
Thermal performance of buildings and materials — Determination of specific airflow rate in buildings — Tracer gas dilution method

*Performance thermique des bâtiments et des matériaux —
Détermination du débit d'air spécifique dans les bâtiments —
Méthode de dilution de gaz traceurs*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see www.iso.org/patents).

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation on the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see the following URL: www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/TC 163, *Thermal performance and energy use in the built environment*, Subcommittee SC 1, *Test and measurement methods*.

This third edition cancels and replaces the second edition (ISO 12569:2012), which has been technically revised.

Introduction

The aim of ventilation is to maintain a proper hygienic status of the room by introducing outdoor air and diluting contaminants, heat, moisture or odour generated in the room, and evacuating them. In terms of energy savings, it is also important to keep the ventilation at the required rate, in order to reduce heat loss and heat gain under air conditioning as much as possible. Measurement of airflow rates is often necessary, for example, to check if the performance of a ventilation system is as intended, to assess the source strength of contaminants, to ensure that contaminants are properly eliminated, etc. The methods described here can be used to measure the ventilation rate or the specific airflow rate.

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Thermal performance of buildings and materials — Determination of specific airflow rate in buildings — Tracer gas dilution method

1 Scope

This document establishes methods to obtain the ventilation rate or specific airflow rate in a building space (which is considered to be a single zone) using a tracer gas.

The measurement methods apply for spaces where the combined conditions concerning the uniformity of tracer gas concentration, measurement of the exhaust gas concentration, effective mixed zone and/or fluctuation of ventilation are satisfied.

This document provides three measurement methods using a tracer gas: concentration decay method, continuous dose method, and constant concentration method.

NOTE Specific measurement conditions are given in [Table 1](#).

2 Normative references

There are no normative references in this document.

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- ISO Online browsing platform: available at <http://www.iso.org/obp>
- IEC Electropedia: available at <http://www.electropedia.org/>

3.1

single zone

V

space which only exchanges air with the outside

3.2

effective mixed zone

V_{emz}

space within a *single zone* ([3.1](#)), excluding sealed furniture or storage space, in which *tracer gas* ([3.6](#)) supplied to the zone is regarded as uniformly distributed

Note 1 to entry: Measured in cubic metres.

Note 2 to entry: Forced mixing of air in the zone is often needed to keep uniform tracer gas concentration.

3.3

ventilation rate

Q_v

total volume of air passing through the zone to the outside per unit of time

Note 1 to entry: Measured in m³/s or m³/h.

**3.4
specific airflow rate**

N
ratio of the *ventilation rate* (3.3) of a zone to the volume of the *effective mixed zone* (3.2), per second or per hour

**3.5
building envelope**
boundary or barrier separating the interior volume of a building from the outside environment

**3.6
tracer gas**
gas that can be mixed with air and measured in very small concentration in order to study airflow rate

**3.7
concentration decay method**
method by which the *specific airflow rate* (3.4) is obtained from the decaying curve of concentration observed after the end of the injection of *tracer gas* (3.6)

**3.8
continuous dose method**
method by which the *ventilation rate* (3.3) is obtained from the concentration resulting from continuous generation or injection of the *tracer gas* (3.6)

**3.9
constant concentration method**
method by which the *ventilation rate* (3.3) is obtained from the injection rate of *tracer gas* (3.6) dosed for constant concentration in the space (standards.iteh.ai)

4 Measurement method and its selection
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4.1 General

Selection of a measurement method and data processing depends on the building structure, ventilation system and measurement instrument employed. One of the three measurement methods (concentration decay method, continuous dose method and constant concentration method) is used to estimate the ventilation rate or specific airflow rate. The concentration decay method has a limited measurement time of up to several hours while the continuous dose and constant concentration methods can provide a longer measurement time up to several weeks. The guideline of selection of the method and what is measured by the method is listed in [Table 1](#).

In order to improve the accuracy of deriving the ventilation rate or specific airflow rate, it is sometimes necessary to devise measures that approximate prerequisite conditions demanded of measurement methods. In particular, if a measurement method were used that requires uniformity of concentration in the effective mixed zone, it would be preferable to forcibly mix the internal air. In general, forced mixing of internal air has little effect on ventilation rate or specific airflow rate, but there is a risk that forced mixing affects the measured ventilation rate if natural ventilation due to temperature differences predominates and the temperature within the room is distributed significantly, or if airflow emitted from a fan for the purpose of mixing air directly impinges on the leakage areas in buildings. In such instances, a mixing system needs to be improved or it would be recommended to select a measurement method that could ensure uniformity of concentration without mixing.

In [Table 1](#), specifications for the various applications are described as follows.

- “Room concentration can be maintained uniform at initial stage only” means making the concentration in the effective mixed zone uniform by a method such as forced mixing when supplying a tracer gas into the zone, but allowing the concentration to be distributed in principle with the measurement.

- If it is specified that “room concentration can be maintained uniform at all times”, continuous forced mixing of air in the effective mixed zone is preferable. However, if the constant concentration method is used, and if concentration is controlled by injecting the tracer gas at several places and air is sampled at several locations, it is possible to assume that concentration is uniform without mixing.
- “Average exhaust concentration can be measured” can either mean instances in which concentration in an effective mixed zone is made uniform using mixing, or instances whereby the pressure inside a zone is kept lower than the outside when using the exhaust ventilation system, or the leakage area is extremely low so the exfiltration rate may be ignored and exhaust pathways may be specified beforehand.
- When using measurement methods that require the “known volume of an effective mixed zone”, the volume of the effective mixed zone can be estimated using room dimensions. However, when using the corresponding average inverse concentration method and average concentration method, high accuracy for estimating the volume of an effective mixed zone is not needed if a sufficiently long time is taken to evaluate the ventilation rate.
- Measurement methods that can be applied in instances where “fluctuation in ventilation rate can be ignored” are designed on the assumption that the ventilation rate or specific airflow rate over time does not change.
- The tracer gas volume is defined as the value of exhaust temperature converted into density. When the room air is mixed well, the room temperature approximately matches the exhaust temperature.
- In addition to the measurement methods in [Table 1](#), there is an intermittent dose method that allows the measurement of the volume of an effective mixed zone and ventilation rate at the same time.
- For measurement of ventilation rate among the other measurements, if volume of an effective mixed zone is known, the ventilation rate can be obtained by multiplying the volume of the effective mixed zone by the specific airflow rate, and then converting to ventilation rate.

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Table 1 — Relationship of method, application and estimated quantities

Method		Application and measured quantities						
		Application					What is measured	
		Room concentration can be maintained uniform at initial stage only	Room concentration can be maintained uniform at all times	Average exhaust concentration can be measured	Known volume of effective mixed zone	Fluctuation in ventilation rate can be ignored	Ventilation rate or specific air-flow rate	Flexibility to significantly transient ventilation rate
Concentration decay method	Two-point decay method	—	•	—	—	—	Specific air-flow rate	Δ
	Multi-point decay method	—	•	—	—	•	Specific air-flow rate	□
	Step-down exhaust concentration method	•	—	•	—	•	Specific air-flow rate	□
	Pulse method	—	—	•	—	•	Ventilation rate	□
Continuous dose method	Average of inverse concentration method	—	•	—	—	•	Ventilation rate	Δ
	Average concentration method	—	•	—	•	•	Ventilation rate	□
	Stationary concentration method	—	—	•	—	•	Ventilation rate	□
Constant concentration method		—	•	—	—	—	Ventilation rate	Δ

“•” indicates the necessary condition for the application to measure the quantity according to each method.
 “—” indicates that it is not a necessary condition for each method to be applied.
 “Δ” indicates reasonable applicability because the basic equation to derive the measurement method permits temporal change in ventilation rate.
 “□” indicates difficulty because the basic equation to derive the measurement method assumes constant ventilation rate.

4.2 Concentration decay method

4.2.1 Principle

At the start of the test, the tracer gas is supplied in the zone where the ventilation rate is to be evaluated based on the concentration decay data obtained. In case of the forced mixing for uniform distribution or if the average exhaust concentration can be measured, the measurement point can be limited to one.

The amount of tracer gas needed is very small for one measurement, and it is not required to accurately measure the amount of injected gas except for the pulse method.

The basic equation that can be commonly applied to the methods is as given in [Formula \(1\)](#), expressed in m³/h or m³/s:

$$\frac{dV_{\text{gas}}(t)}{dt} = -C_E(t)Q_v(t) \quad (1)$$

where

t is the time, in h or s;

$V_{\text{gas}}(t)$ is the total volume of tracer gas in a zone at time t $\left[= \iiint_V C(x,t) dV \right]$, in m³;

x is the location in a zone;

$C(x, t)$ is the concentration at t, x in a zone, in m³/m³;

$Q_v(t)$ is the ventilation rate at t , in m³/h;

$C_E(t)$ is the average exhaust concentration at “ t ”, in m³/m³.

NOTE [Formula \(1\)](#) assumes that indoor-outdoor air density difference, mostly resulting from temperature difference, can be neglected.

4.2.2 Two-point decay method (standards.iteh.ai)

With the concentration in an effective mixed zone continuously made uniform, the time average air change rate of measuring period is calculated from the measurement start point to the end point. It is not necessary for the specific airflow rate to be constant during measuring.

[Formula \(2\)](#) is established from the above conditions:

$$\begin{aligned} V_{\text{gas}}(t) &= V_{\text{emz}} \cdot C(t) \\ C_E(t) &= C(t) \end{aligned} \quad (2)$$

where

$C(t)$ is the concentration in an effective mixed zone (uniform distribution) at t , in m³/m³;

V_{emz} is the volume of an effective mixed zone (no time changes are assumed)
 $\left[= \iiint_V C(x,t) dV / C_E(t) \right]$, in m³.

[Formula \(1\)](#) and [Formula \(2\)](#) provide [Formula \(3\)](#) to give [Formula \(4\)](#):

$$\int_{t_1}^{t_2} \frac{dC}{C(t)} = - \int_{t_1}^{t_2} \frac{Q(t)}{V_{\text{emz}}} dt \quad (3)$$

$$\bar{N} = \frac{1}{t_2 - t_1} \log_e \frac{C(t_1)}{C(t_2)} \quad (4)$$

where

t is the time, in h;

t_1 is the measurement start point, in h;

t_2 is the measurement end point, in h;

\bar{N} is the time-mean specific airflow rate $\left[= \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} \frac{Q(t)}{V_{emz}} dt \right]$, in 1/h.

Based on the measured concentration data of two different time points, the time average specific airflow rate during measuring period is calculated for that period. During the measurement period, the concentration in the effective mixed zone shall be uniformly maintained. It is necessary for the accurate measuring of specific airflow rate that the difference in concentration between the measurement start point and end point be sufficiently greater than the concentration measurement error.

4.2.3 Multipoint decay method

Specific airflow rate is calculated when the concentration distribution in an effective mixed zone is maintained uniform and the ventilation rate does not fluctuate over time.

[Formula \(5\)](#) is obtained when the ventilation rate in [Formula \(3\)](#) is made constant and the formula is transformed:

$$\log_e C(t) = \log_e C(t_1) - N(t - t_1) \tag{5}$$

where

N is the specific airflow rate, in h.

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Specific airflow rate is calculated by applying the measured data of concentration using the least square method to a straight line shown in [Formula \(5\)](#). The precondition that specific airflow rate does not fluctuate over time is confirmed when $\log_e C(t)$ is plotted against t and there is a linear relationship. Lack of a linear relationship indicates that ventilation rate is not constant, so the specific airflow rate obtained using this method is not the time-mean specific airflow rate. In this instance, the two-point decay method should be applied.

4.2.4 Step-down exhaust concentration method

The specific airflow rate is calculated when the average exhaust concentration is measurable, the distribution of the concentration in an effective mixed zone at the measurement start point is uniform, and the ventilation rate does not fluctuate over time. It can also be applied when the concentration is distributed after the start of measuring. Simultaneous measurement with the mean age of air distribution is possible.

When time is integrated up to ∞ by making constant the ventilation rate in [Formula \(1\)](#), [Formula \(6\)](#) is obtained:

$$\int_{t_1}^{\infty} dV_{\text{gas}}(t) = Qv \int_{t_1}^{\infty} C_E(t) dt \quad (6)$$

If the concentration in an effective mixed zone is made uniform at the measurement start point, the result is

$$V_{\text{gas}}(t_1) = V_{\text{emz}} \cdot C(t_1)$$

and after sufficient time has elapsed, the result is

$$V_{\text{gas}}(\infty) = 0$$

which provides [Formula \(7\)](#):

$$N = \frac{c(t_1)}{\int_{t_1}^{\infty} C_E(t) dt} \quad (7)$$

That is, the reciprocal value to the mean local age of air in the exhaust outlet becomes the specific airflow rate in the room. In the event of multiple exhaust outlets, the average exhaust concentration weighted depending on the exhaust airflow rate at each exhaust outlet is used.

NOTE Refer to [Annex F](#) if the difference between the exhaust temperature and room temperature cannot be ignored.

4.2.5 Pulse method

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The ventilation rate is calculated when the average exhaust concentration is measurable and the ventilation rate does not fluctuate over time. The tracer gas volume supplied at the measurement start point needs to be accurately evaluated, but the concentration distribution in a zone does not need to be uniform.

In this instance, in [Formula \(6\)](#), $V_{\text{gas}}(t_1)$ is already known, and after sufficient time has elapsed, the result is

$$V_{\text{gas}}(\infty) = 0$$

which provides [Formula \(8\)](#):

$$Q_v = \frac{V_{\text{gas}}(t_1)}{\int_{t_1}^{\infty} C_E(t) dt} \quad (8)$$

where

$V_{\text{gas}}(t)$ is the tracer gas volume (= supplied tracer gas volume) retained in the room at the measurement start time t_1 , in m^3 .

NOTE For the tracer gas volume, a value of exhaust temperature converted into density is used.

4.3 Continuous dose method

4.3.1 Principle

With the tracer gas being supplied continuously in the zone, the ventilation rate is measured by the amount of the dosage and concentration measurement data. If a measurement method that requires uniformly distributed concentration throughout the effective mixed zone with the tracer gas supplied is used, it normally requires multiple concentration monitoring points to verify the uniform distribution of the concentration. The amount of the tracer gas supplied increases as the measurement time extends; however, the method can be applied to measurement that extends for a long time. The passive measurement that uses carbon dioxide generated by exhalation of residents as the tracer gas is also one of the continuous concentration methods.

The basic formula that can be commonly applied to the methods is as given in [Formula \(9\)](#):

$$\frac{dV_{\text{gas}}(t)}{dt} = m(t) - C_E(t)Q_v(t) \tag{9}$$

where

$m(t)$ is the dosage of tracer gas at t , in m^3/h .

4.3.2 Average inverse concentration method

The time-mean specific airflow rate is calculated from the start to the end of measuring, where the concentration distribution in an effective mixed zone is maintained uniform. It is not necessary for the ventilation rate to be constant during measuring, but the instantaneous concentration during measurement, the instantaneous dosage of tracer gas, and the volume of the effective mixed zone are required.

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[Formula \(10\)](#) is established based on the assumed conditions:

$$\begin{aligned} V_{\text{gas}}(t) &= V_{\text{emz}} \cdot C(t) \\ C_E(t) &= C(t) \end{aligned} \tag{10}$$

where

$C(t)$ is the concentration in an effective mixed zone (uniform distribution) at t , in m^3/m^3 ;

V_{emz} is the volume of an effective mixed zone, in m^3 .

[Formula \(9\)](#) and [Formula \(10\)](#) provide [Formula \(11\)](#), which gives [Formula \(12\)](#):

$$V_{\text{emz}} \int_{t_1}^{t_2} \frac{dC}{C(t)} = \int_{t_1}^{t_2} \frac{m(t)}{C(t)} dt - \int_{t_1}^{t_2} Q_v(t) dt \tag{11}$$

$$\overline{Q_v} = \left[\frac{m}{C} \right] + \frac{V_{\text{emz}}}{t_2 - t_1} \log_e \frac{C(t_1)}{C(t_2)} \tag{12}$$

where

t is the time, in h;

t_1 is the measurement start point, in h;

t_2 is the measurement end point, in h;

\bar{Q}_v is the time-mean specific airflow rate $\left[= \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} Q_v(t) dt \right]$, in m³/h;

$$\left[\frac{\bar{m}}{\bar{C}} \right] = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} \frac{m(t)}{C(t)} dt, \text{ in m}^3/\text{h}.$$

$\overline{(m/C)}$ is in general different to (\bar{m}/\bar{C}) . When the tracer gas dose during measuring is constant and is m , $\overline{(m/C)}$ is replaced by $(1/\bar{C})$. When there is sufficient measuring time, the effect of the second term on the right side in [Formula \(12\)](#) is diminished; so in such circumstance, this method may be applied also to instances where sufficient accuracy is not obtained for estimation of the volume of the effective mixed zone. Immediately after the start of tracer gas dosing, the concentration is generally small, which tends to have a strong effect of delaying the response to the concentration measurement system including the sampling system, and causing errors in the measured concentration value, so at this point data shall not be used for calculating the ventilation rate.

4.3.3 Average concentration method

The ventilation rate that does not fluctuate over time when the concentration distribution in an effective mixed zone has been made constantly uniform is calculated. When there is sufficient measuring time, calculation is possible using only the time-mean tracer gas dose and time-mean concentration during the measuring.

Once [Formula \(10\)](#) is supposed for [Formula \(9\)](#), integration in the measuring time provides [Formula \(13\)](#):

$$\int_{t_1}^{t_2} C(t) Q(t) dt = \int_{t_1}^{t_2} m(t) dt - V_{\text{emz}} \int_{t_1}^{t_2} dC \quad (13)$$

If $Q_v(t) = Q_v$ without the ventilation rate changing over time, [Formula \(14\)](#) is obtained:

$$Q = \frac{\bar{m}}{\bar{C}} - \frac{V_{\text{emz}}}{t_2 - t_1} \left[\frac{C(t_2) - C(t_1)}{\bar{C}} \right] \quad (14)$$

where

$$\bar{m} = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} m(t) dt, \text{ in m}^3/\text{h};$$

$$\bar{C} = \frac{1}{t_2 - t_1} \int_{t_1}^{t_2} C(t) dt, \text{ in m}^3/\text{m}^3.$$

When there is sufficient measuring time, the effect of the second term in [Formula \(14\)](#) is relatively minor and can be ignored. However, in the event that the ventilation rate changes over time, if the mean value theorem in [Formula \(13\)](#) were applied, [Formula \(15\)](#) would be obtained.

$$Q_v(\xi) = \frac{\bar{m}}{\bar{C}} - \frac{V_{\text{emz}}}{t_2 - t_1} \left[\frac{C(t_2) - C(t_1)}{\bar{C}} \right], \quad t_1 \leq \xi \leq t_2 \quad (15)$$

The ventilation rate obtained in [Formula \(15\)](#) provides the ventilation rate at a time during measuring, but it does not end up as the time-mean ventilation rate. The ventilation rate obtained from [Formula \(15\)](#)