

# SLOVENSKI STANDARD oSIST prEN IEC 61803:2020

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# Ugotavljanje močnostnih izgub v visokonapetostnih enosmernih (HVDC) pretvorniških postajah s pretvorniki s komutiranjem

Determination of power losses in high-voltage direct current (HVDC) converter stations with line-commutated converters

Bestimmung der Leistungsverluste in Hochspannungsgleichstrom-(HGÜ-)Stromrichterstationen mit netzgeführten Stromrichtern

Détermination des pertes en puissance dans les postes de conversion en courant continu à haute tension (CCHT) munis de convertisseurs commutés par le réseau

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The CENELEC members are invited to vote through CENELEC online voting system.	71f-8da1-47a9-8d98-dc5667fc5482/sist-en-iec-61803

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#### TITLE:

Determination of power losses in high-voltage direct current (HVDC) converter stations with line-commutated converters

PROPOSED STABILITY DATE: 2024

#### NOTE FROM TC/SC OFFICERS:

This CDV document, based on documents 22F/530/CD and 22F/542A/CC, was developed in accordance with the decision taken at SC 22F plenary meeting in Shanghai, China, on October 21-23, 2019 (see 22F/560/DL, Decision 2019-07, Action 2019-03).

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49 50	INTERNATIONAL ELECTROTECHNICAL COMMISSION
51 52 53 54 55 56 57	DETERMINATION OF POWER LOSSES IN HIGH-VOLTAGE DIRECT CURRENT (HVDC) CONVERTER STATIONS WITH LINE-COMMUTATED CONVERTERS
57 58	FOREWORD
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94 95 96	This second edition cancels and replaces the first edition published in 1999-02-26, Corrigendum 1:1999-10-29, Amendment 1:2010-11-25 and Amendment 2:2016-05-25. This edition constitutes a technical revision.
97	This edition includes the following significant technical changes with respect to the previous edition:
98 99 100 101	a) It is taken into account that the present thyristor production technology provides considerably less thyristor parameters dispersion comparing with the situation in 1999 when the standard was developed and therefore the production records of thyristors can be used for the power losses calculation (subclauses 5.1.7 and 5.8).
102 103	b) The correction is made concerning the calculation of the total station load losses (Cases D1 and D2 in Annex C).

104 c) The logical order of clauses, subclauses and annexes of the standard is established.

105 The committee has decided that the contents of the base publication and its amendments will 106 remain unchanged until the stability date indicated on the IEC web site under 107 "http://webstore.iec.ch" in the data related to the specific publication. At this date, the publication 108 will be

- 109 reconfirmed,
- 110 withdrawn,
- 111 replaced by a revised edition, or
- 112 amended.
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# 120DETERMINATION OF POWER LOSSES IN HIGH-VOLTAGE121DIRECT CURRENT (HVDC) CONVERTER STATIONS WITH LINE-COMMUTATED122CONVERTERS

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#### 124 **1 Scope**

125 This International Standard applies to all line-commutated high-voltage direct current (HVDC) 126 converter stations used for power exchange in utility systems. This standard presumes the use of 127 12-pulse thyristor converters but can, with due care, also be used for 6-pulse thyristor converters.

128 In some applications, synchronous compensators or static var compensators (SVC) may be 129 connected to the a.c. bus of the HVDC converter station. The loss determination procedures for 130 such equipment are not included in this standard.

This standard presents a set of standard procedures for determining the total losses of an HVDC converter station. Typical HVDC equipment is shown in figure 1. The procedures cover all parts, except as noted above, and address no-load operation and operating losses together with their methods of calculation which use, wherever possible, measured parameters.

135 Converter station designs employing novel components or circuit configurations compared to the 136 typical design assumed in this standard, or designs equipped with unusual auxiliary circuits that 137 could affect the losses, shall be assessed on their own merits.

#### 138 2 Normative references

139 The following referenced documents are indispensable for the application of this document. For 140 dated references, only the edition cited applies. For undated references, the latest edition of the 141 referenced document (including any amendments) applies.

142 IEC 60076-1, Power transformers – Part 1: General

https://standards.iteh.ai/catalog/standards/sist/19db871f-8da1-47a9-8d98-dc5667fc5482/sist-en-iec-61803-2021 143 IEC 60076-6, Power transformers – Part 6: Reactors

- 144 IEC 60633, Terminology for high-voltage direct current (HVDC) transmission
- 145 IEC 60700-1, Thyristor valves for high voltage direct current (HVDC) power transmission Part 1: 146 Electrical testing
- 147 IEC 60747-6, Semiconductor devices Part 6: Thyristors

148 IEC 60871-1, Shunt capacitors for a.c. power systems having a rated voltage above 149 1 000 V – Part 1: General

#### 150 **3 Definitions and symbols**

151 For the purpose of this International Standard, the following definitions apply:

#### 152 **3.1 Definitions**

153 **3.1.1** 

#### 154 auxiliary losses

155 electric power required to feed the converter station auxiliary loads

156 Note 1 to entry: The auxiliary losses depend on the number of converter units used and whether the station is in no-load operation or carrying load, in which case the auxiliary losses depend on the load level.

#### 158 **3.1.2**

#### 159 equipment no-load operation losses

160 losses produced in an item of equipment with the converter station energised but with the 161 converters blocked and all station service loads and auxiliary equipment connected as required for 162 immediate pick-up of load to specified minimum power

163 **3.1.3** 

#### 164 load level

this term specifies the direct current, direct voltage, firing angle, a.c. voltage, and converter transformer tap-changer position at which the converter station is operating

#### 167 **3.1.4**

#### 168 equipment operating losses

the losses produced in an item of equipment at a given load level with the converter station energized and the converters operating

#### 171 **3.1.5**

- 172 rated load
- 173 load related to operation at nominal values of d.c. current, d.c. voltage, a.c. voltage and converter 174 firing angle
- 175 Note 1 to entry: The a.c. system shall be assumed to be at nominal frequency and its 3-phase voltages are nominal and 176 balanced. The position of the tap-changer of the converter transformer and the number of a.c. filters and shunt reactive
- 176 balanced. The position of the tap-changer of the converter transformer and the number of a.c. filters and shunt reactive 177 elements connected shall be consistent with operation at rated load, coincident with nominal conditions.
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#### 178 **3.1.6**

#### 179 total station no-load operation losses

180 sum of all equipment no-load operation losses (3.1.2) and corresponding auxiliary losses (3.1.1)

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181 **3.1.7** 

#### 182 total station operating losses

183 sum of all equipment operating losses (3.1.4) and corresponding auxiliary losses (3.1.1) at a 184 particular load level

185 Note 1 to entry: An illustrative example using "Total station operating losses" and corresponding "loss evaluation" is given in Annex C, Case D1.

#### 187 **3.1.8**

#### 188 total station load losses

- total station load losses shall be calculated from the difference between total station operating
   losses (3.1.7) and total station no-load operation losses (3.1.6).
- 191 Note 1 to entry: Such calculated "total station load losses" are considered as being quantitatively equivalent to "load losses" as in conventional a.c. substation practice.
- 193 Note 2 to entry: It is recognised that some purchasers evaluate "Total station no-load operation losses" (definition 3.1.6) and total station load losses individually instead of the evaluating "Total station operating losses" (definition 3.1.7).
- 195 Note 3 to entry: An illustrative example to derive "load losses", "equivalent load losses" and corresponding "loss evaluation" is given in Annex C, case D2.

#### 197 **3.1.9**

## 198 station essential auxiliary load

load whose failure will affect the conversion capability of the HVDC converter station (e.g. valve
 cooling), as well as load that must remain working in case of complete loss of a.c. power supply
 (e.g. battery chargers, operating mechanisms)

#### 202 **3.2 Letter symbols**

- 203  $\alpha$  (trigger/firing) delay angle, in radians (rad)
- 204  $\mu$  overlap angle, in radians (rad)
- 205 f a.c. system frequency, in hertz (Hz)
- 206  $I_d$  direct current, in amperes (A)
- 207  $I_n$  harmonic r.m.s. current of order *n*, in amperes (A)
- 208  $L_1$  the inductance, in henrys (H), referred to the valve winding, between the commutating voltage 209 source and the point of common coupling between star- and delta-connected windings.  $L_1$ 210 shall include any external inductance between the transformer line-winding terminals and the 211 point of connection of the a.c. harmonic filters
- 212  $L_2$  the inductance, in henrys (H), referred to the valve winding, between the point of common 213 coupling between star- and delta-connected windings, and the valve.  $L_2$  shall include the 214 saturated inductance of the valve reactors
- 215 *m* electromagnetic notch coupling factor,  $m = L_1/(L_1 + L_2)$
- 216 *n* harmonic order
- 217 Nt the number of series-connected thyristors per valve
- 218 *P* power loss in an item of equipment, in watts (W)
- 219  $Q_n$  quality factor at harmonic order *n*
- 220 *R* resistance value, in ohms  $(\Omega)$
- 221 U<sub>d</sub> direct voltage, in volts (V)
- 222  $U_n$  harmonic r.m.s. voltage of order *n*, in volts (V)
- U<sub>vo</sub> r.m.s. value of the phase-to-phase no-load voltage on the valve side of the converter
   transformer excluding harmonics, in volts (V)
- 225  $X_n$  inductive reactance at harmonic order *n*, in ohms ( $\Omega$ )

## 5 4 General Document Previ

## 226 **4 General**

#### 227 4.1 Introduction

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Suppliers need to know in detail how and where losses are generated, since this affects component and equipment ratings. Purchasers are interested in a verifiable loss figure which allows equitable bid comparison and in a procedure after delivery which can objectively verify the guaranteed performance requirements of the supplier.

As a general principle, it would be desirable to determine the efficiency of an HVDC converter station by a direct measurement of its energy losses. However, attempts to determine the station losses by subtracting the measured output power from the measured input power should recognize that such measurements have an inherent inaccuracy, especially if performed at high voltage. The losses of an HVDC converter station at full load are generally less than 1% of the transmitted power. Therefore, the loss measured as a small difference between two large quantities is not likely to be a sufficiently accurate indication of the actual losses.

In some special circumstances it may be possible, for example, to arrange a temporary test connection in which two converters are operated from the same a.c. source and also connected together via their d.c. terminals. In this connection, the power drawn from the a.c. source equals the losses in the circuit. However, the a.c. source must also provide var support and commutating voltage to the two converters. Once again, there are practical measurement difficulties.

In order to avoid the problems described above, this standard standardizes a method of calculating the HVDC converter station losses by summing the losses calculated for each item of equipment. The standardized calculation method will help the purchaser to meaningfully compare the competing bids. It will also allow an easy generation of performance curves for the wide range of operating conditions in which the performance has to be known. In the absence of an inexpensive experimental method which could be employed for an objective verification of losses during type tests, the calculation method is the next best alternative as it uses, wherever possible, experimental - 8 -

251 data obtained from measurements on individual equipment and components under conditions 252 equivalent to those encountered in real operation.

253 It is important to note that the power loss in each item of equipment will depend on the ambient 254 conditions under which it operates, as well as on the operating conditions or duty cycles to which it is subjected. Therefore, the ambient and operating conditions shall be defined for each item of 255 256 equipment, based on the ambient and operating conditions of the entire HVDC converter station.

#### 257 4.2 Ambient conditions

258 A set of standard reference ambient conditions shall be used for determining the power losses in HVDC converter stations. 259

#### 260 4.2.1 Outdoor standard reference temperature

An outdoor ambient dry bulb temperature of 20 °C shall be used as the standard reference 261 temperature for determining the total converter station losses. Corresponding valve hall temperature 262 may be defined by the supplier if necessary. The equivalent wet-bulb temperature (where 263 264 necessary) shall be defined by the purchaser.

265 NOTE If not defined, the wet-bulb temperature is recommended to be 14 °C which corresponds to approximately 50 % 266 RH at 20 °C dry bulb temperature.

#### 267 4.2.2 Coolant standard reference temperature

Where forced cooling is used for equipment, the flow rate and temperature of the coolant can 268 influence the temperature rise and associated losses of that equipment. Therefore, the coolant 269 temperatures and flow rates established by the purchaser and the supplier shall be used as a basis 270 271 for determining the losses.

#### 4.2.3 Standard reference air pressure indards.iteh.ai) 272

273 The reference air pressure to be used for the evaluation of total converter station power losses shall 274 be the standard atmospheric pressure (101,3 kPa) corrected to the altitude of the installation in 275 auestion.

#### 276 4.3 an Operating parameters ds/sist/19db8711-8da1-47a9-8d98-dc5667fc5482/sist-en-iec-61803-2021

277 The losses of an HVDC converter station depend on its operating parameters.

278 The losses of HVDC converter stations are classified into two categories, referred to as operating 279 losses (3.1.4 and 3.1.7) and no-load operation losses (3.1.2 and 3.1.6).

280 The operating losses and auxiliary losses are affected by the load level of the station because the 281 numbers of certain types of energized equipment (for example harmonic filters and cooling 282 equipment) may depend upon the load level and because losses in individual items of equipment 283 themselves vary with the load level.

284 HVDC converter station losses shall be determined for nominal (balanced) a.c. system voltage and 285 frequency, symmetrical impedances of the converter transformer and symmetrical firing angles. The 286 transformer tap-changer shall be assumed to be in the position corresponding to nominal a.c. 287 system voltage or as decided by the control system for the defined operating condition.

The operating losses shall be determined for the load levels specified by the purchaser, or at rated 288 load if no such conditions are specified. For each load level, the valve-winding a.c. voltage, d.c. 289 290 current, converter firing angle, shunt compensation and harmonic filtering equipment shall be 291 consistent with the respective load level and other specified performance requirements, relating, for 292 example, to harmonic distortion and reactive power. Cooling and other auxiliary equipment, as 293 appropriate to the standard reference temperature (see 4.2.1 and 4.2.2), shall be assumed to be 294 connected to support the respective load level.

For the no-load operation mode, converter transformers shall be energized and the converters blocked. All filters and reactive power compensation equipment shall be assumed to be disconnected except for those which are required to sustain operation at zero load in order, for example, to meet the specified reactive power requirements. Station service loads and auxiliary equipment (e.g. cooling-water pumps) shall be assumed to be connected as required for immediate pick-up of load for the converter station (without waiting for tap changer movement) to specified minimum power.

#### 302 **5** Determination of equipment losses

#### 303 **5.1 Thyristor valve losses**

The loss production mechanisms applicable when the valves are blocked (no-load operation losses) are different from those applicable in normal operation (operating losses). Operating losses are dealt with in subclauses 5.1.1 to 5.1.10, and no-load operation losses are dealt with in 5.1.11. Auxiliary losses are dealt with in 5.8.

308 A simplified three-phase diagram of an HVDC 12-pulse converter is shown in figure 2. Individual 309 valves are marked in the order of their conduction sequence.

310 A simplified equivalent circuit of a typical valve is shown in figure 3. Symbol th combines together the effects of  $N_t$  thyristors connected in series in the valve.  $C_{AC}$  and  $R_{AC}$  are the corresponding 311 312 combined values of R-C damping circuits used for voltage sharing and overvoltage suppression. 313  $R_{\rm DC}$  represents d.c. grading resistors and other resistive components which incur loss when the valve blocks voltage. It also includes the effects of the thyristor leakage current (see 5.1.4 and 314 315 5.1.11).  $C_s$  includes both stray capacitances and surge distribution capacitors (if used).  $L_s$ represents saturable reactors used to limit the di/dt stresses to safe values and to improve the 316 distribution of fast rising voltages.  $R_s$  represents the resistances of the current conducting 317 components of the valve such as the busbars, contact resistances, resistance of the windings of the 318 319 saturable reactors etc. Power losses in the valve surge arrester (not shown) shall be neglected.

Figure 4 shows, as an example, current and voltage waveforms of valve 1 (according to figure 2) 320 321 operating in rectifier and inverter modes. In the example shown, the firing instants of the valves of 322 the upper bridge are delayed by 30° with respect to the valves of the lower bridge due to the phase 323 shift between the two secondaries. For each valve, the length of the conduction intervals is 130° 324  $(2\pi/3 + \mu)$ . During commutations the valve current is assumed, for this standard, to be changing 325 linearly whereas in reality the valve currents follow portions of sine waves. This simplification has 326 negligible effect on the resulting losses, while the trapezoidal waveform significantly simplifies the 327 calculations. The voltage blocked by the valve shows notches caused by commutations between individual valves. 328

#### 329 **5.1.1** Thyristor conduction loss per valve

This loss component is the product of the conduction current i(t) and the corresponding ideal onstate voltage as shown in figures 5 and 6. Formula  $P_{V1a}$  shall be used provided that the d.c. bridge current is well smoothed. In the event that the root sum square value of the d.c. side harmonic currents, determined in accordance with clause A.4 (annex A), exceeds 5 % of the d.c. component, formula  $P_{V1b}$  shall be used instead.

335 
$$P_{V1a} = \frac{N_t \times I_d}{3} \left[ U_0 + R_0 \times I_d \times \left(\frac{2\pi - \mu}{2\pi}\right) \right]$$

336 
$$P_{V1b} = \frac{N_t \times I_d \times U_0}{3} + \frac{N_t \times R_0}{3} \left( I_d^2 + \sum_{n=12}^{n=48} I_n^2 \right) \left( \frac{2\pi - \mu}{2\pi} \right)$$

337 where

338  $U_0$  is the current-independent component of the on-state voltage of the average thyristor (see 339 note below), in volts;