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## Information technology — Security techniques — Encryption algorithms —

Part 4: Stream ciphers

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### Foreword

ISO (the International Organization for Standardization) and IEC (the International Electrotechnical Commission) form the specialized system for worldwide standardization. National bodies that are members of ISO or IEC participate in the development of International Standards through technical committees established by the respective organization to deal with particular fields of technical activity. ISO and IEC technical committees collaborate in fields of mutual interest. Other international organizations, governmental and non-governmental, in liaison with ISO and IEC, also take part in the work. In the field of information technology, ISO and IEC have established a joint technical committee, ISO/IEC JTC 1.

International Standards are drafted in accordance with the rules given in the ISO/IEC Directives, Part 2.

The main task of the joint technical committee is to prepare International Standards. Draft International Standards adopted by the joint technical committee are circulated to national bodies for voting. Publication as an International Standard requires approval by at least 75 % of the national bodies casting a vote.

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO and IEC shall not be held responsible for identifying any or all such patent rights.

ISO/IEC 18033-4 was prepared by Joint Technical Committee ISO/IEC JTC 1, Information technology, Subcommittee SC 27, IT Security techniques: ANDARD PREVIEW

This second edition cancels and replaces the first edition (ISO/IEC 18033-4:2005), which has been technically revised. It also incorporates the Amendment ISO/IEC 18033-4:2005/Amd.1:2009.

ISO/IEC 18033 consists of the following parts, under the general title Information technology — Security techniques — Encryption algorithms. dards.iteh.ai/catalog/standards/sist/5a589dc3-bcf1-4617-b03b-79ac98ae145f/iso-jec-18033-4-2011

- Part 1: General
- Part 2: Asymmetric ciphers
- Part 3: Block ciphers
- Part 4: Stream ciphers

#### Introduction

This part of ISO/IEC 18033 includes stream cipher algorithms. A stream cipher is an encryption mechanism that uses a keystream to encrypt a plaintext in a bitwise or a block-wise manner. There are two types of stream ciphers: a synchronous stream cipher, in which the keystream is generated from only the secret key (and an initialization vector) and a self-synchronizing stream cipher, in which the keystream is generated from the secret key and some past ciphertexts (and an initialization vector). This part of ISO/IEC 18033 describes both pseudorandom number generators for producing keystream and output functions to combine a keystream with plaintext.

This part of ISO/IEC 18033 includes two output functions:

- Binary-additive output function; and
- MULTI-S01 output function.

This part of ISO/IEC 18033 includes five dedicated keystream generators:

- MUGI keystream generator;
- SNOW 2.0 keystream generator, ANDARD PREVIEW
- Rabbit keystream generator; (standards.iteh.ai)
- Decim<sup>v2</sup> keystream generator; and <u>ISO/IEC 18033-4:2011</u> https://standards.iteh.ai/catalog/standards/sist/5a589dc3-bcf1-4617-b03b-
- KCipher-2 (K2) keystream generator<sub>8ae145f/iso-iec-18033-4-2011</sub>

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## Information technology — Security techniques — Encryption algorithms —

## Part 4: Stream ciphers

#### 1 Scope

This part of ISO/IEC 18033 specifies

- a) output functions to combine a keystream with plaintext,
- b) keystream generators for producing keystream, and
- c) object identifiers assigned to dedicated keystream generators in accordance with ISO/IEC 9834.
- NOTE 1 The list of assigned object identifiers is given in Annex A.

NOTE 2 Any change to the specification of these algorithms resulting in a change of functional behaviour will result in a change of the object identifier assigned to the algorithms concerned.

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#### 2 Normative references

The following referenced documents are indispensable for the application of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO/IEC 18033-1, Information technology — Security techniques — Encryption algorithms — Part 1: General

#### 3 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO/IEC 18033-1 and the following apply.

#### 3.1

#### big-endian

method of storage of multi-byte numbers with the most significant bytes at the lowest memory addresses

[ISO/IEC 10118-1:2000]

#### 3.2

#### ciphertext

data which has been transformed to hide its information content

[ISO/IEC 10116:2006]

#### 3.3

#### confidentiality

property that information is not made available or disclosed to unauthorized individuals, entities, or processes

#### 3.4

#### data integrity

property that data has not been altered or destroyed in an unauthorized manner

[ISO/IEC 9797-1:2011]

#### 3.5

#### decryption

reversal of a corresponding encryption

[ISO/IEC 10116:2006]

#### 3.6

#### encryption

reversible transformation of data by a cryptographic algorithm to produce ciphertext, i.e., to hide the information content of the data

[ISO/IEC 9797-1:2011]

#### 3.7

#### initialization value

value used in defining the starting point of an encryption process **PREVIEW** 

3.8 key

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sequence of symbols that controls the operation of a cryptographic transformation (e.g., encryption, decryption, cryptographic check function computation, signature generation, or signature verification)

[ISO/IEC 11770-1:2010]

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#### 3.9

#### keystream function

function that takes as input, the current state of the keystream generator and (optionally) part of the previously generated ciphertext, and gives as output the next part of the keystream

#### 3.10

#### keystream generator

state-based process (i.e., a finite state machine) that takes as input, a key, an initialization vector, and if necessary the ciphertext, and gives as output a keystream (i.e., a sequence of bits or blocks of bits) of arbitrary length

#### 3.11

#### *n*-bit block cipher

block cipher with the property that plaintext blocks and ciphertext blocks are n bits in length

#### [ISO/IEC 10116:2006]

#### 3.12

#### next-state function

function that takes as input, the current state of the keystream generator and (optionally) part of the previously generated ciphertext, and gives as output a new state for the keystream generator

#### 3.13

#### output function

function that combines the keystream and the plaintext to produce the ciphertext

NOTE This function is often bitwise XOR.

#### 3.14

padding appending extra bits to a data string

[ISO/IEC 10118-1:2000]

#### 3.15

plaintext unencrypted information

[ISO/IEC 9797-1:2011]

#### 3.16

secret key

key used with symmetric cryptographic techniques by a specified set of entities

[ISO/IEC 11770-3:2008]

#### 3.17

state

current internal state of a keystream generator

#### 4 Symbols and abbreviated terms

## 4.1 Symbols **iTeh STANDARD PREVIEW** (standards.iteh.ai)

0 <i>x</i>	Prefix for hexadecimal values.
0 <sup>(n)</sup>	<i>n</i> -bit variable where 0 is assigned to every bit. https://standards.iteh.ai/catalog/standards/sist/5a589dc3-bcf1-4617-b03b-
AND	Bitwise logical AND operation.
$Am^{(i)}[Y]$	The <i>Y</i> -th bit of the register $Am^{(i)}$ in KCipher-2 (K2).
a <sub>i</sub>	Variables in an internal state of a keystream generator.
$b_i$	Variables in an internal state of a keystream generator.
CFB	Cipher FeedBack mode of a block cipher.
CTR	Counter mode of a block cipher.
$C_i$	Ciphertext block.
D <sub>i</sub>	64-bit constants used for MUGI.
$e_K$	Symmetric block cipher encryption function using secret key <i>K</i> .
F	Subfunction used for MUGI.
FSM	Subfunction used for SNOW 2.0.
$GF(2^n)$	Finite field of exactly $2^n$ elements.
$GF(2^n)[x]$	The polynomial ring over the finite field $GF(2^n)$ .

#### ISO/IEC 18033-4:2011(E)

- *Init* Function which generates the initial internal state of a keystream generator.
- *IV* Initialization vector.
- *IK* Internal key used for KCipher-2 (K2).
- K Key.
- *M* Subfunction used for MUGI.
- *Next* Next-state function of a keystream generator.
- *NLF* Nonlinear function used for KCipher-2 (K2).
- *n* Block length.
- OFB Output FeedBack mode of a block cipher.
- *OR* Bitwise logical OR operation.
- *Out* Output function combining keystream and plaintext in order to generate ciphertext.
- P Plaintext.
- *P<sub>i</sub>* Plaintext block. **iTeh STANDARD PREVIEW**
- *R* Additional input to Out.
- S<sub>R</sub> Subfunction used for MUGI.
- ISO/IEC 18033-4:2011

   Strm
   Keystream function//of adkeystream/generatohrds/sist/5a589dc3-bcf1-4617-b03b
- 79ac98ae145f/iso-iec-18033-4-2011
- SUB Lookup table used for MUGI and SNOW 2.0.
- Sub<sub>K2</sub> Subfunction used for KCipher-2 (K2).
- $S_i$  Internal state of a keystream generator.

NOTE During normal operation of the cipher, *i* will increase monotonically starting from zero. However, during initialization of the ciphers, it is convenient from a notational point of view to let *i* take negative values and define the starting state  $S_0$  in terms of values of  $S_i$  for *i* < 0.

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- *T* Subfunction used for SNOW 2.0.
- Z Keystream.
- *Z<sub>i</sub>* Keystream block.
- $\alpha_{MUL}$  Lookup table used for SNOW 2.0.
- $\alpha_{MUL0}$  Lookup table with index 0 used for KCipher-2 (K2).
- $\alpha_{MUL1}$  Lookup table with index 1 used for KCipher-2 (K2).
- $\alpha_{MUL2}$  Lookup table with index 2 used for KCipher-2 (K2).

$\alpha_{\rm MLII 3}$	Lookup table with index 3 used for KCipher-2 (K2)	
		1

 $\alpha_{\text{inv MUL}}$  Inverse lookup table used for SNOW 2.0.

 $\rho_1$  Subfunction used for MUGI.

 $\lambda_1$  Subfunction used for MUGI.

x The smallest integer greater than or equal to the real number *x*.

- $\neg x$  Bitwise complement operation.
- Polynomial multiplication.

|| Bit concatenation.

- +<sub>*m*</sub> Integer addition modulo  $2^m$ .
- ⊕ Bitwise XOR (eXclusive OR) operation.

 $\otimes$  Operation of multiplication of elements in the finite field *GF*(2<sup>*n*</sup>).

EXAMPLE  $C = A \otimes B$ : In this operation, the finite field is represented as a selected irreducible polynomial F(x) of degree *n* with binary coefficients, the *n*-bit blocks  $A = (a_0, a_1, ..., a_{n-1})$  and  $B = (b_0, b_1, ..., b_{n-1})$  (where the  $a_i$  and  $b_i$  are bits) are represented as the polynomials,  $A(x) = a_{n-1}x^{n-1} + a_{n-2}x^{n-2} + ... + a_1$  and  $B(x) = b_{n-1}x^{n-1} + b_{n-2}x^{n-2} + ... + b_0$  respectively, then let  $C(x) = A(x) \bullet B(x)$  mod F(x), i.e., C(x) is the polynomial of degree at most *n*-1 obtained by multiplying A(x) and B(x), dividing the result by F(x), and then taking the remainder. If  $C(x) = c_{n-1}x^{n-1} + c_{n-2}x^{n-2} + ... + c_0$  (where the  $c_i$  are bits) then let *C* be the *n*-bit block  $(c_0, c_1, ..., c_{n-1})$ .

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+ Modular addition operation<sup>8ae145f/iso-iec-18033-4-2011</sup>

 $<<_n t$  *t*-bit left shift in an *n*-bit register.

 $>>_n t$  *t*-bit right shift in an *n*-bit register.

 $<<<_n t$  t-bit left circular rotation in an *n*-bit register.

>>>  $_{n} t$  *t*-bit right circular rotation in an *n*-bit register.

#### 4.2 Functions

#### 4.2.1 Left-truncation of bits

The operation of selecting the *j* leftmost bits of an array  $A=(a_0,a_1,...,a_{m-1})$  to generate a *j*-bit array is written

 $(j \sim A) = (a_0, a_1, \dots, a_{j-1})$ 

This operation is defined only when  $1 \le j \le m$ .

See ISO/IEC 10116:2006.

#### 4.2.2 Shift operation

The operation *Shift* is defined as follows: Given an *n*-bit variable *X* and a *k*-bit variable *V* where  $1 \le k \le n$ , the effect of the shift function Shift is to produce the *n*-bit variable

 $Shift_{k}(X \mid V) = (x_{k}, x_{k+1}, ..., x_{n-1}, v_{0}, v_{1}, ..., v_{k-1}) \qquad (k < n)$  $Shift_{k}(X \mid V) = (v_{0}, v_{1}, ..., v_{k-1}) \qquad (k = n)$ 

The effect is to shift the bits of array *X* left by *k* places, discarding  $x_0, x_1, ..., x_{k-1}$  and to place the array *V* in the rightmost *k* places of *X*. When k = n the effect is to totally replace *X* by *V*.

See ISO/IEC 10116:2006.

#### 4.2.3 Variable *I*(*k*)

The variable I(k) is a k-bit variable where 1 is assigned to every bit.

#### 5 Framework for stream ciphers

This clause contains a high-level description of a framework for the stream ciphers specified in this part of ISO/IEC 18033. A detailed description of the general model for a stream cipher is provided in Clause 6. A stream cipher specified in this part of ISO/IEC 18033 is defined by the specification of the following processes:

- a) The keystream generator, which may be either (standards.iteh.ai)
  - a Synchronous keystream generator, or

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- a Self-synchronizingskeystream generatorandards/sist/5a589dc3-bcf1-4617-b03b-

79ac98ae145f/iso-iec-18033-4-2011

NOTE 1 Block cipher modes of operation are methods by which a block cipher can be used to construct a keystream generator. These modes are standardised in ISO/IEC 10116, and the meaning of the functions used in the specification is defined in 6.2.1 and 6.2.2.

NOTE 2 Block ciphers are defined in this part of ISO/IEC 18033.

- b) The output function, which may be either
  - the Binary-additive output function, or
  - the MULTI-S01 output function.

#### 6 General models for stream ciphers

#### 6.1 Keystream generators

#### 6.1.1 Synchronous keystream generators

A synchronous keystream generator is a finite-state machine. It is defined by:

a) An initialization function, *Init*, which takes as input a key K and an initialization vector IV, and outputs an initial state  $S_0$  for the keystream generator. The initialization vector should be chosen so that no two messages are ever encrypted using the same key and the same IV.

- b) A next-state function, Next, which takes as input the current state of the keystream generator S<sub>i</sub>, and outputs the next state of the keystream generator  $S_{i+1}$ .
- c) A keystream function, Strm, which takes as input a state of the keystream generator  $S_i$ , and outputs a keystream block  $Z_i$ .

When the synchronous keystream generator is first initialized, it will enter an initial state  $S_0$  defined by:

 $S_0 = Init(IV, K).$ 

On demand the synchronous keystream generator will, for i=0,1,...:

- Output a keystream block  $Z_i = Strm(S_i, K)$ . a)
- Update the state of the machine  $S_{i+1} = Next(S_i, K)$ . b)

Therefore to define a synchronous keystream generator it is only necessary to specify the functions Init, Next and Strm, including the lengths and alphabets of the key, the initialization vector, the state, and the output block.

#### 6.1.2 Self-synchronizing keystream generators

Generation of a keystream for a self-synchronizing stream cipher is dependent only on previous ciphertexts, the key, and the initialization vector. A general model for a keystream generator for a self-synchronizing stream cipher is now defined:

An initialization function, Init, which takes as input a key K and an initialization vector IV and outputs an a) internal input for the keystream generator S and r dummy ciphertext blocks C<sub>1</sub>, C<sub>2</sub>, ..., C<sub>r</sub>.

https://standards.iteh.ai/catalog/standards/sist/5a589dc3-bcf1-4617-b03b-b) A keystream function, Strm, that takes as input S and s ciphertext blocks  $C_{i-1}$ ,  $C_{i-2}$ , ...,  $C_{i-r}$ , and outputs a keystream block  $Z_i$ .

To define a self-synchronizing keystream generator it is only necessary to specify the number of feedback blocks r and the functions Init and Strm.

A self-synchronizing stream cipher differs from a synchronous stream cipher in that the keystream depends NOTE only on previous ciphertext, the initialization vector and the key, i.e., the keystream generator operates in a stateless fashion. As a result, a decryptor for such a cipher can recover from loss of synchronization after receiving sufficient ciphertext blocks. This also means that the method of keystream generation is dependent upon the selected output function Out, which is typically the bitwise XOR operation.

#### 6.2 Output functions

#### 6.2.1 General model of output function

6.2 specifies two stream cipher output functions, i.e., techniques to be used in a stream cipher to combine a keystream with plaintext to derive ciphertext.

An output function for a synchronous or a self-synchronizing stream cipher is a function Out that combines a plaintext block  $P_i$ , a keystream block  $Z_i$ , and some other input R if necessary to give a ciphertext block  $C_i$  ( $i \ge 1$ 0). A general model for a stream cipher output function is now defined:

Encryption of a plaintext block  $P_i$  by a keystream block  $Z_i$  is given by:

 $C_i = Out(P_i, Z_i, R),$ 

and decryption of a ciphertext block  $C_i$  by a keystream block  $Z_i$  is given by:

$$P_i = Out^{-1}(C_i, Z_i, R).$$

The output function shall satisfy that for any keystream block  $Z_i$ , plaintext block  $P_i$ , and other input R,

 $P_i = Out^{-1}(Out(P_i, Z_i, R), Z_i, R).$ 

#### 6.2.2 Binary-additive output function

A binary-additive stream cipher is a stream cipher in which the keystream, plaintext, and ciphertext blocks are strings of binary digits, and the operation to combine plaintext with keystream is bitwise XOR. The operation *Out* takes two inputs and does not use any additional information *R* for calculation. Let *n* to be the bit length of  $P_i$ . This function is specified by

 $Out(P_i, Z_i, R) = P_i \oplus Z_i.$ 

The operation *Out* <sup>-1</sup> is specified by

Out  ${}^{-1}(C_i, Z_i, R) = C_i \oplus Z_i$ .

NOTE The binary-additive stream cipher does not provide any integrity protection for encrypted data. If data integrity is required, either the MULTI-S01 output function or a separate integrity mechanism should be used, such as a MAC, i.e., a Message Authentication Code (such mechanisms are specified in ISO/IEC 9797).

#### 6.2.3 MULTI-S01 output function (standards.iteh.ai)

a) General model of MULTI-S01

#### ISO/IEC 18033-4:2011

MULTI-S01 is an output function for a synchronous stream cipher that supports both data confidentiality and data integrity. The MULTI-S01 encryption operation is suitable for use in an online environment. However, the decryption operation of MULTI-S01 can only be performed in an offline situation, as the integrity check is only performed after receiving all the ciphertext blocks. MULTI-S01 has a security parameter *n*. The computation of Out depends on the choice of a field  $GF(2^n)$ , i.e., on the choice of an irreducible polynomial over GF(2) of degree *n*. The MULTI-S01 function only accepts messages whose length is a multiple of *n*. To encrypt messages whose length is not a multiple of *n*, a padding mechanism Pad(M) is required.

NOTE 1 The redundancy *R* is generated in such a way that the sender and the receiver share it. *R* can be a fixed public value like 0x00...0.

b) The encryption function *Out*(*P*, *Z*, *R*)

Input:  $n \cdot u$  -bit plaintext *P*, keystream  $Z = (Z_0, Z_1, ...)$ , where  $Z_i$  are *n*-bit blocks, *n*-bit redundancy *R*.

Output: Ciphertext C.

- 1) Let *t* be the lowest value of *i* ( $i \ge 0$ ) such that  $Z_i \neq 0^{(n)}$ .
- 2) Let  $(P_0, P_1, ..., P_{u-1}) = P$ , where  $P_i$  is an *n*-bit block.
- 3) Set  $P_u = Z_{t+u+3}$ .
- 4) Set  $P_{u+1} = R$ .

- 5) For each  $P_i$ , do the following calculations (for i = 0, 1, ..., u + 1):
  - Let  $W_i = P_i \oplus Z_{t+i+1}$ .
  - Let  $X_i = Z_t \otimes W_i$  (in  $GF(2^n)$ ).
  - Let  $C_i = X_i \oplus W_{i-1}$ , where  $W_{i-1}$  is the W value of the previous block i 1, and  $W_{-1} = 0^{(n)}$ .
  - Set  $C = C_0 \parallel C_1 \parallel ... \parallel C_{u+1}$ .
  - Output C.

Figure 1 shows the block diagram of Out function.



Figure 1 — Out function of MULTI-S01 mode https://standards.iteh.avcatalog/standards/sist/3a589dc3-bc11-4617-b03b-

79ac98ae145f/iso-iec-18033-4-2011

NOTE 2 The irreducible polynomial used to define multiplication in the field depends on *n*. For instance, in the case of *n* = 64 and 128, the irreducible polynomial  $x^{64} + x^4 + x^3 + x + 1$  and  $x^{128} + x^7 + x^2 + x + 1$  can be used.

c) The decryption function  $Out^{-1}(P, Z, R)$ 

Input:  $n \cdot v$ -bit ciphertext C, keystream Z, n-bit redundancy R.

Output: Plaintext P or "reject".

- 1) Let *t* be the lowest value of *i* ( $i \ge 0$ ) such that  $Z_i \ne 0^{(n)}$ .
- 2) Let  $(C_0, C_1, ..., C_{v-1}) = C$ , where  $C_i$  is an *n*-bit block.
- 3) For each  $C_i$ , do the following calculations (for i = 0, 1, ..., v 1):

$$- \text{Let } X_i = C_i \oplus W_{i-1}, \text{ where } W_{-1} = 0^{(n)}.$$
$$- \text{Let } W_i = Z_t^{-1} \otimes X_i \text{ (in } GF(2^n)).$$

- Let  $P_i = W_i \oplus Z_{t+i+1}$ .
- 4) If  $P_{v-2} = Z_{t+v+1}$  and  $P_{v-1} = R$ , output  $P = P_0 || P_1 || ... || P_{v-3}$  as plaintext. Otherwise, output the special symbol meaning "*reject*" without any text.