28.360 | 42.285 | 47.816 | 52.544 | 60.091 | 68.082 | 73.575 | 76.347 | 77.537 | 80.511 | 84.649 | 92.668 |
| H | 10.000 | 0.909 | 7.190 | 17.566 | 37.921 | 52.579 | 58.034 | 62.550 | 69.485 | 76.471 | 81.056 | 83.300 | 84.248 | 86.576 | 89.712 | 95.400 |
| J | 0.150 | 8.75E-04 | 7.01E-02 | 0.545 | 3.745 | 9.262 | 12.399 | 15.594 | 21.835 | 30.291 | 37.465 | 41.591 | 43.479 | 48.532 | 56.462 | 75.683 |
| $J$ | 0.650 | 3.54E-03 | 0.178 | 1.097 | 5.967 | 13.137 | 16.916 | 20.624 | 27.564 | 36.497 | 43.761 | 47.832 | 49.671 | 54.529 | 61.978 | 79.294 |
| J | 1.000 | 8.44E-03 | 0.318 | 1.693 | 7.970 | 16.322 | 20.516 | 24.535 | 31.856 | 40.977 | 48.193 | 52.170 | 53.953 | 58.621 | 65.671 | 81.622 |
| J | 1.500 | $1.61 \mathrm{E}-02$ | 0.488 | 2.336 | 9.880 | 19.174 | 23.674 | 27.909 | 35.467 | 44.653 | 51.770 | 55.642 | 57.367 | 61.854 | 68.553 | 83.394 |
| J | 2.500 | 4.17E-02 | 0.921 | 3.762 | 13.573 | 24.332 | 29.257 | 33.769 | 41.572 | 50.702 | 57.551 | 61.205 | 62.817 | 66.966 | 73.049 | 86.085 |
| $J$ | 4.000 | 8.49E-02 | 1.480 | 5.369 | 17.206 | 29.068 | 34.268 | 38.932 | 46.805 | 55.747 | 62.285 | 65.718 | 67.221 | 71.056 | 76.597 | 88.151 |
| J | 6.500 | 0.194 | 2.569 | 8.117 | 22.665 | 35.741 | 41.179 | 45.932 | 53.720 | 62.243 | 68.277 | 71.382 | 72.727 | 76.123 | 80.937 | 90.614 |
| J | 10.000 | 0.455 | 4.532 | 12.427 | 30.107 | 44.223 | 49.760 | 54.462 | 61.914 | 69.729 | 75.055 | 77.728 | 78.873 | 81.723 | 85.666 | 93.224 |
| K | 0.100 | $2.29 \mathrm{E}-04$ | 2.87E-02 | 0.279 | 2.397 | 6.627 | 9.208 | 11.930 | 17.468 | 25.339 | 32.287 | 36.380 | 38.274 | 43.409 | 51.641 | 72.380 |
| K | 0.400 | 9.22E-04 | 7.26E-02 | 0.560 | 3.810 | 9.384 | 12.543 | 15.757 | 22.026 | 30.503 | 37.683 | 41.809 | 43.696 | 48.744 | 56.659 | 75.815 |
| K | 0.650 | 2.18E-03 | 0.129 | 0.861 | 5.078 | 11.638 | 15.189 | 18.719 | 25.426 | 34.214 | 41.468 | 45.570 | 47.431 | 52.371 | 60.008 | 78.023 |
| K | 1.000 | 4.13E-03 | 0.197 | 1.184 | 6.279 | 13.648 | 17.499 | 21.263 | 28.275 | 37.248 | 44.510 | 48.567 | 50.399 | 55.227 | 62.612 | 79.698 |
| K | 1.500 | 1.05E-02 | 0.368 | 1.892 | 8.584 | 17.256 | 21.556 | 25.652 | 33.060 | 42.211 | 49.400 | 53.344 | 55.109 | 59.718 | 66.653 | 82.230 |
| K | 2.500 | 2.11E-02 | 0.586 | 2.680 | 10.826 | 20.536 | 25.162 | 29.484 | 37.127 | 46.317 | 53.373 | 57.190 | 58.887 | 63.285 | 69.819 | 84.160 |
| K | 4.000 | 4.72E-02 | 1.001 | 4.003 | 14.147 | 25.099 | 30.075 | 34.618 | 42.441 | 51.548 | 58.351 | 61.970 | 63.564 | 67.662 | 73.656 | 86.442 |
| K | 6.500 | 1.07E-01 | 1.726 | 6.023 | 18.577 | 30.789 | 36.065 | 40.765 | 48.635 | 57.483 | 63.898 | 67.247 | 68.710 | 72.431 | 77.781 | 88.830 |
| K | 10.000 | 3.10E-01 | 3.513 | 10.265 | 26.505 | 40.193 | 45.708 | 50.454 | 58.093 | 66.264 | 71.934 | 74.813 | 76.053 | 79.161 | 83.511 | 92.043 |
| L | 0.065 | 5.60E-05 | 1.12E-02 | 0.138 | 1.498 | 4.659 | 6.731 | 8.999 | 13.810 | 20.996 | 27.605 | 31.595 | 33.465 | 38.596 | 47.008 | 69.057 |
| L | 0.250 | $2.24 \mathrm{E}-04$ | 2.83E-02 | 0.276 | 2.378 | 6.589 | 9.160 | 11.874 | 17.400 | 25.259 | 32.203 | 36.294 | 38.189 | 43.324 | 51.560 | 72.323 |
| L | 0.400 | 5.28E-04 | 5.00E-02 | 0.423 | 3.164 | 8.162 | 11.081 | 14.094 | 20.071 | 28.316 | 35.418 | 39.540 | 41.435 | 46.530 | 54.591 | 74.418 |
| L | 0.650 | 9.93E-04 | 7.63E-02 | 0.581 | 3.906 | 9.560 | 12.753 | 15.994 | 22.302 | 30.807 | 37.997 | 42.122 | 44.007 | 49.048 | 56.942 | 76.004 |
| L | 1.000 | 2.51E-03 | 0.142 | 0.924 | 5.324 | 12.059 | 15.676 | 19.258 | 26.035 | 34.868 | 42.127 | 46.221 | 48.077 | 52.994 | 60.578 | 78.393 |
| L | 1.500 | 5.00E-03 | 0.224 | 1.302 | 6.692 | 14.316 | 18.259 | 22.092 | 29.191 | 38.210 | 45.466 | 49.505 | 51.325 | 56.114 | 63.415 | 80.208 |
| L | 2.500 | 1.10E-02 | 0.379 | 1.931 | 8.701 | 17.432 | 21.752 | 25.861 | 33.285 | 42.441 | 49.623 | 53.562 | 55.323 | 59.920 | 66.834 | 82.341 |
| L | 4.000 | 2.43E-02 | 0.644 | 2.875 | 11.347 | 21.272 | 25.963 | 30.327 | 38.010 | 47.195 | 54.215 | 58.002 | 59.682 | 64.032 | 70.478 | 84.556 |
| L | 6.500 | 6.80E-02 | 1.277 | 4.805 | 15.979 | 27.499 | 32.618 | 37.241 | 45.105 | 54.121 | 60.768 | 64.275 | 65.814 | 69.753 | 75.472 | 87.501 |
| M | 0.040 | 1.43E-05 | 4.52E-03 | $6.98 \mathrm{E}-02$ | 0.951 | 3.314 | 4.972 | 6.852 | 11.004 | 17.508 | 23.726 | 27.570 | 29.391 | 34.453 | 42.926 | 65.990 |
| M | 0.150 | 5.72E-05 | $1.14 \mathrm{E}-02$ | 0.139 | 1.508 | 4.683 | 6.763 | 9.037 | 13.858 | 21.055 | 27.669 | 31.662 | 33.532 | 38.664 | 47.074 | 69.105 |
| M | 0.250 | $1.34 \mathrm{E}-04$ | 2.01E-02 | 0.214 | 2.005 | 5.798 | 8.176 | 10.719 | 15.978 | 23.594 | 30.423 | 34.484 | 36.372 | 41.515 | 49.831 | 71.100 |
| M | 0.400 | $2.52 \mathrm{E}-04$ | 3.06E-02 | 0.293 | 2.473 | 6.786 | 9.403 | 12.158 | 17.746 | 25.660 | 32.628 | 36.725 | 38.620 | 43.752 | 51.968 | 72.608 |
| M | 0.650 | 6.35E-04 | 5.66E-02 | 0.464 | 3.364 | 8.547 | 11.544 | 14.623 | 20.697 | 29.021 | 36.151 | 40.276 | 42.169 | 47.250 | 55.266 | 74.877 |
| M | 1.000 | 1.25E-03 | 8.91E-02 | 0.652 | 4.221 | 10.133 | 13.429 | 16.756 | 23.183 | 31.778 | 38.991 | 43.113 | 44.993 | 50.008 | 57.831 | 76.595 |
| M | 1.500 | 2.73E-03 | 0.150 | 0.963 | 5.472 | 12.311 | 15.967 | 19.580 | 26.396 | 35.255 | 42.516 | 46.605 | 48.457 | 53.361 | 60.913 | 78.610 |
| M | 2.500 | 5.98E-03 | 0.253 | 1.425 | 7.108 | 14.978 | 19.007 | 22.905 | 30.083 | 39.142 | 46.387 | 50.408 | 52.216 | 56.965 | 64.183 | 80.692 |
| M | 4.000 | 1.63E-02 | 0.494 | 2.356 | 9.936 | 19.256 | 23.764 | 28.005 | 35.568 | 44.754 | 51.868 | 55.737 | 57.461 | 61.942 | 68.631 | 83.441 |
| N | 0.025 | 3.58E-06 | $1.79 \mathrm{E}-03$ | 3.49E-02 | 0.599 | 2.343 | 3.654 | 5.193 | 8.734 | 14.553 | 20.339 | 24.002 | 25.757 | 30.695 | 39.137 | 63.010 |
| N | 0.100 | 1.43E-05 | $4.51 \mathrm{E}-03$ | 6.96E-02 | 0.950 | 3.310 | 4.968 | 6.846 | 10.996 | 17.498 | 23.715 | 27.559 | 29.380 | 34.441 | 42.914 | 65.981 |
| N | 0.150 | 3.35E-05 | 7.96E-03 | 0.107 | 1.262 | 4.096 | 6.003 | 8.118 | 12.674 | 19.603 | 26.070 | 30.010 | 31.864 | 36.976 | 45.422 | 67.882 |
| N | 0.250 | 6.27E-05 | $1.21 \mathrm{E}-02$ | 0.146 | 1.555 | 4.792 | 6.902 | 9.205 | 14.073 | 21.315 | 27.954 | 31.955 | 33.827 | 38.962 | 47.364 | 69.318 |
| N | 0.400 | 1.57E-04 | 2.23E-02 | 0.231 | 2.113 | 6.031 | 8.467 | 11.063 | 16.403 | 24.095 | 30.960 | 35.032 | 36.923 | 42.064 | 50.358 | 71.475 |
| N | 0.650 | 3.10E-04 | 3.51E-02 | 0.324 | 2.648 | 7.143 | 9.842 | 12.667 | 18.363 | 26.371 | 33.379 | 37.486 | 39.382 | 44.506 | 52.683 | 73.106 |
| N | 1.000 | 6.71E-04 | 5.87E-02 | 0.477 | 3.427 | 8.666 | 11.687 | 14.786 | 20.888 | 29.235 | 36.374 | 40.499 | 42.392 | 47.468 | 55.470 | 75.015 |
| N | 1.500 | 1.46E-03 | 9.86E-02 | 0.704 | 4.440 | 10.524 | 13.889 | 17.271 | 23.776 | 32.426 | 39.653 | 43.771 | 45.647 | 50.643 | 58.419 | 76.983 |
| N | 2.500 | 3.93E-03 | 0.191 | 1.155 | 6.179 | 13.485 | 17.313 | 21.060 | 28.049 | 37.010 | 44.272 | 48.334 | 50.168 | 55.006 | 62.411 | 79.570 |
| P | 0.015 | 8.75E-07 | 7.01E-04 | 1.72E-02 | 0.374 | 1.647 | 2.671 | 3.917 | 6.905 | 12.059 | 17.390 | 20.845 | 22.520 | 27.292 | 35.625 | 60.117 |
| P | 0.065 | 3.48E-06 | $1.76 \mathrm{E}-03$ | 3.44E-02 | 0.593 | 2.326 | 3.631 | 5.163 | 8.692 | 14.497 | 20.274 | 23.932 | 25.685 | 30.620 | 39.061 | 62.949 |
| P | 0.100 | 8.15E-06 | $3.10 \mathrm{E}-03$ | 5.26E-02 | 0.788 | 2.878 | 4.386 | 6.121 | 10.016 | 16.239 | 22.284 | 26.057 | 27.854 | 32.870 | 41.341 | 64.760 |
| P | 0.150 | 1.53E-05 | $4.71 \mathrm{E}-03$ | 7.20E-02 | 0.971 | 3.366 | 5.042 | 6.938 | 11.119 | 17.654 | 23.891 | 27.743 | 29.567 | 34.633 | 43.105 | 66.128 |
| P | 0.250 | 3.82E-05 | 8.69E-03 | 0.114 | 1.318 | 4.233 | 6.182 | 8.335 | 12.956 | 19.950 | 26.454 | 30.407 | 32.265 | 37.383 | 45.822 | 68.180 |
| P | 0.400 | 7.50E-05 | $1.36 \mathrm{E}-02$ | 0.160 | 1.651 | 5.011 | 7.182 | 9.539 | 14.498 | 21.828 | 28.514 | 32.530 | 34.407 | 39.546 | 47.931 | 69.731 |
| P | 0.650 | 1.62E-04 | 2.28E-02 | 0.234 | 2.134 | 6.074 | 8.522 | 11.127 | 16.482 | 24.188 | 31.060 | 35.133 | 37.024 | 42.166 | 50.455 | 71.544 |
| P | 1.000 | 3.50E-04 | 3.81E-02 | 0.345 | 2.760 | 7.368 | 10.117 | 12.985 | 18.746 | 26.811 | 33.843 | 37.954 | 39.850 | 44.968 | 53.120 | 73.409 |
| P | 1.500 | 9.37E-04 | 7.34E-02 | 0.564 | 3.831 | 9.421 | 12.588 | 15.807 | 22.085 | 30.567 | 37.750 | 41.876 | 43.762 | 48.809 | 56.719 | 75.855 |
| Q | 0.010 | 2.29E-07 | 2.87E-04 | 8.83E-03 | 0.240 | 1.179 | 1.984 | 2.997 | 5.524 | 10.088 | 14.986 | 18.233 | 19.824 | 24.411 | 32.583 | 57.493 |
| Q | 0.040 | 9.12E-07 | 7.21E-04 | 1.76E-02 | 0.380 | 1.664 | 2.696 | 3.949 | 6.953 | 12.126 | 17.470 | 20.931 | 22.609 | 27.386 | 35.724 | 60.200 |
| Q | 0.065 | 2.13E-06 | $1.27 \mathrm{E}-03$ | 2.69E-02 | 0.504 | 2.058 | 3.257 | 4.682 | 8.011 | 13.581 | 19.201 | 22.789 | 24.516 | 29.397 | 37.807 | 61.931 |
| Q | 0.100 | 3.99E-06 | 1.93E-03 | 3.68E-02 | 0.621 | 2.407 | 3.743 | 5.306 | 8.892 | 14.764 | 20.584 | 24.261 | 26.022 | 30.971 | 39.419 | 63.237 |
| Q | 0.150 | 9.98E-06 | 3.55E-03 | 5.82E-02 | 0.843 | 3.026 | 4.587 | 6.373 | 10.359 | 16.681 | 22.789 | 26.588 | 28.394 | 33.427 | 41.900 | 65.197 |
| Q | 0.250 | 1.96E-05 | 5.56E-03 | 8.15E-02 | 1.055 | 3.581 | 5.328 | 7.291 | 11.589 | 18.248 | 24.559 | 28.440 | 30.274 | 35.357 | 43.824 | 66.677 |
| Q | 0.400 | 4.22E-05 | $9.28 \mathrm{E}-03$ | 0.120 | 1.362 | 4.339 | 6.319 | 8.501 | 13.171 | 20.215 | 26.746 | 30.710 | 32.571 | 37.693 | 46.125 | 68.406 |
| Q | 0.650 | 9.10E-05 | $1.55 \mathrm{E}-02$ | 0.176 | 1.761 | 5.259 | 7.497 | 9.916 | 14.973 | 22.399 | 29.134 | 33.166 | 35.047 | 40.189 | 48.553 | 70.183 |
| Q | 1.000 | 2.42E-04 | 2.98E-02 | 0.287 | 2.440 | 6.717 | 9.318 | 12.059 | 17.625 | 25.520 | 32.480 | 36.575 | 38.470 | 43.603 | 51.826 | 72.509 |
| R | 0.025 | 2.23E-07 | 2.81E-04 | 8.69E-03 | 0.237 | 1.170 | 1.970 | 2.979 | 5.496 | 10.047 | 14.936 | 18.178 | 19.767 | 24.349 | 32.518 | 57.435 |
| R | 0.040 | 5.21E-07 | 4.96E-04 | 1.33E-02 | 0.315 | 1.447 | 2.380 | 3.531 | 6.332 | 11.252 | 16.415 | 19.790 | 21.433 | 26.136 | 34.413 | 59.086 |
| R | 0.065 | 9.73E-07 | 7.53E-04 | 1.82E-02 | 0.388 | 1.691 | 2.735 | 4.001 | 7.028 | 12.231 | 17.596 | 21.068 | 22.749 | 27.535 | 35.879 | 60.331 |
| R | 0.100 | 2.43E-06 | $1.39 \mathrm{E}-03$ | 2.87E-02 | 0.526 | 2.126 | 3.352 | 4.804 | 8.186 | 13.818 | 19.479 | 23.086 | 24.820 | 29.716 | 38.135 | 62.199 |
| R | 0.150 | 4.76E-06 | $2.17 \mathrm{E}-03$ | 4.02E-02 | 0.659 | 2.515 | 3.892 | 5.496 | 9.157 | 15.114 | 20.991 | 24.692 | 26.462 | 31.429 | 39.884 | 63.609 |


[^0]:    ${ }^{1}$ This practice is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.30 on Statistical Quality Control.

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    ${ }^{2}$ For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For Annual Book of ASTM Standards volume information, refer to the standard's Document Summary page on the ASTM website.

[^1]:    ${ }^{3}$ The boldface numbers in parentheses refer to the list of references at the end of this standard.

[^2]:    ${ }^{4}$ In some disciplines, the Weibull shape $\beta$ parameter is referred to as the "Weibull slope."

