

# ETSI TS 103 744 V1.1.1 (2020-12)



## **CYBER; Quantum-safe Hybrid Key Exchanges**

**ITeH STANDARD PREVIEW**  
(standards.iteh.ai)  
Full standard:  
<https://standards.iteh.ai/catalog/standards/sis/5c9666d4-69a4-45f9-81da-c5b750b5c2a5/etsi-ts-103-744-v1-1-2020-12>

---

**Reference**DTS/CYBER-QSC-0015

---

**Keywords**key exchange, quantum safe cryptography

---

**ETSI**650 Route des Lucioles  
F-06921 Sophia Antipolis Cedex - FRANCE

---

Tel.: +33 4 92 94 42 00 Fax: +33 4 93 65 47 16

Siret N° 348 623 562 00017 - NAF 742 C  
Association à but non lucratif enregistrée à la  
Sous-Préfecture de Grasse (06) N° 7803/88

---

**Important notice**

---

The present document can be downloaded from:  
<http://www.etsi.org/standards-search>

The present document may be made available in electronic versions and/or in print. The content of any electronic and/or print versions of the present document shall not be modified without the prior written authorization of ETSI. In case of any existing or perceived difference in contents between such versions and/or in print, the prevailing version of an ETSI deliverable is the one made publicly available in PDF format at [www.etsi.org/deliver](http://www.etsi.org/deliver).

Users of the present document should be aware that the document may be subject to revision or change of status. Information on the current status of this and other ETSI documents is available at <https://portal.etsi.org/TB/ETSIDeliverableStatus.aspx>

If you find errors in the present document, please send your comment to one of the following services:  
<https://portal.etsi.org/People/CommiteeSupportStaff.aspx>

---

**Copyright Notification**

---

No part may be reproduced or utilized in any form or by any means, electronic or mechanical, including photocopying and microfilm except as authorized by written permission of ETSI.

The content of the PDF version shall not be modified without the written authorization of ETSI.

The copyright and the foregoing restriction extend to reproduction in all media.

© ETSI 2020.  
All rights reserved.

**DECT™**, **PLUGTESTS™**, **UMTS™** and the ETSI logo are trademarks of ETSI registered for the benefit of its Members.  
**3GPP™** and **LTE™** are trademarks of ETSI registered for the benefit of its Members and of the 3GPP Organizational Partners.

**oneM2M™** logo is a trademark of ETSI registered for the benefit of its Members and of the oneM2M Partners.

**GSM®** and the GSM logo are trademarks registered and owned by the GSM Association.

# Contents

Intellectual Property Rights .....	5
Foreword.....	5
Modal verbs terminology.....	5
Introduction .....	5
1 Scope .....	6
2 References .....	6
2.1 Normative references .....	6
2.2 Informative references.....	7
3 Definition of terms, symbols and abbreviations.....	8
3.1 Terms.....	8
3.2 Symbols.....	9
3.3 Abbreviations .....	9
4 Purpose of quantum-safe hybrid key exchanges .....	10
4.1 Status of quantum-safe key exchange protocols.....	10
5 Architecture for quantum-safe hybrid key exchange .....	10
5.1 Functional entities .....	10
5.2 Information relationships (reference points) .....	11
6 Introductory information .....	11
6.1 Introduction .....	11
6.2 Notation.....	11
6.2.1 Radix.....	11
6.2.2 Conventions .....	12
6.2.3 Bit/Byte ordering .....	12
6.2.4 Integer encoding .....	12
7 Cryptographic primitives.....	12
7.1 Hash functions (hash).....	12
7.2 Context formatting function ( $f$ ) .....	13
7.3 PseudoRandom Function (PRF).....	13
7.3.1 PRF description .....	13
7.3.2 PRF to HMAC mapping .....	14
7.4 Key Derivation Functions (KDFs) .....	14
7.4.1 KDF description.....	14
7.4.2 KDF to HKDF mapping .....	14
7.5 Elliptic Curve Diffie-Hellman (ECDH) .....	15
7.5.1 ECDH description.....	15
7.5.2 Elliptic curve domain parameters .....	15
7.6 Key encapsulation mechanisms (KEMs).....	15
7.6.1 KEM description.....	15
7.6.2 Post-quantum KEMs.....	16
8 Hybrid key agreement schemes.....	16
8.1 General .....	16
8.1.1 Key exchange abstraction .....	16
8.1.2 Key exchange abstraction to ECDHE.....	17
8.1.3 Key exchange abstraction to KEM .....	17
8.2 Concatenate hybrid key agreement scheme.....	17
8.3 Cascade hybrid key agreement scheme .....	19
<b>Annex A (informative): Background .....</b>	<b>21</b>
A.1 Quantum computing threats to classical key exchange protocols .....	21
A.2 Rationale for quantum-safe hybrid key exchanges .....	21

<b>Annex B (informative):</b>	<b>Security consideration .....</b>	<b>23</b>
B.1	Security definitions .....	23
<b>Annex C (informative):</b>	<b>Test Vectors .....</b>	<b>24</b>
C.1	Introduction .....	24
C.2	Test vectors for CatKDF .....	24
C.2.1	ECDH with NIST P-256, SIKEp434, and SHA-256 .....	24
C.2.2	ECDH with NIST P-256, SIKEp434, and SHA3-256 .....	25
C.2.3	ECDH with NIST P-384, SIKEp503 and SHA-384 .....	25
C.2.4	ECDH with NIST P-384, SIKEp503, and SHA3-384 .....	25
C.2.5	ECDH with NIST P-384, SIKEp610 and SHA-384 .....	26
C.2.6	ECDH with NIST P-384, SIKEp610, and SHA3-384 .....	26
C.2.7	ECDH with NIST P-521, SIKEp751 and SHA-512 .....	27
C.2.8	ECDH with NIST P-384, SIKEp751, and SHA3-512 .....	27
C.2.9	ECDH with NIST P-256, Kyber512, and SHA-256 .....	28
C.2.10	ECDH with NIST P-256, Kyber512, and SHA3-256 .....	28
C.2.11	ECDH with NIST P-384, Kyber768 and SHA-384 .....	29
C.2.12	ECDH with NIST P-384, Kyber768, and SHA3-384 .....	30
C.2.13	ECDH with NIST P-512, Kyber1024 and SHA-512 .....	30
C.2.14	ECDH with NIST P-512, Kyber1024, and SHA3-512 .....	31
C.3	Test vectors for CasKDF .....	32
C.3.1	ECDH with NIST P-256, SIKEp434, and SHA-256 .....	32
C.3.2	ECDH with NIST P-256, SIKEp434, and SHA3-256 .....	32
C.3.3	ECDH with NIST P-384, SIKEp503 and SHA-384 .....	33
C.3.4	ECDH with NIST P-384, SIKEp503, and SHA-384 .....	34
C.3.5	ECDH with NIST P-384, SIKEp610 and SHA-384 .....	34
C.3.6	ECDH with NIST P-384, SIKEp610, and SHA3-384 .....	35
C.3.7	ECDH with NIST P-521, SIKEp751 and SHA-512 .....	35
C.3.8	ECDH with NIST P-384, SIKEp751, and SHA3-512 .....	36
C.3.9	ECDH with NIST P-256, Kyber512, and SHA-256 .....	36
C.3.10	ECDH with NIST P-256, Kyber512, and SHA3-256 .....	37
C.3.11	ECDH with NIST P-384, Kyber768 and SHA-384 .....	38
C.3.12	ECDH with NIST P-384, Kyber768, and SHA3-384 .....	39
C.3.13	ECDH with NIST P-384, Kyber1024 and SHA-512 .....	40
C.3.14	ECDH with NIST P-384, Kyber1024, and SHA3-384 .....	41
History .....		42

---

# Intellectual Property Rights

## Essential patents

IPRs essential or potentially essential to normative deliverables may have been declared to ETSI. The information pertaining to these essential IPRs, if any, is publicly available for **ETSI members and non-members**, and can be found in ETSI SR 000 314: "*Intellectual Property Rights (IPRs); Essential, or potentially Essential, IPRs notified to ETSI in respect of ETSI standards*", which is available from the ETSI Secretariat. Latest updates are available on the ETSI Web server (<https://ipr.etsi.org/>).

Pursuant to the ETSI IPR Policy, no investigation, including IPR searches, has been carried out by ETSI. No guarantee can be given as to the existence of other IPRs not referenced in ETSI SR 000 314 (or the updates on the ETSI Web server) which are, or may be, or may become, essential to the present document.

## Trademarks

The present document may include trademarks and/or tradenames which are asserted and/or registered by their owners. ETSI claims no ownership of these except for any which are indicated as being the property of ETSI, and conveys no right to use or reproduce any trademark and/or tradename. Mention of those trademarks in the present document does not constitute an endorsement by ETSI of products, services or organizations associated with those trademarks.

---

# Foreword

This Technical Specification (TS) has been produced by ETSI Technical Committee Cyber Security (CYBER).

---

# Modal verbs terminology

In the present document "**shall**", "**shall not**", "**should**", "**should not**", "**may**", "**need not**", "**will**", "**will not**", "**can**" and "**cannot**" are to be interpreted as described in clause 3.2 of the [ETSI Drafting Rules](#) (Verbal forms for the expression of provisions).

"**must**" and "**must not**" are **NOT** allowed in ETSI deliverables except when used in direct citation.

---

# Introduction

Hybrid Key Exchanges are constructions that combine a traditional key exchange, such as elliptic curve Diffie Hellman [1], with a quantum-safe key exchange such as Supersingular Isogeny Key Establishment (SIKE) [i.17], into a single key exchange. Hybrid key exchanges are a migration technique to move to quantum-safe technology in advance of establishing full security assurance in the underlying post-quantum cryptographic scheme.

---

# 1 Scope

The present document specifies several methods for deriving cryptographic keys from multiple shared secrets. The shared secrets are established using existing classical key agreement schemes, like elliptic curve Diffie-Hellman (ECDH) in NIST SP800-56Ar3 [1], and new quantum-safe key encapsulation mechanisms (KEMs).

---

## 2 References

### 2.1 Normative references

References are either specific (identified by date of publication and/or edition number or version number) or non-specific. For specific references, only the cited version applies. For non-specific references, the latest version of the referenced document (including any amendments) applies.

Referenced documents which are not found to be publicly available in the expected location might be found at <https://docbox.etsi.org/Reference>.

NOTE: While any hyperlinks included in this clause were valid at the time of publication, ETSI cannot guarantee their long term validity.

The following referenced documents are necessary for the application of the present document.

[1] NIST SP800-56Ar3: "Recommendation for Pair-Wise Key-Establishment Schemes Using Discrete Logarithm Cryptography".

NOTE: Available at <https://nvlpubs.nist.gov/nistpubs/SpecialPublications/nist.sp.800-56Ar3.pdf>.

[2] IETF RFC 2104: "HMAC: Keyed-Hashing for Message Authentication".

NOTE: Available at <https://tools.ietf.org/html/rfc2104>.

[3] IETF RFC 5869: "HMAC-based Extract-and-Expand Key Derivation Function (HKDF)".

NOTE: Available at <https://tools.ietf.org/html/rfc5869>.

[4] FIPS PUB 180-4: "Secure Hash Standard (SHS)".

NOTE: Available at <https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.180-4.pdf>.

[5] FIPS PUB 202: "SHA-3 Standard: Permutation-Based Hash and Extendable-Output Functions".

NOTE: Available at <https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.202.pdf>.

[6] FIPS PUB 186-4: "Digital Signature Standard (DSS)".

NOTE: Available at <https://nvlpubs.nist.gov/nistpubs/fips/nist.fips.186-4.pdf>.

[7] IETF RFC 5639: "Elliptic Curve Cryptography (ECC) Brainpool Standard Curves and Curve Generation".

NOTE: Available at <https://tools.ietf.org/html/rfc5639>.

[8] IETF RFC 7748: "Elliptic Curves for Security".

NOTE: Available at <https://tools.ietf.org/html/rfc7748>.

## 2.2 Informative references

References are either specific (identified by date of publication and/or edition number or version number) or non-specific. For specific references, only the cited version applies. For non-specific references, the latest version of the referenced document (including any amendments) applies.

NOTE: While any hyperlinks included in this clause were valid at the time of publication, ETSI cannot guarantee their long term validity.

The following referenced documents are not necessary for the application of the present document but they assist the user with regard to a particular subject area.

[i.1] NIST Post Quantum Round 2 Submission: "BIKE: Bit Flipping Key Encapsulation", Round 3 Submission, 22 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.2] NIST Post Quantum Round 3 Submission: "Classic McEliece: conservative code-based cryptography", 10 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.3] NIST Post Quantum Round 3 Submission: "CRYSTALS-Kyber", Version 3.0, 1 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.4] NIST Post Quantum Round 3 Submission: "FrodoKEM Learning With Errors Key Encapsulation", 30 September 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.5] NIST Post Quantum Round 3 Submission: "Hamming Quasi-Cyclic (HQC)", 1 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.6] NIST Post Quantum Round 3 Submission: "NTRU", 30 September 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.7] NIST Post Quantum Round 3 Submission: "NTRU Prime: round 3", 7 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.8] NIST Post Quantum Round 3 Submission: "SABER: Mod-LWR based KEM (Round 3 Submission)", Accessed 26 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.9] NIST Post Quantum Round 3 Submission: "Supersingular Isogeny Key Encapsulation", 1 October 2020.

NOTE: Available at <https://csrc.nist.gov/projects/post-quantum-cryptography/round-3-submissions>.

[i.10] Y. Dodis, R. Gennaro, J. Håstad, H. Krawczyk, and T. Rabin: "Randomness Extraction and Key derivation Using the CBC, Cascade, and HMAC Modes", Crypto 04, LNCS 3152, pp. 494-510. Springer Verlag, 2004.

[i.11] F. Giacon, F. Heuer, B. Poettering: "KEM Combiners", Public-Key Cryptography - PKC 2018, LNCS 10769.

NOTE: Available at <https://eprint.iacr.org/2018/024.pdf>.

[i.12] N. Bindel, J. Brendel, M. Fischlin, B. Goncalves, D. Stebila: "Hybrid Key Encapsulation Mechanisms and Authenticated Key Exchange", IACR eprint 2018-903.

NOTE: Available at <https://eprint.iacr.org/2018/903.pdf>.

- [i.13] N. Bindel, U. Herath, M. McKague, D. Stebila: "Transitioning to a Quantum-Resistant Public Key Infrastructure", Post-Quantum Cryptography, 8<sup>th</sup> International Workshop, PQCrypto 2017, Utrecht, The Netherlands Proceedings. pp. 384-405. Springer International Publishing, Cham (2017).
- [i.14] Simon, D. R.: "On the power of quantum computation", SFCS 94 Proceedings of the 35<sup>th</sup> Annual Symposium on Foundations of Computer Science, November 1994, Pages 116-123.
- NOTE: Available at <https://doi.org/10.1109/SFCS.1994.365701>.
- [i.15] Shor, P.W.: "Algorithms for quantum computation: discrete logarithms and factoring", SFCS 94: Proceedings of the 35th Annual Symposium on Foundations of Computer Science, November 1994, Pages 124-134.
- NOTE: Available at <https://dl.acm.org/doi/abs/10.1109/SFCS.1994.365700>.
- [i.16] NIST CAVP SP 800-56A ECC CDH Primitive Test Vectors.
- NOTE: Available at <https://csrc.nist.gov/CSRC/media/Projects/Cryptographic-Algorithm-Validation-Program/documents/components/ecccdhtestvectors.zip>.
- [i.17] SIKE Round 2 Known Answers Tests (KATs).
- NOTE: Available at <https://csrc.nist.gov/CSRC/media/Projects/Post-Quantum-Cryptography/documents/round-2/submissions/SIKE-Round2.zip>.
- [i.18] Campagna, M., Petcher, A.: "Security of Hybrid Key Encapsulation", IACR eprint 2020-1364.
- NOTE: Available at <https://eprint.iacr.org/2020/1364.pdf>.

---

## 3 Definition of terms, symbols and abbreviations

### 3.1 Terms

For the purposes of the present document, the following terms apply:

**asymmetric cryptography:** cryptographic system that utilizes a pair of keys, a private key known only to one entity, and a public key which can be openly distributed without loss of security

**big-endian:** octet ordering that signifies "big-end", or most significant octet value is stored to the left, or at the lowest storage location

EXAMPLE: The decimal value 108591, which is 0x0001A82F as a hex encoded 32-bit integer, is encoded as a length 4 octet string as 0001A82F.

**cryptographic hash function:** function that maps a bit string of arbitrary length to a fixed length bit string (*message digest* or *digest* for short)

NOTE: Hash functions are designed to satisfy the following properties:

- 1) (One-way) It is computationally infeasible to find any input that maps to any pre-specified output.
- 2) (Collision resistant) It is computationally infeasible to find any two distinct inputs that map to the same output.

**cryptographic key:** binary string used as a secret by a cryptographic algorithm

EXAMPLE: AES-256 requires a random 256-bit string as a secret key.

**entity:** person, device or system that is executing the steps of one of the processes defined or referenced in the present document



**key agreement scheme:** key-establishment procedure in which the resultant secret keying material is a function of contributions of the entities participating, such that no entity can predetermine that value of the secret keying material independently of the other entities' contributions

**key derivation:** process to derive key material from one or more shared secrets

**key encapsulation mechanism:** method to secure the establishment of a cryptographic key for transmission using public key cryptography

**key establishment/exchange method:** cryptographic procedure by which cryptographic keys are established between two parties

**label:** octet string that specifies a separation of use for the application or instance of the key derivation or exchange

**message digest/digest:** fixed-length output of a cryptographic hash function over a variable length input

**octet string:** ordered sequence of octets/bytes consisting of 8-bits each

**private key:** key in an asymmetric cryptographic scheme that is kept secret

**public key:** key in an asymmetric cryptographic scheme that can be made public without loss of security

**public key cryptography:** See asymmetric cryptography.

**random oracle:** theoretical black box that responds to every unique query with a uniformly random selection from the set of possible responses, with repeated queries receiving the same response

**security level:** measure of the strength of a cryptographic algorithm. If  $2^n$  operations are required to break the cryptographic algorithm/scheme/method, then the security level is  $n$ . Sometimes also referred to as *bit-strength*

**shared secret:** secret value that has been computed using a key-establishment scheme

## 3.2 Symbols

For the purposes of the present document, the following symbols apply:

$A    B$	The concatenation of binary strings A followed by B
$\emptyset$	A zero-length octet string
$[x]_n$	An integer value $x$ expressed as an $n$ -bit integer
$\lceil q \rceil$	The least integer value $x$ greater than or equal to $q$
$len(A)$	The number of octets in an octet string A
$hash( )$	A cryptographic hash function
$digest\_len$	The length in octets of a hash function's digest
$C$	A ciphertext value created by a KEM
$d$	A private key for elliptic curve cryptography
$k$	A cryptographic secret or key
$P$	A public key for an asymmetric cryptographic scheme
$psk$	A pre-shared key
$Q$	A public key for elliptic curve cryptography
$sk$	A private key for an asymmetric cryptographic scheme

## 3.3 Abbreviations

For the purposes of the present document, the following abbreviations apply:

AES	Advanced Encryption Standard
CAVP	Cryptographic Algorithm Validation Program
CDH	Cofactor Diffie-Hellman
ECC	Elliptic Curve Cryptography
ECDH	Elliptic Curve Diffie-Hellman
ECDHE	Elliptic Curve Diffie-Hellman Ephemeral
HKDF	HMAC-based Key Derivation Function
HMAC	Hash-based Message Authentication Code

IND-CCA	INDistinguishability under Chosen-Ciphertext Attacks
IND-CPA	INDistinguishability under Chosen-Plaintext Attacks
KDF	Key Derivation Function
KEM	Key Encapsulation Mechanism
LNCS	Lecture Notes in Computer Science
MA	Message from entity A
MB	Message from entity B
NIST	National Institute of Standards and Technology
OW-CPA	One-Way Chosen-Plaintext Attack
PRF	PseudoRandom Function
QA	A public-key from entity A
QB	A public-key from entity B
QKD	Quantum Key Distribution
RSA	Rivest, Shamir and Adelman
SIKE	Supersingular Isogeny Key Encapsulation
SP	Special Publication
SSH	Secure Shell
TLS	Transport Layer Security

---

## 4 Purpose of quantum-safe hybrid key exchanges

### 4.1 Status of quantum-safe key exchange protocols

NIST has initiated a process of analysing and standardizing one or more new quantum-safe key encapsulation mechanisms suitable to replace classical key exchanges. At the time of the present document, there are 9 round 3 post-quantum KEMs still under consideration [i.1] to [i.9].

The present document addresses the following cases:

- 1) One or more key exchange method establishes a shared secret from which randomness extraction is necessary.
- 2) One or more key exchange method incorporates a hash-based key derivation function prior to use within the hybrid method defined in the present document.

The quantum-safe hybrid key exchanges specified in the present document ensure that the derived key is at least as secure as the maximum security of the key exchange method. The resulting hybrid scheme will remain secure if one of the key exchange methods remains secure.

Quantum Key Distribution (QKD) provides an alternative method of establishing a shared secret between two entities using quantum mechanics. The scope of the present document is limited to elliptic curve Diffie-Hellman and quantum-safe key encapsulation mechanisms.

---

## 5 Architecture for quantum-safe hybrid key exchange

### 5.1 Functional entities

There are two entities defined for quantum-safe hybrid key exchange, an Initiator *A* that initiates a key exchange mechanism, and a Responder *B* who responds to the request. The entities communicate over a network medium.

**EXAMPLE:** Examples of such mediums are: ethernet, wireless and cellular networks.



Figure 1: Communicating entities *A* and *B*

## 5.2 Information relationships (reference points)

The network media over which the Initiator and Responder communicate will have a packet formatting scheme that allows the encoding and transmission of octet (byte) strings. The Initiator and Responder will exchange messages, where each message is an octet string that can span multiple packets. *MA* denotes a message from *A* to *B*, and *MB* denotes a message sent from *B* to *A*.

*A* initiates a hybrid key exchange by the transmission of a message to *B*. *B* responds to this message. The exchange between the entities can consist of a single message in each direction or multiple rounds of messages.

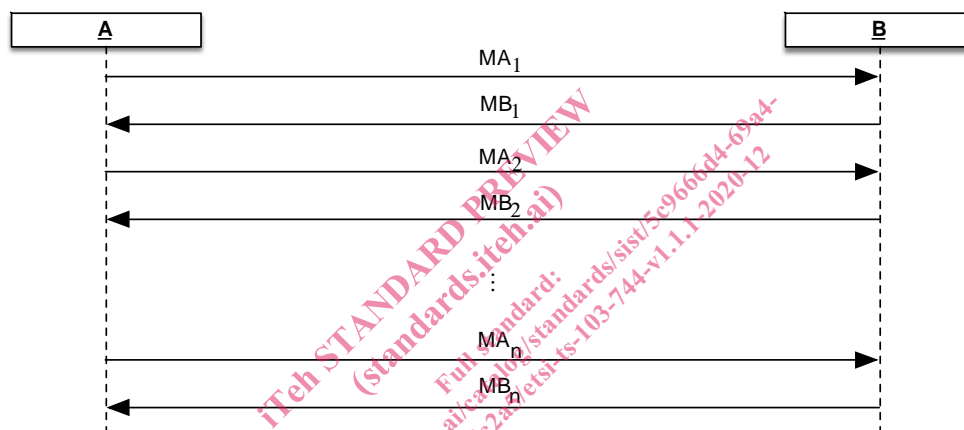


Figure 2: Messages exchanged between entities *A* and *B*

The transcript of the key exchange is the list of all messages exchanged between *A* and *B*, in the sequence order they were sent:

$$\text{transcript} = (MA_1, MB_1, MA_2, MB_2, \dots, MA_n, MB_n)$$

# 6 Introductory information

## 6.1 Introduction

Quantum-safe hybrid key exchange mechanisms combine a classic key exchange method like ECDH and a quantum-safe key-encapsulation mechanism (KEM). The hybrid exchange mechanisms specified in the present document use two or more shared secrets to derive cryptographic key material using a key derivation function. The key derivation functions for the hybrid key exchanges specified in the present document provide both the key expansion property and random extraction as per Crypto 04, LNCS 3152 [i.10].

## 6.2 Notation

### 6.2.1 Radix

The prefix "0x" indicates hexadecimal numbers.

## 6.2.2 Conventions

The assignment operator "=", as used in several programming languages:

$$\langle \text{variable} \rangle = \langle \text{expression} \rangle$$

means that  $\langle \text{variable} \rangle$  assumes the value that  $\langle \text{expression} \rangle$  had before the assignment took place. For instance:

$$x = x + y + 3$$

means:

(new value of  $x$ ) becomes (old value of  $x$ ) + (old value of  $y$ ) + 3.

## 6.2.3 Bit/Byte ordering

All data variables are represented with the most significant bit (or byte) on the left-hand side and the least significant bit (or byte) on the right-hand side. Where a variable is broken down into a number of sub-strings, the left most (most significant) sub-string is numbered 0, the next most significant is numbered 1 and so on through to the least significant.

EXAMPLE: An  $n$ -bit MESSAGE is subdivided into 64-bit substrings  $M_0, M_1, \dots, M_i$  so if the message is:

0x0123456789ABCDEFEDCBA987654321086545381AB594FC28786404C50A37...

then:

$M_0 = 0x0123456789ABCDEF$

$M_1 = 0xFEDCBA9876543210$

$M_2 = 0x86545381AB594FC2$

$M_3 = 0x8786404C50A37...$

## 6.2.4 Integer encoding

Integers are represented in the bit/byte ordering defined in clause 6.2.3. The most significant bit (or byte) on the left-hand side and the least significant bit (or byte) on the right-hand side.

EXAMPLE: a 32-bit integer of the value  $I = 37$  is encoded as:

$I = 0x00000025$

NOTE: This is big-endian or network byte ordering.

---

# 7 Cryptographic primitives

## 7.1 Hash functions (hash)

A hash function maps an arbitrary length bit string (*input*) to a fixed length (*digest\_len*) octet string output (*digest*):

$$\text{digest} = \text{hash}(\text{input})$$

Approved hash functions for the purpose of the present document shall be limited to those in the following list:

- SHA-256, SHA-384, SHA-512, SHA-512/256 as defined in FIPS PUB 180-4 [4].
- SHA3-256, SHA3-384, SHA3-512 as defined in FIPS PUB 202 [5].