
Calculation of load capacity of spur and helical gears —

Part 20:

Calculation of scuffing load capacity (also applicable to bevel and hypoid gears) — Flash temperature method

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*Calcul de la capacité de charge des engrenages cylindriques à
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*Partie 20: Calcul de la capacité de charge au grippage (applicable
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ISO copyright office
Ch. de Blandonnet 8 • CP 401
CH-1214 Vernier, Geneva, Switzerland
Tel. +41 22 749 01 11
Fax +41 22 749 09 47
copyright@iso.org
www.iso.org

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Foreword

ISO (the International Organization for Standardization) is a worldwide federation of national standards bodies (ISO member bodies). The work of preparing International Standards is normally carried out through ISO technical committees. Each member body interested in a subject for which a technical committee has been established has the right to be represented on that committee. International organizations, governmental and non-governmental, in liaison with ISO, also take part in the work. ISO collaborates closely with the International Electrotechnical Commission (IEC) on all matters of electrotechnical standardization.

The procedures used to develop this document and those intended for its further maintenance are described in the ISO/IEC Directives, Part 1. In particular the different approval criteria needed for the different types of ISO documents should be noted. This document was drafted in accordance with the editorial rules of the ISO/IEC Directives, Part 2 (see www.iso.org/directives).

Attention is drawn to the possibility that some of the elements of this document may be the subject of patent rights. ISO shall not be held responsible for identifying any or all such patent rights. Details of any patent rights identified during the development of the document will be in the Introduction and/or on the ISO list of patent declarations received (see www.iso.org/patents).

Any trade name used in this document is information given for the convenience of users and does not constitute an endorsement.

For an explanation on the voluntary nature of standards, the meaning of ISO specific terms and expressions related to conformity assessment, as well as information about ISO's adherence to the World Trade Organization (WTO) principles in the Technical Barriers to Trade (TBT) see the following URL: www.iso.org/iso/foreword.html

This document was prepared by Technical Committee ISO/TC 60, *Gears*, Subcommittee SC 2, *Gear capacity calculation*.

This first edition of ISO/TS 6336-20 cancels and replaces ISO/TR 13989-1.

A list of all parts in the ISO 6336 series can be found on the ISO website. See also the Introduction for an overview.

Introduction

The ISO 6336 series consists of International Standards, Technical Specifications (TS) and Technical Reports (TR) under the general title *Calculation of load capacity of spur and helical gears* (see [Table 1](#)).

- International Standards contain calculation methods that are based on widely accepted practices and have been validated.
- TS contain calculation methods that are still subject to further development.
- TR contain data that is informative, such as example calculations.

The procedures specified in ISO 6336-1 to ISO 6336-19 cover fatigue analyses for gear rating. The procedures described in ISO 6336-20 to ISO 6336-29 are predominantly related to the tribological behaviour of the lubricated flank surface contact. ISO 6336-30 to ISO 6336-39 include example calculations. The ISO 6336 series allows the addition of new parts under appropriate numbers to reflect knowledge gained in the future.

Requesting standardized calculations according to ISO 6336 without referring to specific parts requires the use of only those parts that are currently designated as International Standards (see [Table 1](#) for listing). When requesting further calculations, the relevant part or parts of ISO 6336 need to be specified. Use of a Technical Specification as acceptance criteria for a specific design needs to be agreed in advance between manufacturer and purchaser.

Table 1 — Overview of ISO 6336

Calculation of load capacity of spur and helical gears	International Standard	Technical Specification	Technical Report
<i>Part 1: Basic principles, introduction and general influence factors</i>	X		
<i>Part 2: Calculation of surface durability (pitting)</i>	X		
<i>Part 3: Calculation of tooth bending strength</i>	X		
<i>Part 4: Calculation of tooth flank fracture load capacity</i> (Replaces ISO/TR 13989-1)	X	X	
<i>Part 5: Strength and quality of materials</i>	X		
<i>Part 6: Calculation of service life under variable load</i>	X		
<i>Part 20: Calculation of scuffing load capacity (also applicable to bevel and hypoid gears) — Flash temperature method</i> (Replaces ISO/TR 13989-1)		X	
<i>Part 21: Calculation of scuffing load capacity (also applicable to bevel and hypoid gears) — Integral temperature method</i> (Replaces ISO/TR 13989-2)		X	
<i>Part 22: Calculation of micropitting load capacity</i> (Replaces ISO/TR 15144-1)		X	
<i>Part 30: Calculation examples for the application of ISO 6336-1, ISO 6336-2, ISO 6336-3 and ISO 6336-5</i>			X
<i>Part 31: Calculation examples of micropitting load capacity</i> (Replaces ISO/TR 15144-2)			X

At the time of publication of this document, some of the parts listed here were under development. Consult the ISO website.

Since 1990, the flash temperature method has been enriched with research for short exposure times, consideration of transition diagrams, new approximations for the coefficient of friction, and completely renewed load sharing factors. In 1991, the extension of Blok's flash temperature formula made it directly applicable to hypoid gears.

The integral temperature, presented in ISO/TS 6336-21, averages the flash temperature and supplements empirical influence factors to the hidden load sharing factor. The resulting value approximates the maximum contact temperature, thus yielding about the same assessment of scuffing

risk as the flash temperature method of this document. The integral temperature method is less sensitive for those cases where there are local temperature peaks, usually in gearsets that have low contact ratio or contact near the base circle or other sensitive geometries.

The risk of scuffing damage varies with the properties of gear materials, the lubricant used, the surface roughness of tooth flanks, the sliding velocities and the load. In contrast to the relatively long time of development of fatigue damage, one single momentary overload can initiate scuffing damage of such severity that affected gears may no longer be used. According to Blok^{[12][13][14][15][16][17]}, high contact temperatures of lubricant and tooth surfaces at the instantaneous contact position may effect a breakdown of the lubricant film at the contact interface.

The interfacial contact temperature is conceived as the sum of two components.

- The interfacial bulk temperature of the moving interface, which, if varying, does so only comparatively slowly. The bulk temperature, θ^M , is the equilibrium temperature of the surface of the gear teeth before they enter the contact zone. For evaluating this component, it may be suitably averaged from the two overall bulk temperatures of the two rubbing teeth. The latter two bulk temperatures follow from the thermal network theory^[18].
- The rapidly fluctuating flash temperature of the moving faces in contact. The flash temperature is the calculated increase in gear tooth surface temperature at a given point along the path of contact resulting from the combined effects of gear tooth geometry, load, friction, velocity and material properties during operation. Special attention has to be paid to the coefficient of friction. A common practice is the use of a coefficient of friction valid for regular working conditions, although it may be stated that at incipient scuffing, the coefficient of friction has significantly higher values.

The complex relationship between mechanical, hydrodynamical, thermodynamical and chemical phenomena has been the object of extensive research and experiment. Experimental investigations may induce empirical influence factors. A direct substitution of empirical influence factors may enforce the related functional factors in the main formula to be fixated to average values. However, correct treatment of functional factors (e.g. coefficient of friction, load sharing factor, thermal contact coefficient) keeps the main formula intact, in confirmation with the experiments and practice.

Next to the maximum contact temperature, the progress of the contact temperature along the path of contact provides necessary information to the gear design.

Calculation of load capacity of spur and helical gears —

Part 20:

Calculation of scuffing load capacity (also applicable to bevel and hypoid gears) — Flash temperature method

1 Scope

This document specifies methods and formulae for evaluating the risk of scuffing, based on Blok's contact temperature concept.

The fundamental concept is applicable to all machine elements with moving contact zones. The flash temperature formulae are valid for a band-shaped or approximately band-shaped Hertzian contact zone and working conditions characterized by sufficiently high Péclet numbers.

2 Normative references

The following documents are referred to in the text in such a way that some or all of their content constitutes requirements of this document. For dated references, only the edition cited applies. For undated references, the latest edition of the referenced document (including any amendments) applies.

ISO 1122-1, *Vocabulary of gear terms — Part 1: Definitions related to geometry*

ISO 6336-1, *Calculation of load capacity of spur and helical gears — Part 1: Basic principles, introduction and general influence factors*

ISO 10300-1:2014, *Calculation of load capacity of bevel gears — Part 1: Introduction and general influence factors*

ISO 10825, *Gears — Wear and damage to gear teeth — Terminology*

3 Terms and definitions, symbols and units

3.1 Terms and definitions

For the purposes of this document, the terms and definitions given in ISO 1122-1 and ISO 10825 apply.

ISO and IEC maintain terminological databases for use in standardization at the following addresses:

- IEC Electropedia: available at <http://www.electropedia.org/>
- ISO Online browsing platform: available at <http://www.iso.org/obp>

3.2 Symbols and units

The symbols used in the formulae are shown in [Table 2](#). The units of length, metre, millimetre and micrometre, have been chosen in accordance with common practice. To achieve a "coherent" system, the units for B_M , c_Y and X_M have been adapted to the mixed application of metre and millimetre or millimetre and micrometre.

Table 2 — Symbols and units

Symbol	Description	Unit
a	Centre distance	mm
b	Facewidth, smaller value for pinion or wheel ^a	mm
b_{eff}	Effective facewidth	mm
b_H	Semi-width of Hertzian contact band	mm
B_M	Thermal contact coefficient	N/(mm ^{1/2} ·m ^{1/2} ·s ^{1/2} ·K)
B_{M1}	Thermal contact coefficient of pinion	N/(mm ^{1/2} ·m ^{1/2} ·s ^{1/2} ·K)
B_{M2}	Thermal contact coefficient of wheel	N/(mm ^{1/2} ·m ^{1/2} ·s ^{1/2} ·K)
C_{a1}	Tip relief of pinion	µm
C_{a2}	Tip relief of wheel	µm
C_{eff}	Optimal tip relief	µm
$C_{\text{eq}1}$	Equivalent tip relief of pinion	µm
$C_{\text{eq}2}$	Equivalent tip relief of wheel	µm
C_{f1}	Root relief of pinion	µm
C_{f2}	Root relief of wheel	µm
c_{M1}	Specific heat per unit mass of pinion	J/(kg·K)
c_{M2}	Specific heat per unit mass of wheel	J/(kg·K)
c_γ	Mesh stiffness	N/(mm·µm)
d_1	Reference diameter of pinion	mm
d_2	Reference diameter of wheel	mm
d_{a1}	Tip diameter of pinion	mm
d_{a2}	Tip diameter of wheel	mm
E_1	Modulus of elasticity of pinion	N/mm ²
E_2	Modulus of elasticity of wheel	N/mm ²
E_r	Reduced modulus of elasticity	N/mm ²
F_{ex}	External axial force	N
F_n	Normal load in wear test	N
F_t	Nominal tangential force	N
H_1	Auxiliary dimension	mm
H_2	Auxiliary dimension	mm
$h_{\text{am}1}$	Tip height in mean cone of pinion	mm
$h_{\text{am}2}$	Tip height in mean cone of wheel	mm
K_A	Application factor	—
$K_{B\alpha}$	Transverse load factor (scuffing)	—
$K_{B\beta}$	Face load factor (scuffing)	—
$K_{H\alpha}$	Transverse load factor (contact stress)	—
$K_{H\beta}$	Face load factor (contact stress)	—
K_{mp}	Multiple path factor	—
K_v	Dynamic factor	—
m_n	Normal module	mm
n_1	Revolutions per minute of pinion	r/min
n_p	Number of mesh contacts	—
$P_{\text{e}1}$	Péclet number of pinion material	—
$P_{\text{e}2}$	Péclet number of wheel material	—

The term *wheel* is used for the mating gear of a pinion.

Table 2 (continued)

Symbol	Description	Unit
Q	Quality grade	—
R_{a1}	Tooth flank surface roughness of pinion	µm
R_{a2}	Tooth flank surface roughness of wheel	µm
R_m	Cone distance of mean cone	mm
r_{m1}	Reference radius in mean cone of pinion	mm
r_{m2}	Reference radius in mean cone of wheel	mm
S_B	Safety factor for scuffing	—
S_{FZG}	Load stage (in FZG test)	—
t_1	Contact exposure time of pinion	µs
t_2	Contact exposure time of wheel	µs
t_c	Contact exposure time at bend of curve	µs
t_{\max}	Longest contact exposure time	µs
u	Gear ratio	—
u_v	Virtual ratio	—
v_g	Sliding velocity	m/s
v_{g1}	Tangential velocity of pinion	m/s
v_{g2}	Tangential velocity of wheel	m/s
$v_{g\Sigma C}$	Sum of tangential velocities in pitch point	m/s
v_t	Pitch line velocity	m/s
w_{Bn}	Normal unit load	N/mm
w_{Bt}	Transverse unit load	N/mm
$X_{\text{but},\Gamma}$	Buttressing factor	—
$X_{\text{but},A}$	Buttressing value	—
$X_{\text{but},E}$	Buttressing value	—
X_G	Geometry factor	—
X_J	Approach factor	—
X_L	Lubricant factor	—
X_M	Thermo-elastic factor	K·N ^{-3/4} ·s ^{-1/2} ·m ^{-1/2} ·mm
X_{mp}	Multiple mating pinion factor	—
X_R	Roughness factor	—
X_S	Lubrication system factor	—
X_W	Structural factor	—
$X_{\alpha\beta}$	Angle factor	—
X_Γ	Load sharing factor	—
X_Θ	Gradient of the scuffing temperature	—
z_1	Number of teeth of pinion	—
z_2	Number of teeth of wheel	—
α_{a1}	Transverse tip pressure angle of pinion	°
α_{a2}	Transverse tip pressure angle of wheel	°
α_t	Transverse pressure angle	°
α_{wn}	Normal working pressure angle	°
α_{wt}	Transverse working pressure angle	°
α_{y1}	Pinion pressure angle at arbitrary point	°

The term *wheel* is used for the mating gear of a pinion.

Table 2 (continued)

Symbol	Description	Unit
β	Helix angle	°
β_b	Base helix angle	°
β_{bm}	Base helix angle in midcone	°
β_w	Working helix angle	°
Γ_A	Parameter on the line of action at point A	—
Γ_{AA}	Parameter on the line of action at point AA	—
Γ_{AB}	Parameter on the line of action at point AB	—
Γ_{AU}	Parameter on the line of action at point AU	—
Γ_B	Parameter on the line of action at point B	—
Γ_{BB}	Parameter on the line of action at point BB	—
Γ_D	Parameter on the line of action at point D	—
Γ_{DD}	Parameter on the line of action at point DD	—
Γ_{DE}	Parameter on the line of action at point DE	—
Γ_E	Parameter on the line of action at point E	—
Γ_{EE}	Parameter on the line of action at point EE	—
Γ_{EU}	Parameter on the line of action at point EU	—
Γ_M	Parameter on the line of action at point M	—
Γ_y	Parameter on the line of action at arbitrary point	—
γ_1	Angle of direction of tangential velocity of pinion	—
γ_2	Angle of direction of tangential velocity of wheel	—
δ_1	Pitch cone angle of pinion	°
δ_2	Pitch cone angle of wheel	°
ε_α	Transverse contact ratio	—
ε_β	Overlap ratio	—
ε_γ	Total contact ratio	—
η_{oil}	Absolute (dynamic) viscosity at oil temperature	$\text{mPa}\cdot\text{s}$
θ_B	Contact temperature	°C
θ_{Bmax}	Maximum contact temperature	°C
θ_{fl}	Flash temperature	K
θ_{flm}	Average flash temperature	K
θ_{flmax}	Maximum flash temperature	K
θ_{flmaxT}	Maximum flash temperature at test	K
θ_M	Bulk temperature	°C
θ_{Mi}	Interfacial bulk temperature	°C
θ_{M1}	Bulk temperature of pinion teeth	°C
θ_{M2}	Bulk temperature of wheel teeth	°C
θ_{MT}	Bulk temperature at test	°C
θ_{oil}	Oil temperature before reaching the mesh	°C
θ_S	Scuffing temperature	°C
θ_{Sc}	Scuffing temperature at long contact time	°C
λ_{M1}	Heat conductivity of pinion	$\text{N}/(\text{s}\cdot\text{K})$
λ_{M2}	Heat conductivity of wheel	$\text{N}/(\text{s}\cdot\text{K})$
μ	Coefficient of friction in pin-and-ring test	—

The term *wheel* is used for the mating gear of a pinion.

Table 2 (continued)

Symbol	Description	Unit
μ_m	Mean coefficient of friction	—
v_1	Poisson's ratio of pinion material	—
v_2	Poisson's ratio of wheel material	—
ρ_{M1}	Density of pinion material	kg/m ³
ρ_{M2}	Density of wheel material	kg/m ³
ρ_{relC}	Transverse relative radius of curvature at pitch point	mm
ρ_{y1}	Radius of curvature at arbitrary point of pinion	mm
ρ_{y2}	Radius of curvature at arbitrary point of wheel	mm
ρ_{relY}	Relative radius of curvature at arbitrary point y	mm
Σ	Shaft angle	°
Φ	Quill shaft twist	°

The term *wheel* is used for the mating gear of a pinion.

4 Scuffing and wear

4.1 Occurrence of scuffing and wear

When gear teeth are completely separated by a full fluid film of lubricant, there is no contact between the asperities of the tooth surfaces, and usually, there is no scuffing or wear. Here, the coefficient of friction is rather low. In exceptional cases, a damage similar to scuffing may be caused by a sudden thermal instability[19] in a thick oil film, which phenomenon is not treated here.

For thinner elastohydrodynamic films, incidental asperity contact takes place. Accordingly, as the mean film thickness decreases, the number of contacts increases. Abrasive wear, adhesive wear or scuffing becomes possible. Abrasive wear may occur due to the rolling action of the gear teeth or the presence of abrasive particles in the lubricant. Adhesive wear occurs by localized welding and subsequent detachment and transfer of particles from one or both of the meshing teeth. Abrasive or adhesive wear may not be harmful if it is mild and if it subsides with time, as in a normal run-in process.

In contrast to mild wear, scuffing is a severe form of adhesive wear that can result in progressive damage to the gear teeth. In contrast to pitting and fatigue breakage which show a distinct incubation period, a short transient overloading can result in scuffing failure.

Excessive aeration or the presence in the lubricant of contaminants such as metal particles in suspension, or water, also increases the risk of scuffing damage. After scuffing, high-speed gears tend to suffer high levels of dynamic loading due to vibration which usually cause further damage by scuffing, pitting or tooth breakage.

In most cases, the resistance of gears to scuffing can be improved by using a lubricant with enhanced anti-scuff additives.

NOTE The less correct designation Extreme Pressure (EP) is replaced by anti-scuff.

It is important however, to be aware that some disadvantages attend the use of anti-scuff additives: corrosion of copper, embrittlement of elastomers, lack of world-wide availability, etc.

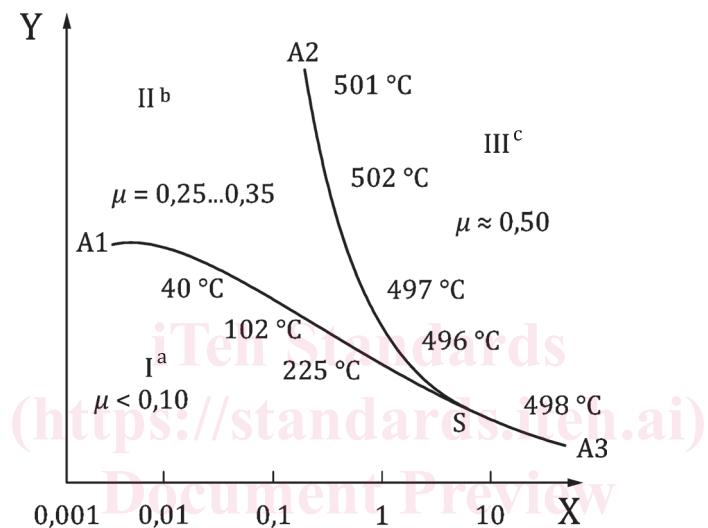
The methods described are not suitable for "cold scuffing" which is in general associated with low speed, under approximately 4 m/s, through hardened heavily loaded gears of rather poor quality.

4.2 Transition diagram

The lubrication condition of sliding concentrated steel contacts, which operate in a liquid lubricant, can be described^{[20][21][22][23]} in terms of transition diagrams. A transition diagram, according to [Figure 1](#), is considered to be applicable to contacts functioning at constant oil bath temperature.

At combinations of normal force, F_n , and relative sliding velocity, v_g , which fall below the line A1-S, in region I (see [Figure 1](#)), the lubrication condition is characterized by a coefficient of friction of about 0,1 and a specific wear rate of $10^{-2} \text{ mm}^3/(\text{N}\cdot\text{m})$ to $10^{-6} \text{ mm}^3/(\text{N}\cdot\text{m})$ (i.e. volume wear per unit of normal force, per unit of sliding distance).

If, with v_g not above a value according to point S, the load is increased into region II, a transition into a second condition of lubrication occurs. This mild wear lubrication condition is characterized by a coefficient of friction of about 0,3 to 0,4 and a specific wear rate of $1 \text{ mm}^3/(\text{N}\cdot\text{m})$ to $5 \text{ mm}^3/(\text{N}\cdot\text{m})$.



Key

X relative sliding velocity, v_g , in m/s

[ISO/TS 6336-20:2017](#)

Y normal force, F_n <http://standards.iTech.ai/catalog/standards/iso/419553c4-2385-42be-bdc4-95b283cdb85e/iso-ts-6336-20-2017>

a "No wear" or extremely mild wear.

b Mild wear.

c Scuffing — severe wear.

Figure 1 — Transition diagram for contraform contacts with example of calculated contact temperatures

If load is increased still further, a transition into a third condition of lubrication, region III, occurs at intersection of the line A2-S. This region is characterized by a coefficient of friction equal to 0,4 to 0,5. The wear rate, however, is considerably higher, i.e. $100 \text{ mm}^3/(\text{N}\cdot\text{m})$ to $1000 \text{ mm}^3/(\text{N}\cdot\text{m})$, than in regions I and II, and the worn surfaces show evidence of severe wear in the form of scuffing. If load increases at relative sliding velocities beyond point S, a direct transition from region I to region III takes place.

There is strong evidence that the position of the line A1-S-A3 depends upon lubricant viscosity^[24] as well as upon Hertzian contact pressure^{[20][21]}. At combinations of F_n and v_g that fall below this line, it is believed that the surfaces are kept apart by a thin lubricant film which is, however, penetrated by roughness asperities. In this context, the term "partial elastohydrodynamic lubrication" has been used^[21].

In region II, liquid film effects are completely absent. This region is identical to the region of "incipient scuffing"^[25]. There is evidence that the transition which occurs at intersecting the line A2-S is associated with reaching a critical value of the contact temperature. This is the fundamental concept according to References [\[12\]](#), [\[13\]](#), [\[14\]](#), [\[15\]](#), [\[16\]](#), [\[17\]](#), [\[18\]](#) and [\[19\]](#).