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Raumfahrttechnik - Handbuch Knicken und Beulen von Strukturen

Ingénierie spatiale - Flambement des structures

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