
**Thermal insulation — Test method
for thermal diffusivity — Periodic
heat method**

*Isolation thermique — Méthode d'essai pour la diffusivité thermique
— Méthode de chauffage périodique*

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular, the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

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For an explanation of the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT), see www.iso.org/iso/foreword.html.

This document was prepared by Technical Committee ISO/TC 163, *Thermal performance and energy use in the built environment*, Subcommittee SC 1, *Test and measurement methods*.

Any feedback or questions on this document should be directed to the user's national standards body. A complete listing of these bodies can be found at www.iso.org/members.html.

Thermal insulation — Test method for thermal diffusivity — Periodic heat method

1 Scope

This document specifies a periodic heat method for measurement of the thermal diffusivity of thermal insulation material in the shape of a flat plate.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 8302:1991, *Thermal insulation — Determination of steady-state thermal resistance and related properties — Guarded hot plate apparatus*

3 Terms and definitions

For the purposes of this document, the following terms and definitions apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- ISO Online browsing platform: available at <https://www.iso.org/obp>
- IEC Electropedia: available at <http://www.electropedia.org/>

3.1

phase

quantity that shows the stage of progress in one *period* (3.5) of wave motion and other periodic phenomenon

EXAMPLE $\omega t + \varphi_1$ in $y = A \sin(\omega t + \varphi_1)$ is the phase.

3.2

phase lag

difference between two *phases* (3.1) provided by periodic temperature changes measured at two different points on the surface and inside a test specimen

EXAMPLE When the periodic temperature changes 1 and 2 are given by $y_1 = A_1 \sin(\omega t + \varphi_1)$ and $y_2 = A_2 \sin(\omega t + \varphi_2)$, respectively, the phase lag between them is $\varphi_2 - \varphi_1$.

3.3

amplitude

half of the difference between the maximum and minimum values of the amount of displacement in a periodic temperature change

EXAMPLE A in a sine wave given by $A \sin(\omega t + \varphi)$ or $A \exp[i(\omega t + \varphi)]$ refers to the amplitude.

3.4 amplitude ratio

ratio of two *amplitudes* (3.3) provided by periodic temperature changes measured at any point on the surface and inside a test specimen.

EXAMPLE When the periodic temperature changes y_1 on the surface and y_2 inside the test specimen are given by $y_1 = A_1 \sin(\omega t + \phi_1)$ and $y_2 = A_2 \sin(\omega t + \phi_2)$, respectively, the amplitude ratio between the two amplitudes is A_2/A_1 .

3.5 period

reproduction interval of a periodic phenomenon (or a periodic function)

Note 1 to entry: When the time interval is constant, the period f is given by $f = 1/\nu = 2\pi/\omega$, where ν is the frequency (3.6) and ω is the angular frequency (3.7).

3.6 frequency

number of repetitions of the same state within a certain time interval of any temporal periodic phenomena

Note 1 to entry: It is expressed as $\nu = 1/f$, where f is the period (3.5).

3.7 angular frequency

rotation angle per second

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Note 1 to entry: Angular frequency is obtained by multiplying the frequency (3.6) ν by 2π ($2\pi\nu$) or by multiplying the reciprocal of the period (3.5) f by 2π ($2\pi/f$).

4 Symbols

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The symbols used in this document are given in Table 1.

Table 1 — Symbols

Symbol	Quantity	Unit
a	Thermal diffusivity	m^2/s
c	Specific heat capacity	$J/(kg \cdot K)$
D	Difference	%
d	Thickness of test specimen (total thickness of the two pieces when using two stacked test pieces in a measurement)	m
f	Period	s
i	Imaginary unit	-
k	Damping coefficient	1/m
L	Length of one side of test specimen	m
l	Distance from periodic heating surface ($d - x_m$)	m
m	Mass prior to measuring thermal diffusivity (prior to grooving)	kg
T	Absolute temperature	K
V	Volume prior to measuring thermal diffusivity (prior to grooving)	m^3
x	x coordinate	m
x_m	Location of temperature measurement point inside a test specimen	m
ϵ	Phase lag on $x = 0$ surface	rad
η	Arbitrary phase	rad

Table 1 (continued)

Symbol	Quantity	Unit
θ	Temperature	°C
λ	Thermal conductivity	W/(m·K)
ν	Frequency	1/s
π	Circular constant	-
ρ	Density, bulk density	kg/m ³
φ	Phase lag at $x = x_m$ cross section	rad
ω	Angular frequency	1/s

5 Principle

5.1 General

The periodic heat method is a method for obtaining thermal diffusivity by measuring the temperature at two different points in a test specimen. Thermal diffusivity is evaluated by the phase lag between two phases provided by periodically changing the temperature of one side surface of the test specimen. Here, those temperatures are measured at any point on the heating surface and inside (the internal plane perpendicular to the direction of thermal diffusion) the test specimen.

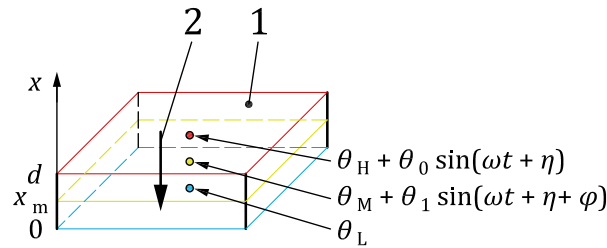
This measurement method uses a solution of the heat conduction equation that is obtained under the condition that the temperature on one side of a test specimen changes as a trigonometric function of time and the change propagates in a one-dimensional direction, and further, the temperature on the opposite side is kept constant.

The periodical temperature change on the heated surface shall be expressed by a trigonometric function of time. <https://standards.iteh.ai/catalog/standards/sist/fa505272-5f19-4c64-954e-f4db22087cfe/iso-21901-2021>

It is contrary to the measurement principle to generate a distorted temperature change on the heated surface. In addition, in reality, the waveform easily changes in a distorted temperature change during propagation in a test specimen, and this becomes a cause of measurement errors.

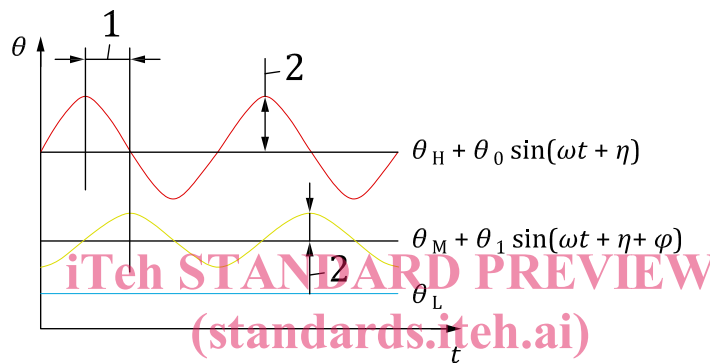
5.2 Calculation of thermal diffusivity

As shown in [Figure 1](#), the x-axis is taken upward along the thickness direction of a test specimen, and the heat dissipation surface (the surface in contact with the low-temperature side heater) of the test specimen with thickness d is set as the origin, while the heating surface is set at $x = d$. Accordingly, as shown by the thick arrow, heat flows downward from the heating surface to the heat dissipation surface. At the heat dissipation surface, the temperature is kept constant, and the temperature of the heating surface is changed periodically based on $\theta_H + \theta_0 \sin(\omega t + \eta)$. Under these conditions, the phase lag (rad) between the point at $x = d$ and an arbitrary point at $x = x_m$ is obtained by solving the one-dimensional heat conduction equation. As a result, [Formula \(1\)](#) is given (see [Figure 2](#)).



- Key**
- 1 test specimen
 - 2 heat flow

Figure 1 — Relation between test specimen and coordinate (one-dimensional heat flow, in the case θ_L is kept constant)



- Key**
- 1 phase lag
 - 2 amplitude

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Figure 2 — Periodic temperature change, in the case θ_L is kept constant

$$\varphi = \arg \left\{ \frac{\sinh kx_m(1+i)}{\sinh kd(1+i)} \right\} \tag{1}$$

The damping coefficient k in [Formula \(1\)](#) is defined by [Formula \(2\)](#).

$$k = \sqrt{\frac{\omega}{2a}} \tag{2}$$

Also, the angular frequency ω is defined by [Formula \(3\)](#).

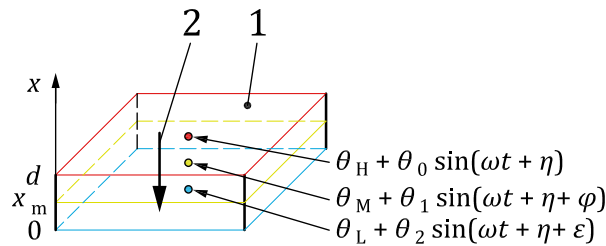
$$\omega = \frac{2\pi}{f} \tag{3}$$

At this time, mean temperature of a test specimen θ_S is calculated by [Formula \(4\)](#).

$$\theta_S = (\theta_H + \theta_L) / 2 \tag{4}$$

When using [Formula \(1\)](#), the surface temperature on the low-temperature side of a test specimen shall always be controlled so as to be constant.

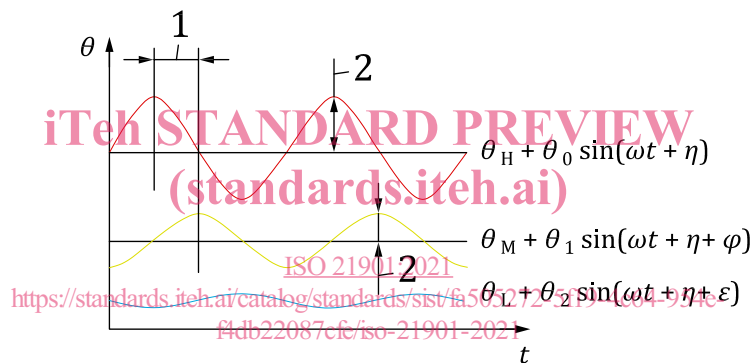
If the periodical temperature changes on the low-temperature side, as described in [Figure 3](#), it is also possible to solve the phase lag between $x = d$ and $x = x_m$ by solving the one-dimensional heat conduction equation in the same manner as shown above. However, in this case, thermal diffusivity is calculated using the phase lag and the amplitude ratio.



Key

- 1 test specimen
- 2 heat flow

Figure 3 — Relation between test specimen and coordinates (one-dimensional heat flow, in the case θ_L changes periodically)



Key

- 1 phase lag
- 2 amplitude

Figure 4 — Periodic temperature change, in the case θ_L changes periodically

As a result, [Formula \(5\)](#) is given (see [Figure 4](#)). The coefficients used in [Formula \(5\)](#) are shown in [Formulae \(6\), \(7\), \(8\)](#) and [\(9\)](#). The damping coefficient k and the angular frequency ω are defined in [Formulae \(2\)](#) and [\(3\)](#).

If the temperature on the low-temperature side is constant, [Formula \(5\)](#) is equal to [Formula \(1\)](#).

$$\varphi = \arctan \left\{ \frac{\theta_{1H} \sin(\varphi_H) + \theta_{1L} \sin(\varphi_L + \varepsilon)}{\theta_{1H} \cos(\varphi_H) + \theta_{1L} \cos(\varphi_L + \varepsilon)} \right\} + \begin{cases} 0 & \text{if } \theta_{1H} \cos(\varphi_H) + \theta_{1L} \cos(\varphi_L + \varepsilon) \geq 0, \\ \pi & \text{if } \theta_{1H} \cos(\varphi_H) + \theta_{1L} \cos(\varphi_L + \varepsilon) < 0, \end{cases} \quad (5)$$

$$\theta_{1H} = \theta_0 \sqrt{\frac{\cosh(2kx_m) - \cos(2kx_m)}{\cosh(2kd) - \cos(2kd)}} \quad (6)$$

$$\theta_{1L} = \theta_2 \sqrt{\frac{\cosh(2kl) - \cos(2kl)}{\cosh(2kd) - \cos(2kd)}} \quad (7)$$

$$\varphi_H = \arg\left(\frac{\sinh\{kx_m(1+i)\}}{\sinh\{kd(1+i)\}}\right) \quad (8)$$

$$\varphi_L = \arg\left(\frac{\sinh\{kl(1+i)\}}{\sinh\{kd(1+i)\}}\right) \quad (9)$$

6 Test specimen

6.1 Sample

The test specimen taken from the sample shall satisfy the homogeneity prescribed in ISO 8302:1991, 1.8.2. Here, the term “homogeneous” means that raw materials such as fibres and particles constituting the specimen are distributed evenly along the direction of heat flow. Namely, the distribution of fibres and particles is independent of their location in the specimen, and there are no extreme voids inside the specimen. The thermal diffusivity of various kinds of materials like fibrous insulations such as ceramic fibre, rock wool, glass fibre and fibrous board, and furthermore, styrene foam, urethane foam, brick and concrete can be measured by applying the periodic heat method. However, the thermal diffusivity of materials which undergo phase change, release gases, expand or shrink excessively or deform as a result of phenomena such as cracks cannot be measured by this method.

6.2 Details of test specimen

The details of the test specimen are as follows.

- a) The dimensions of the test specimen shall be the same as those of the heater for periodic heating with the dimensional tolerance of ± 2 mm with respect to the heater dimensions.
- b) The relationship between the length L of one side and the thickness d of the test specimen should be restricted so as to reduce the error due to heat inflow (outflow) from the edges of the test specimen. In addition, the minimum thickness d of the test specimen should be restricted so as to reduce the error due to the diameter of the thermocouples on the upper/middle/lower surfaces of the test specimen. For example, when using a 3 mm diameter insulator tube, the minimum thickness d is 20 mm.
- c) The heating and low-temperature surfaces of the test specimen shall be smooth, and if necessary, test specimens made of deformable materials shall be held by a support frame or a spacer.
- d) The test specimen shall be dried in a drier at $105 \text{ }^\circ\text{C} \pm 2 \text{ }^\circ\text{C}$ until it reaches a constant mass. When there is a risk of alteration or deformation by heat, the test specimen shall be dried until it reaches a constant mass at a temperature that causes no alteration, deformation or other property changes.
- e) The bulk density of the test specimen can be calculated by using [Formula \(10\)](#) based on the volume at the time of measurement of thermal diffusivity and on the mass prior to measurement of thermal diffusivity.

$$\rho = \frac{m}{V} \quad (10)$$

It is recommended that the ratio of length to width of the specimen (L/d) be 6 or more, as L/d may affect the results of the measurement. If it is necessary to use a smaller value of L/d , the accuracy of the measurement shall be verified by the method described in [Annex A](#).

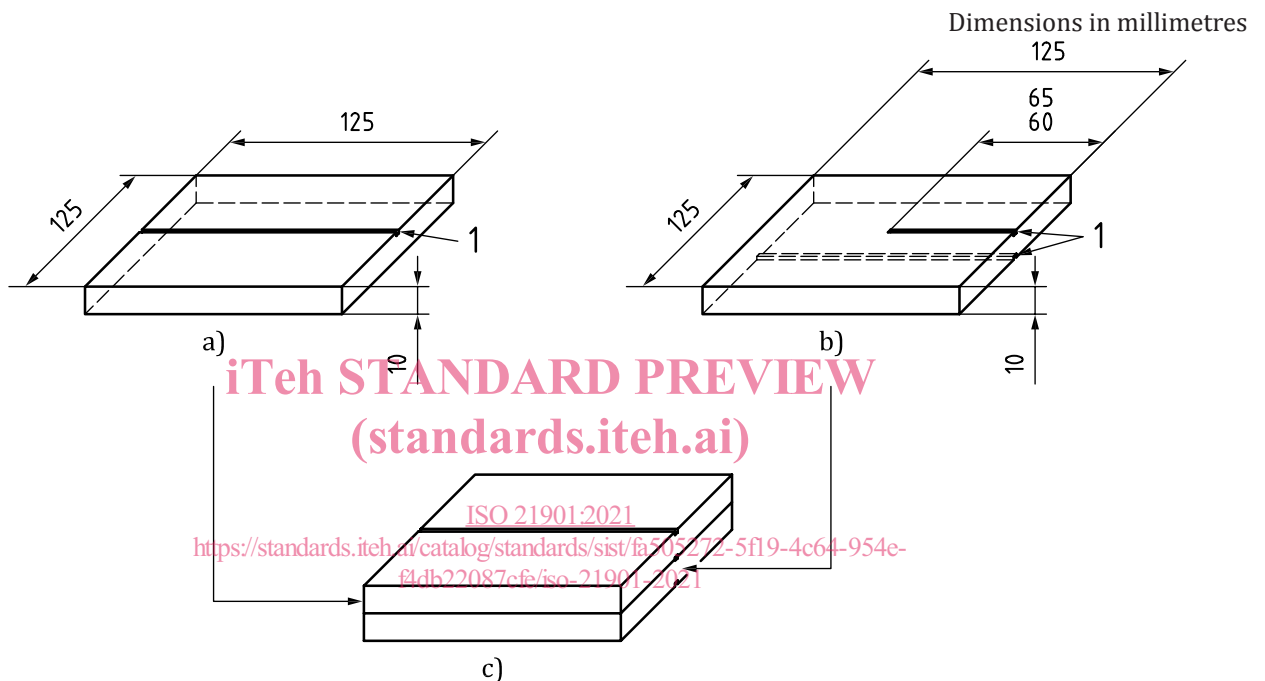
6.3 Machining of test specimen

6.3.1 When using two test specimens

Prepare two test specimens with approximately the same bulk density, and perform the machining work required to set the thermocouples for temperature measurement according to the procedure

shown below. In this case, the total thickness of the specimen composed of the two specimens shall be restricted as described in 6.2.

- On one specimen, cut a groove about 3 mm wide and 1,5 mm deep at the centre of one surface so that the groove runs across the specimen; see Figure 5 a).
- On the other specimen, cut a groove about 3 mm wide and 1,5 mm deep from the side to the centre of the specimen surface. In Figure 5 b), the groove length is 60 mm to 65 mm. Also cut a groove with the same dimensions on the other surface so that the groove runs across the specimen; see Figure 5 b).
- As shown in Figure 5 c), place the test specimen in Figure 5 a) over the test specimen in Figure 5 b), with no space between them.



Key

- 1 groove

Figure 5 — Test specimen (machining process required when using two test specimens) (example)

6.3.2 When using a single test specimen

When using a single test specimen, the thickness of the specimen shall be restricted as described in 6.2.

As shown in Figure 6, cut grooves about 3 mm wide and 1,5 mm deep at the centre of the top and bottom surfaces so that the grooves run across the specimen. In addition, drill a hole having a diameter of about 2,5 mm toward the centre perpendicular to the side surface from the centre of the thickness direction on the side surface. In Figure 6, the length of the hole is about 60 mm to 65 mm.