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An American National Standard

Standard Practice for Calculating Sample Size to Estimate, With a Specified Tolerable Error, Precision, the Average for a Characteristic of a Lot or Process¹

This standard is issued under the fixed designation E 122; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon (ϵ) indicates an editorial change since the last revision or reapproval.

This standard has been approved for use by agencies of the Department of Defense.

1. Scope

1.1 This practice covers simple methods for calculating how many units to include in a random sample in order to estimate with a <u>prescribedspecified</u> precision, a measure of quality for all the units of a lot of material, or produced by a process. This practice will clearly indicate the sample size required to estimate the average value of some property or the fraction of nonconforming items produced by a production process during the time interval covered by the random sample. If the process is not in a state of statistical control, the result will not have predictive value for immediate (future) production. The practice treats the common situation where the sampling units can be considered to exhibit a single (overall) source of variability; it does not treat multi-level sources of variability.

2. Referenced Documents

2.1 ASTM Standards: ²

E 456Definitions of Terms Relating to Statistical Methods Terminology Relating to Quality and Statistics

3. Terminology

3.1 Definitions-Unless-: Unless otherwise noted, all statistical terms are defined in DefinitionsTerminology E 456.

3.2 Symbols: Symbols used in all equations are defined as follows:

- E =maximum tolerable error for the sample average, that is, the maximum acceptable difference between true average and the sample average. the maximum acceptable difference between the true average and the sample average.
- $e = E/\mu$, maximum allowable sampling error acceptable difference expressed as a fraction of μ .
- k = the total number of samples available from the same or similar lots. 69-8005-bf00d22fee60/astm-e122-07
- μ = lot or process mean or expected value of X, the result of measuring all the units in the lot or process.
- μ_0 = an advance estimate of μ .
- N = size of the lot.
- n = size of the sample taken from a lot or process.
- n_i = size of sample *j*.
- n_L = size of the sample from a finite lot (7.4).
- p' = fraction of a lot or process whose units have the nonconforming characteristic under investigation.
- p_0 = an advance estimate of p'.
- p = fraction nonconforming in the sample.
- R = range of a set of sampling values. The largest minus the smallest observation.
- R_j = range of sample *j*.
- $\vec{R} =$
 - $\sum R/k$, average of the range of k samples, all of the same size (8.2.2).
- $\sigma = 1\overline{\delta t}$ or process standard deviation of X, the result of measuring all of the units of a finite lot or process.
- σ_0 = an advance estimate of σ .

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For Annual Book of ASTM Standards , Vol 14.02.volume information, refer to the standard's Document Summary page on the ASTM website.

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- $s = \left[\sum_{k=1}^{n} (X_i \overline{X} \overline{X})^2 / (n-1)\right]^{1/2}, \text{ an estimate of the standard deviation } \sigma \text{ from n observation, } X_i, i = 1 \text{ to n.}$ $\bar{s} = \sum_{k=1}^{n} (X_i - \overline{X} - \overline{X})^2 / (n-1) = 1 \text{ to n.}$
 - $\sum_{k=1}^{\infty} S_k/k$, average s from k samples all of the same size (8.2.1).
 - = $p\bar{b}$ obled (weighted average) s from k samples, not all of the same size (8.2).
- s_j = standard derivation deviation of sample j.
 - = a factor (the 99.865th percentile of the Student's distribution) corresponding to the degrees of freedom f_o of an advance estimate σ_o (5.1).
- $V = \sigma/\mu$, the coefficient of variation of the lot or process.
- V_o = an advance estimate of V(8.3.1)., equal to δ_o/μ_o .
- $z = s/\bar{X}$, the coefficient of variation estimated from the sample.
- v_j = coefficient of variation from sample *j*. X = numerical value of the characteristic of
 - = numerical value of the characteristic of an individual unit being measured.
- $\bar{X} = ,$

 $\sum_{i=1}^{n} X_i / n_i \text{ average of } n \text{ observations, } X_i, i = 1 \text{ to n.}$

4. Significance and Use

4.1 This practice is intended for use in determining the sample size required to estimate, with <u>prescribedspecified</u> precision, a measure of quality of a lot or process. The practice applies when quality is expressed as either the lot average for a given property, or as the lot fraction not conforming to prescribed standards. The level of a characteristic may often be taken as an indication of the quality of a material. If so, an estimate of the average value of that characteristic or of the fraction of the observed values that do not conform to a specification for that characteristic becomes a measure of quality with respect to that characteristic. This practice is intended for use in determining the sample size required to estimate, with <u>prescribedspecified</u> precision, such a measure of the quality of a lot or process either as an average value or as a fraction not conforming to a specified value.

5. Empirical Knowledge Needed

5.1 Some empirical knowledge of the problem is desirable in advance.

5.1.1 We may have some idea about the standard deviation of the characteristic.

5.1.2 If we have not had enough experience to give a precise estimate for the standard deviation, we may be able to state our belief about the range or spread of the characteristic from its lowest to its highest value and possibly about the shape of the distribution of the characteristic; for instance, we might be able to say whether most of the values lie at one end of the range, or are mostly in the middle, or run rather uniformly from one end to the other (Section 9).

5.2 If the aim is to estimate the fraction nonconforming, then each unit can be assigned a value of 0 or 1 (conforming or nonconforming), and the standard deviation as well as the shape of the distribution depends only on p', the fraction nonconforming to in the lot or process. Some rough idea concerning the size of p' is therefore needed, which may be derived from preliminary sampling or from previous experience.

5.3Sketchy5.3 More knowledge is sufficient to start with, although more knowledge permits a smaller sample size. Seldom will there be difficulty in acquiring enough information to compute the required size of sample. A sample that is larger than the equations indicate is used in actual practice when the empirical knowledge is sketchy to start with and when the desired precision is critical.

5.4In any case, even with sketchy knowledge, the 5.4 The precision of the estimate made from a random sample may itself be estimated from the sample. This estimation of the precision from one sample makes it possible to fix more economically the sample size for the next sample of a similar material. In other words, information concerning the process, and the material produced thereby, accumulates and should be used.

6. Precision Desired

6.1 The approximate precision desired for the estimate must be prescribed. That is, it must be decided what maximum deviation, E, can be tolerated between the estimate to be made from the sample and the result that would be obtained by measuring every unit in the lot or process.

6.2 In some cases, the maximum allowable sampling error is expressed as a proportion, e, or a percentage, 100 e. For example, one may wish to make an estimate of the sulfur content of coal with maximum allowable error of within 1%, or e = 0.01.

7. Equations for Calculating Sample Size

7.1 Based on a normal distribution for the characteristic, the equation for the size, n, of the sample is as follows:

$$n = (3\sigma_o/E)^2$$

$\sigma \theta$

where:

 $\sigma_{\overline{a}}$ = the advance estimate of the standard deviation of the lot or process,

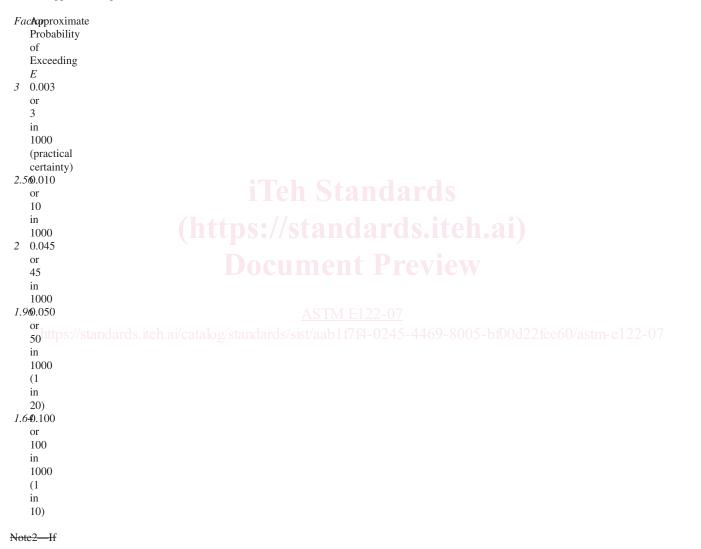
E = the maximum allowable error between the estimate to be made from the sample and the result of measuring (by the same methods) all the units in the lot or process, and

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3 = a factor corresponding to a low probability that the difference between the sample estimate and the result of measuring (by the same methods) all the units in the lot or process is greater than *E*. The choice of the factor 3 is recommended for general use. With the factor 3, and with a lot or process standard deviation equal to the advance estimate, it is *practically certain* that the sampling error will not exceed *E*. Where a lesser degree of certainty is desired a smaller factor may be used (

The multiplier 3 is a factor corresponding to a low probability that the difference between the sample estimate and the result of measuring (by the same methods) all the units in the lot or process is greater than E. The value 3 is recommended for general use. With the multiplier 3, and with a lot or process standard deviation equal to the advance estimate, it is practically certain that the sampling error will not exceed E. Where a lesser degree of certainty is desired a smaller multiplier may be used (Note 1).

NOTE1—For example, the factor<u>multiplying by</u> 2 in place of 3 gives a probability of about 45 parts in 1000 that the sampling error will exceed <u>E.E.</u> Although distributions met in practice may not be normal (Note 2),<u>normal</u>, the following text table (based on the normal distribution) indicates approximate probabilities:



<u>7.1.1 If a lot of material has a highly asymmetric distribution in the characteristic measured, the factor 3 will give a different probability, possibly much greater than 3 parts sample size as calculated in 1000 if the sample size is small. Eq 1 may not be adequate. There are two things to do when asymmetry is suspected.</u>

7.1.1.1 Probe the material with a view to discovering, for example, extra-high values, or possibly spotty runs of abnormal character, in order to approximate roughly the amount of the asymmetry for use with statistical theory and adjustment of the sample size if necessary.

7.1.1.2 Search the lot for abnormal material and segregate it for separate treatment.

7.2 There are some materials for which σ varies approximately with μ , in which case $V (= \sigma/\mu)$ remains approximately constant from large to small values of μ .

7.2.1 For the situation of 7.2, the equation for the sample size, n, is as follows: