INTERNATIONAL STANDARD

ISO 10110-12

Third edition 2019-11

Optics and photonics — Preparation of drawings for optical elements and systems —

Part 12: **Aspheric surfaces**

Optique et photonique — Préparation des dessins pour éléments et systèmes optiques —

Partie 12: Surfaces asphériques

Document Preview

ISO 10110-12:2019

https://standards.1teh.a1/catalog/standards/1so/03c3a0db-4920-4e35-9db6-b/07c6301119/1so-10110-12-2019



iTeh Standards (https://standards.iteh.ai) Document Preview

ISO 10110-12:2019

https://standards.iteh.ai/catalog/standards/iso/03c3a0db-4920-4e35-9db6-b707c6301119/iso-10110-12-2019



COPYRIGHT PROTECTED DOCUMENT

© ISO 2019

All rights reserved. Unless otherwise specified, or required in the context of its implementation, no part of this publication may be reproduced or utilized otherwise in any form or by any means, electronic or mechanical, including photocopying, or posting on the internet or an intranet, without prior written permission. Permission can be requested from either ISO at the address below or ISO's member body in the country of the requester.

ISO copyright office CP 401 • Ch. de Blandonnet 8 CH-1214 Vernier, Geneva Phone: +41 22 749 01 11 Fax: +41 22 749 09 47 Email: copyright@iso.org

Website: www.iso.org Published in Switzerland

Foreword		Page
		iv
1 9	Scope	1
2	Normative references	1
3	Terms and definitions	1
2	Mathematical description of aspheric surfaces 4.1 Coordinate system 4.2 Sign conventions 4.3 Surface descriptions 4.3.1 General 4.3.2 Surface description — Rotationally invariant (h² = x² + y²) 4.3.3 Surface description — Rotationally variant	
]]	Indications in drawings 5.1 Indication of the theoretical surface 5.2 Indication of surface form tolerances 5.3 Indication of centring tolerances 5.4 Indication of surface imperfection and surface texture tolerances	10 11 11
(Examples 6.1 Parts with rotationally invariant surfaces 6.2 Parts with rotationally variant surfaces	11
Annex A	A (informative) Summary of aspheric surface types	19
Annex l	B (informative) Description of orthonormal in slope aspheres	22
	C (informative) Description of orthonormal in amplitude aspheres	
Bibliog	raphy Document Freview	26

ISO 10110-12:2019

https://standards.iteh.ai/catalog/standards/iso/03c3a0db-4920-4e35-9db6-b707c6301119/iso-10110-12-2019

Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular, the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see www.iso.org/patents).

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation of the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/TC 172, *Optics and photonics*, Subcommittee SC 1, *Fundamental standards*.

This third edition cancels and replaces the second edition (ISO 10110-12:2007), which has been technically revised. It also incorporates the Amendment ISO 10110-12:2007/Amd.1:2013.

The main changes compared to the previous edition are as follows:

- a) The document has been updated with respect to surface form tolerances as described in ISO 10110-5.
- b) The reference to the new part ISO 10110-19 has been added.
- The document has been restructured.
- d) A few surface descriptions have been added.

A list of all the parts in the ISO 10110 series can be found on the ISO website.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Optics and photonics — Preparation of drawings for optical elements and systems —

Part 12:

Aspheric surfaces

1 Scope

This document specifies rules for presentation of aspheric surfaces and surfaces with low order symmetry such as cylinders and toroids in the ISO 10110 series, which standardizes drawing indications for optical elements and systems. It also specifies sign conventions and coordinate systems.

This document does not apply to off-axis aspheric and discontinuous surfaces such as Fresnel surfaces or gratings.

NOTE For off-axis aspheric and non-symmetric surfaces, see ISO 10110-19.

This document does not specify the method by which conformity with the specifications is tested.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 1101:2017, Geometrical product specifications (GPS) — Geometrical tolerancing — Tolerances of form, orientation, location and run-out $\underline{|SO||10110-12:2019}$

ISO 10110-1, Optics and photonics — Preparation of drawings for optical elements and systems — Part 1: General

ISO 10110-5, Optics and photonics — Preparation of drawings for optical elements and systems — Part 5: Surface form tolerances

ISO 10110-6, Optics and photonics — Preparation of drawings for optical elements and systems — Part 6: Centring tolerances

ISO 10110-7, Optics and photonics — Preparation of drawings for optical elements and systems — Part 7: Surface imperfections

ISO 10110-8, Optics and photonics — Preparation of drawings for optical elements and systems — Part 8: Surface texture

3 Terms and definitions

No terms and definitions are listed in this document.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- ISO Online browsing platform: available at https://www.iso.org/obp
- IEC Electropedia: available at http://www.electropedia.org/

4 Mathematical description of aspheric surfaces

4.1 Coordinate system

Aspheric surfaces are described in a right-handed, orthogonal coordinate system in which the Z axis is the optical axis.

Unless otherwise specified, the Z axis is in the plane of the drawing and runs from left to right; if only one cross section is drawn, the Y axis is in the plane of the drawing and is oriented upwards.

The origin of the coordinate system is at the vertex of the aspheric surface (see Figure 1).

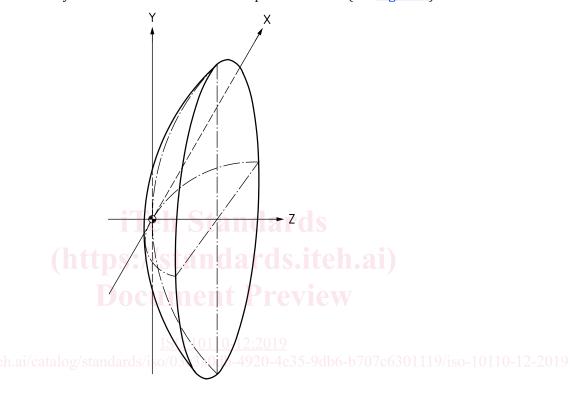


Figure 1 — Coordinate system

4.2 Sign conventions

As shown later in this document, the various types of aspheric surfaces are given by mathematical formulae. In the drawings the chosen formula and the corresponding constants and coefficients are specified. To achieve unambiguous indications of the surfaces, sign conventions for the constants and coefficients shall be introduced.

The sign of the radius of curvature is positive if the centre of curvature is to the right of the vertex, and negative if the centre of curvature is to the left of the vertex.

The sagitta of a point of the aspheric surface is positive if this point is to the right of the vertex (XY plane) and negative if it is to the left of the vertex (XY plane).

NOTE 1 In this case, "left" and "right" presume Z is increasing from left to right. When the Z axis is reversed as a result of a reflection (a 180-degree rotation about the Y axis), the sign convention for radius and sagitta is also reversed. This is discussed further in 4.3.

NOTE 2 This is the default sign convention, assuming no coordinate system according to ISO 10110-1:2019, 5.3 has been defined for the surface of interest. See ISO 10110-1 for more information about defining local coordinate systems.

4.3 Surface descriptions

4.3.1 General

The phrase "aspheric surfaces" is commonly used in optics to describe rotationally invariant surfaces such as are described below in 4.3.2. Surface descriptions for surfaces which are not rotationally invariant such as cylindrical surfaces are described in 4.3.3. More complex optical surfaces can be described using the methods given in ISO 10110-19.

Surface description — **Rotationally invariant** $(h^2 = x^2 + y^2)$ 4.3.2

4.3.2.1 Aspheric surface described by a conic section and a power series

The aspheric surface description consists of a conic part and a power series where the axis of rotation is the Z axis.

$$z(h) = \frac{h^2}{R\left[1 + \sqrt{1 - (1 + \kappa)\left(\frac{h}{R}\right)^2}\right]} + \sum_{i=2}^n A_{2i}h^{2i}$$
 (1)

where

is the sagitta; Z

is surface height perpendicular to Z-axis $(h \ge 0)$;

is the radius of curvature of the base sphere;

is the conic constant; Ocument Preview

is the aspheric coefficient.

https://Where the basic conic formula behaves as follow: 4920-4e35-9db6-b707c6301119/iso-10110-12-2019

 $\kappa > 0$ oblate ellipse;

 $\kappa = 0$ circle:

 $-1 < \kappa < 0$ prolate ellipse;

parabola: $\kappa = -1$

 $\kappa < -1$ hyperbola.

NOTE 1 The formula of second order can also be used without the power series.

NOTE 2 In three dimensions, the conic formula shapes are called ellipsoid, sphere, paraboloid, and hyperboloid.

For an example drawing, see Figure 4.

ISO 10110-12:2019(E)

An extended version with the complete power series of this description is described in Formula (2).

$$z(h) = \frac{h^2}{R \left[1 + \sqrt{1 - (1 + \kappa) \left(\frac{h}{R}\right)^2} \right]} + \sum_{i=1}^{n} A_i h^i$$
 (2)

In a special version this formula describes an axicon:

$$z(h) = A_1 h \tag{3}$$

Care should be taken that the signs of the power series named formulae z(h) are in accordance with the conventions defined in 4.1 and 4.2.

In the case where the direction of the Z axis is reversed, but the lens stays unchanged, the signs of the radius of curvature and of the aspheric coefficients shall be changed. The signs of the conic constants remain unchanged.

4.3.2.2 Aspheric surface described by a conic section and orthogonal polynomials

4.3.2.2.1 Orthonormal in slope aspheres with spherical base

A surface of higher order can also be generated by combining a spherical surface with a polynomial of the following kind, which has orthonormal derivatives.

$$z(h) = \frac{h^2}{R\left[1 + \sqrt{1 - \left(\frac{h}{R}\right)^2}\right]} + \frac{w^2 \left[1 - w^2\right]}{\sqrt{1 - \left(\frac{h}{R}\right)^2}} \sum_{m=0}^{n} B_m Q_m^{\text{bfs}}(w^2)$$
(4)

where

R is the radius of curvature of the base sphere;

h is the surface height:

 h_0 marks the upper limit of h; and

w (normalized surface height) is defined as $w = \frac{h}{h_0}$;

 $B_{\rm m}$ is the coefficient; and

 $Q_{\rm m}^{\rm bfs}$ is the polynomial term.

The description z is valid for $0 \le h \le h_0$ only. The formula for the polynomial terms is

$$Q_{m+1}^{\text{bfs}}\left(w^{2}\right) = \left[P_{m+1}\left(w^{2}\right) - g_{m}Q_{m}^{\text{bfs}}\left(w^{2}\right) - k_{m-1}Q_{m-1}^{\text{bfs}}\left(w^{2}\right)\right]/l_{m+1}$$
(5)

starting with

$$Q_0^{\text{bfs}}\left(w^2\right) = 1 \tag{6}$$

$$Q_1^{\text{bfs}}\left(w^2\right) = \frac{1}{\sqrt{19}} \left(13 - 16w^2\right) \tag{7}$$

$$Q_2^{\text{bfs}}\left(w^2\right) = \sqrt{\frac{2}{95}} \left[29 - 4w^2 \left(25 - 19w^2\right)\right] \tag{8}$$

$$P_{m+1}(w^2) = (2-4w^2)P_m(w^2) - P_{m-1}(w^2)$$
(9)

starting with

$$P_0\left(w^2\right) = 2\tag{10}$$

$$P_{1}\left(w^{2}\right) = 6 - 8w^{2} \tag{11}$$

These auxiliary polynomials have to be solved in the order given here and are valid for $m \ge 2$.

$$k_{m-2} = -m(m-1)/2l_{m-2} \tag{12}$$

$$g_{m-1} = -(1 + g_{m-2}k_{m-2})/l_{m-1}$$
(13)

$$l_{m} = \left[m(m+1) + 3 - g_{m-1}^{2} - k_{m-2}^{2} \right]^{\frac{1}{2}}$$
(14)

starting with

iTeh Standards

$$g_0 = -\frac{1}{2}$$
 (https://standards.iteh.ai) (15)

$$l_0 = 2$$
 Document Preview (16)

$$l_1 = \frac{1}{2}\sqrt{19}$$
 [ISO 10110-12:2019] (17) adards.iteh.ai/catalog/standards/iso/03c3a0db-4920-4e35-9db6-b707c6301119/iso-10110-12-2019

NOTE 1 $Q_2^{\text{bfs}}(w^2)$ is given above to be used as a check of the recursion algorithm provided in Formulae (5) through (17). See also Annex B.

NOTE 2 "bfs" is an abbreviation for "best fit sphere", which matches the sag of the aspherical surface at the vertex and h_0 .

For an example drawing, see Figure 5.

4.3.2.2.2 Orthonormal in slope aspheres with conic base

It is also possible to generate a surface by combining a conical surface with a polynomial of the same kind as in <u>Formula (4)</u>. This kind is also an orthonormal set of polynomials.

$$z(h) = \frac{h^2}{R \left[1 + \sqrt{1 - (1 + \kappa) \left(\frac{h}{R}\right)^2} \right]} + \frac{w^2 \left[1 - w^2 \right]}{\sqrt{1 - \left(\frac{h}{R}\right)^2}} \sum_{m=0}^{n} B_m Q_m^{\text{bfs}} \left(w^2 \right)$$
(18)

ISO 10110-12:2019(E)

where

R is the radius of curvature of the base sphere;

h is the surface height;

 h_0 marks the upper limit of h;

w (normalized surface height) is defined as $w = \frac{h}{h_0}$;

 κ is the conic constant;

 $B_{\rm m}$ are the coefficients; and

 $Q_{\rm m}^{
m bfs}$ are the polynomial terms.

4.3.2.2.3 Orthonormal in amplitude aspheres

A surface of higher order can also be generated by combining a conical surface with a polynomial of the following kind, which has orthonormal amplitudes.

$$z(h) = \frac{h^2}{R \left[1 + \sqrt{1 - (1 + \kappa) \left(\frac{h}{R}\right)^2} \right]} + w^4 \sum_{m=0}^{n} C_m Q_m^{\text{con}} \left(w^2\right)$$
ere

(19)

where

R is the radius of curvature of the base sphere;

h is the surface height;

ISO 10110-12:2019

 h_{tt} h_0 /stan marks the upper limit of h; and h_0 /stan marks the upper limit of h.

w (normalized surface height) is defined as
$$w = \frac{h}{h_0}$$
;

 κ is the conic constant;

 $C_{\rm m}$ are the coefficients; and

 $Q_{\rm m}^{\rm con}$ are the polynomial terms.

The formula for the polynomial terms is

$$Q_m^{\text{con}}\left(w^2\right) = T_m\left(2w^2 - 1\right) \tag{20}$$

starting with

$$Q_0^{\text{con}}\left(w^2\right) = 1\tag{21}$$

$$Q_1^{\text{con}}(w^2) = -(5 - 6w^2) \tag{22}$$

$$Q_2^{\text{con}}(w^2) = 15 - 14w^2(3 - 2w^2) \tag{23}$$

$$T_{m}(w^{2}) = \left[\left(b(m) + c(m)w^{2} \right) T_{m-1}(w^{2}) - d(m) T_{m-2}(w^{2}) \right] / a(m)$$
(24)

starting with

$$T_0\left(w^2\right) = 1\tag{25}$$

$$T_1(w^2) = 3w^2 - 2$$
 (26)

These auxiliary polynomials have to be solved in the order given here and are valid for $m \ge 2$.

$$a(m) = 2m(m+4)(2m+2) \tag{27}$$

$$b(m) = -32m - 48 \tag{28}$$

$$c(m) = (2m+2)(2m+3)(2m+4)$$
(29)

$$d(m) = 2(m-1)(m+3)(2m+4)$$
(30)

NOTE 1 $Q_0^{\text{con}}(w^2)$, $Q_1^{\text{con}}(w^2)$ and $Q_2^{\text{con}}(w^2)$ are given above to be used as a check of the recursion algorithm provided in Formulae (20) through (30). See also Annex C.

NOTE 2 The polynomial form given here is identical to Zernike radial polynomial expansion $R_{2n}^q\left(w^2\right)$ of order q=4 correlated to ISO/TR 14999-2 as $w^4Q_m^{con}\left(w^2\right)=R_{2n}^4\left(w^2\right)$ with n=m+2, and m=0,1,2,3,4,5,6 ...

NOTE 3 Instead of using the recursion algorithm above, for lower orders of m ($m \le 8$), the polynomials can easily be computed using the formula $Q_m^{con}\left(w^2\right) = \sum_{s=0}^m (-1)^s \frac{(2m+4-s)!}{s!(m+4-s)!(m-s)!} w^{2(m-s)}$.

For an example drawing, see Figure 6.

4.3.3 Surface description — Rotationally variant

4.3.3.1 Centred quadrics

In the coordinate system given in 4.1, the formulae of the surfaces of second order which fall within the scope of this document are derived from the canonical forms

$$\frac{x^2}{a^2} + \frac{y^2}{h^2} + \frac{z^2}{c^2} = 1$$
 for centered quadrics (31)

where

a, b are real or imaginary constants;

c is a real constant.