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StandardPractice for Size Scaling of Tensile Strengths Using Weibull Statistics for Advanced Ceramics¹

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1. Scope

1.1 This standard practice provides methodology to convert fracture strength parameters (primarily the mean strength and the Weibull characteristic strength) estimated from data obtained with one test geometry to strength parameters representing other test geometries. This practice addresses uniaxial strength data as well as some biaxial strength data. It may also be used for more complex geometries proved that the effective areas and effective volumes can be estimated. It is for the evaluation of Weibull probability distribution parameters for advanced ceramics that fail in a brittle fashion. Fig. 1 shows the typical variation of strength with size. The larger the specimen or component, the weaker it is likely to be.

1.2 As noted in Practice C1239, the failure strength of advanced ceramics is treated as a continuous random variable. A number of functions may be used to characterize the strength distribution of brittle ceramics, but the Weibull distribution is the most appropriate especially since it permits strength scaling for the size of specimens or component. Typically, a number of test specimens with well-defined geometry are broken under well-defined loading conditions. The force at which each test specimen fails is recorded and fracture strength calculated. The strength values are used to obtain Weibull parameter estimates associated with the underlying population distribution.

1.3 This standard is restricted to the assumption that the distribution underlying the failure strengths is the twoparameter Weibull distribution with size scaling. The practice also assumes that the flaw population is stable with time and that no slow crack growth occurs.

1.4 This practice includes the following topics:

	Section
Scope	1
Referenced Documents	2
Terminology	3
Summary of Practice	4
Significance and Use	5
Probability of Failure Relationships	6
Test Specimens with Uniaxial Stress States—Effective	7
Volume and Area Relationships	
Uniaxial Tensile Test Specimens	7.1
Rectangular Flexure Test Specimens	7.2
Round Flexure Test Specimens	7.3
C-Ring Test Specimens	7.4
Test Specimens with Multiaxial Stress States—Effective	8
Volume and Area Relationships	
Pressure-on-Ring Test Specimens	8.1
Ring-on-Ring Test Specimens	8.2
Examples of Converting Characteristic Strengths	9
Report CV	10
Precision and Bias	11
Keywords	12
Combined Gamma Function for Round Rods Tested	Annex A1
in Flexure	
Components or Test Specimens with Multiaxial Stress Distributions	Annex A2
Components or Test Specimens with Complex Geometries and Stress Distributions	Annex A3

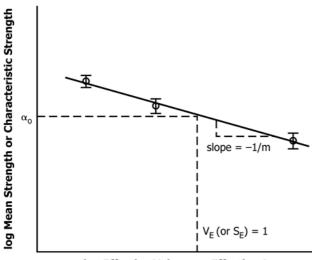
1.5 The values stated in SI units are to be regarded as standard. No other units of measurement are included in this standard.

1.5.1 The values stated in SI units are in accordance with IEEE/ASTM SI 10.

1.6 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

¹ This practice is under the jurisdiction of ASTM Committee C28 on Advanced Ceramics and is the direct responsibility of Subcommittee C28.01 on Mechanical Properties and Performance.

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log Effective Volume or Effective Area FIG. 1 Strength Scales with Size

2. Referenced Documents

- 2.1 ASTM Standards:²
- C1145 Terminology of Advanced Ceramics
- C1161 Test Method for Flexural Strength of Advanced Ceramics at Ambient Temperature
- C1211 Test Method for Flexural Strength of Advanced Ceramics at Elevated Temperatures
- C1239 Practice for Reporting Uniaxial Strength Data and Estimating Weibull Distribution Parameters for Advanced Ceramics
- C1273 Test Method for Tensile Strength of Monolithic Advanced Ceramics at Ambient Temperatures
- C1322 Practice for Fractography and Characterization of Fracture Origins in Advanced Ceramics
- C1323 Test Method for Ultimate Strength of Advanced Ceramics with Diametrally Compressed C-Ring Specimens at Ambient Temperature
- C1366 Test Method for Tensile Strength of Monolithic Advanced Ceramics at Elevated Temperatures
- C1499 Test Method for Monotonic Equibiaxial Flexural Strength of Advanced Ceramics at Ambient Temperature
 E6 Terminology Relating to Methods of Mechanical Testing
 E456 Terminology Relating to Quality and Statistics

3. Terminology

3.1 Unless otherwise noted, the Weibull parameter estimation terms and equations found in Practice C1239 shall be used.

3.2 For definitions of other statistical terms, terms related to mechanical testing, and terms related to advanced ceramics used in this guide, refer to Terminologies E6, E456, and C1145, or to appropriate textbooks on statistics (1-4).³

3.3 Nomenclature:

 A_T = gage area of a uniaxial tensile test specimen

 A_{B4} = gage area of a four-point flexure test specimen

 A_{B3} = gage area of a three-point flexure test specimen

 A_{POR} = gage area of a pressure-on-ring test specimen

 A_{ROR} = gage area of a ring-on-ring test specimen

 A_{CR} = gage area of a C-ring test specimen

b = thickness of a C-ring

b = width of a flexure test specimen

d = thickness of a flexure test specimen

D = diameter of a round flexure test specimen

D = overall diameter of a ring-on-ring disk test specimen

 D_L = loading (inner) ring diameter, ring-on-ring disk specimen

 D_s = support ring diameter, ring-on-ring or pressure-on-ring disk specimen

h = thickness of pressure-on-ring or ring-on-ring disk test specimen

k = load factor

 L_{gs} = length of the gage section in a uniaxial tensile test specimen

 L_{i4} = length of the inner span for a four-point flexure test specimen

 L_{o4} = length of the outer span for a four-point flexure test specimen

 L_{o3} = length of the outer span for a three-point flexure test specimen

m = Weibull modulus

 $P_f =$ probability of failure

 r_i = inner radius of a C-ring

 r_o = outer radius of a C-ring

t = thickness of a C-ring

 R_s = radius of the support ring for pressure-on-ring

 R_d = radius of the pressure-on-ring disk specimen

 S_E = effective surface area of a test specimen

 V_E = effective volume of a test specimen

 V_{POR} = gage volume of a pressure-on-ring test specimen V_{ROR} = gage volume of a ring-on-ring disk test specimen

 V_T = gage volume of tensile test specimen

 V_{B4} = gage volume of a four-point flexure test specimen

 V_{B3} = gage volume of a three-point flexure test specimen

 V_{CR} = gage volume of a C-ring test specimen

 σ = uniaxial tensile stress

 σ_{max} = maximum tensile stress in a test specimen at fracture σ_1 , σ_2 , σ_3 = principal stresses (tensile) at the integration points in any finite element

 σ_0 = Weibull material scale parameter (strength relative to unit size)

 σ_{θ} = Weibull characteristic strength

 $\sigma_{\theta T}$ = Weibull characteristic strength of a uniaxial tensile test specimen

 $\sigma_{\theta B4}$ = Weibull characteristic strength for a four-point flexure test specimen

 $\sigma_{\theta B3}$ = Weibull characteristic strength for a three-point flexure test specimen

 $\sigma_{\theta CR}$ = Weibull characteristic strength for a C-ring test specimen

² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

³ The boldface numbers in parentheses refer to the list of references at the end of this standard.

 $\sigma_{\theta POR}$ = Weibull characteristic strength for a pressure-onring test specimen

 $\sigma_{\theta \textit{ROR}}$ = Weibull characteristic strength for a ring-on-ring test specimen

 σ^* = an arbitrary, assumed estimate of the Weibull material scale factor

 $\bar{\sigma}$ = mean strength

 $\bar{\sigma}_T$ = mean strength for a uniaxial tensile test specimen $\bar{\sigma}_{B4}$ = mean strength for a four-point flexure test specimen $\bar{\sigma}_{B3}$ = mean strength for a three-point flexure test specimen $\bar{\sigma}_{CR}$ = mean strength for a C-ring test specimen $\bar{\sigma}_{POR}$ = mean strength for a pressure-on-ring test specimen $\bar{\sigma}_{ROR}$ = mean strength for a ring-on-ring test specimen θ = angle in a C-ring test specimen v = Poisson's ratio

4. Summary of Practice

4.1 The observed strength values of advanced ceramics are dependent on test specimen size, geometry and stress state. This standard practice enables the user to convert tensile strength parameters obtained from one test geometry to that of another, on the basis of assumptions listed in 5.5. Using the existing fracture strength data, estimates of the Weibull characteristic strength σ_{θ} , and the Weibull modulus *m*, are calculated in accordance with related Practice C1239 for the original test geometry. This practice uses the test specimen and loading sizes and geometries, and σ_{θ} and *m* to calculate the Weibull material scale parameter σ_0 . The Weibull characteristic strength σ_{θ} , the mean strength $\bar{\sigma}$, or the Weibull material scale factor σ_{0} , may be scaled to alternative test specimen geometries. Finally, a report citing the original test specimen geometry and strength parameters, as well as the size scaled Weibull strength parameters is prepared.

https://standards.iteh.a/catalog/standards/sist/8e152612 5. Significance and Use

5.1 Advanced ceramics usually display a linear stress-strain behavior to failure. Lack of ductility combined with flaws that have various sizes and orientations typically leads to large scatter in failure strength. Strength is not a deterministic property but instead reflects the intrinsic fracture toughness and a distribution (size and orientation) of flaws present in the material. This standard is applicable to brittle monolithic ceramics which fail as a result of catastrophic propagation of flaws. Possible rising R-curve effects are also not considered, but are inherently incorporated into the strength measurements.

5.2 Two- and three-parameter formulations exist for the Weibull distribution. This standard is restricted to the two-parameter formulation.

5.3 Tensile and flexural test specimens are the most commonly used test configurations for advanced ceramics. Ringon-ring and pressure-on-ring test specimens which have multiaxial states of stress are also included. Closed-form solutions for the effective volume and effective surfaces and the Weibull material scale factor are included for these configurations. This practice also incorporates size scaling methods for C-ring test specimens for which numerical approaches are necessary. A generic approach for arbitrary shaped test specimens or components that utilizes finite element analyses is presented in Annex A3.

5.4 The fracture origins of failed test specimens can be determined using fractographic analysis. The spatial distribution of these strength controlling flaws can be over a volume or an area (as in the case of surface flaws). This standard allows for the conversion of strength parameters associated with either type of spatial distribution. Length scaling for strength controlling flaws located along edges of a test specimen is not covered in this practice.

5.5 The scaling of strength with size in accordance with the Weibull model is based on several key assumptions (5). It is assumed that the same specific flaw type controls strength in the various specimen configurations. It is assumed that the material is uniform, homogeneous, and isotropic. If the material is a composite, it is assumed that the composite phases are sufficiently small that the structure behaves on an engineering scale as a homogeneous and isotropic body. The composite must contain a sufficient quantity of uniformly-distributed, randomly-oriented, reinforcing elements such that the material is effectively homogeneous. Whisker-toughened ceramic composites may be representative of this type of material. This practice is also applicable to composite ceramics that do not exhibit any appreciable bilinear or nonlinear deformation behavior. This standard and the conventional Weibull strength scaling with size may not be suitable for continuous fiberreinforced composite ceramics. The material is assumed to fracture in a brittle fashion, a consequence of stress causing catastrophic propagation of flaws. The material is assumed to be consistent (batch to batch, day to day, etc.). It is assumed that the strength distribution follows a Weibull two parameter distribution. It is assumed that each test piece has a statistically significant number of flaws and that they are randomly distributed. It is assumed that the flaws are small relative to the specimen cross section size. If multiple flaw types are present and control strength, then strengths may scale differently for each flaw type. Consult Practice C1239 and the example in 9.1 for further guidance on how to apply censored statistics in such cases. It is also assumed that the specimen stress state and the maximum stress are accurately determined. It is assumed that the actual data from a set of fractured specimens are accurate and precise. (See Terminology E456 for definitions of the latter two terms.) For this reason, this standard frequently references other ASTM standard test methods and practices which are known to be reliable in this respect.

5.6 Even if test data has been accurately and precisely measured, it should be recognized that the Weibull parameters determined from test data are in fact estimates. The estimates can vary from the actual (population) material strength parameters. Consult Practice C1239 for further guidance on the confidence bounds of Weibull parameter estimates based on test data for a finite sample size of test fractures.

5.7 When correlating strength parameters from test data from one specimen geometry to a second, the accuracy of the correlation depends upon whether the assumptions listed in 5.5 are met. In addition, statistical sampling effects as discussed in

5.6 may also contribute to variations between computed and observed strength-size scaling trends.

5.8 There are practical limits to Weibull strength scaling that should be considered. For example, it is implicitly assumed in the Weibull model that flaws are small relative to the specimen size. Pores that are 50 μ m (0.050 mm) in diameter are volume-distributed flaws in tension or flexural strength specimens with 5 mm or greater cross section sizes. The same may not be true if the cross section size is only 100 μ m.

6. Probability of Failure Relationships

6.1 General:

6.1.1 The random variable representing uniaxial tensile strength of an advanced ceramic will assume only positive values, and the distribution is usually asymmetric about the mean. These characteristics limit the use of the normal distribution (as well as others) and point to the use of the Weibull and similar skewed distributions. Fig. 2 shows the shape of the Weibull distribution as compared to a normal distribution. If the random variable representing uniaxial tensile strength of an advanced ceramic is characterized by a two-parameter Weibull distribution (see Practice C1239 for a detailed discussion regarding the mathematical description of the Weibull distribution), then the failure probability for a test specimen fabricated from such an advanced ceramic is given by the cumulative distribution function:

 $P_{f} = 1 - \exp\left[-\left(\frac{\sigma_{max}}{\sigma_{\theta}}\right)^{m}\right] \sigma_{max} > 0$ (1) $P_{f} = 0 \quad \sigma_{max} \le 0$ (2)

where:

 P_f = the probability of failure, σ_{max} = maximum tensile stress in a test specimen at failure, σ_{θ} = the Weibull characteristic strength (corresponding to $a P_f = 0.632$ or 63.2 %), and m = Weibull modulus.

6.1.2 As noted earlier, the Weibull characteristic strength is dependent on the test specimen and will change with test specimen geometry as well as the stress state. The Weibull characteristic strength has units of stress, and should be reported using units of MPa or GPa. As was noted in the previous section, strength controlling flaws can be spatially distributed over the volume or the surface (area) of a test specimen. If the strength controlling flaws are volumedistributed, the volume characteristic strength shall be designated as $(\sigma_{\theta})_{V}$, and the volume Weibull modulus shall be designated m_V . If the strength controlling flaws are surfacedistributed, the area characteristic strength shall be designated as $(\sigma_{\theta})_A$, and the area Weibull modulus shall be designated m_A . Fractographic Practice C1322 should be used to determine whether flaws are surface- or volume-distributed. It should be borne in mind that a flaw *located* at the surface of a test specimen does not necessarily mean it was a surfacedistributed flaw. It may be a surface-distributed flaw, or it may be a volume-distributed flaw which by chance is located at the surface.

6.2 Volume Distribution:

6.2.1 An alternative expression for the probability of failure is given by:

$$P_{f} = 1 - \exp\left[\int_{V} \left(\frac{\sigma}{(\sigma_{0})_{V}}\right)^{m_{V}} dV\right]$$
(3)

$$P_f = 0 \quad \sigma \le 0 \tag{4}$$

6.2.1.1 The integration within the exponential function is performed over all tensile stressed regions of the test specimen volume if the strength-controlling flaws are randomly distributed through the volume of the material. m_V is the Weibull modulus associated with strength controlling flaws distributed through the volume. $(\sigma_0)_V$ is the Weibull material scale parameter and can be described as the Weibull characteristic strength of a hypothetical test specimen with unit volume loaded in uniform uniaxial tension. The Weibull material scale

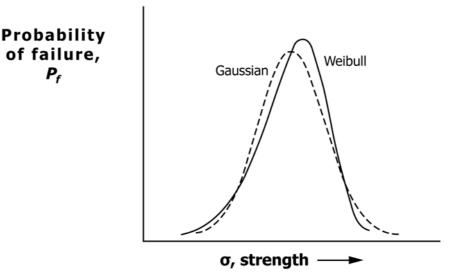


FIG. 2 The Probability Density Function Graphs for Weibull and Gaussian (Normal) Strength Distributions

parameter has units of stress (volume)^{1/m_V} and should be reported using units of MPa·(m)^{3/m_V} or GPa·(m)^{3/m_V}. Eq 1 and Eq 3 can be equated for a given test specimen geometry, which yields an expression relating $(\sigma_0)_V$ and $(\sigma_0)_V$ for that test specimen geometry. Expressions for specific test specimen geometries are presented in Sections 7 and 8.

6.2.2 For the general case where stress varies with position within a test specimen are volume-distributed, the integration given by Eq 3 can be carried out to yield the following expression:

$$P_{f} = 1 - \exp\left[-kV\left(\frac{\sigma_{max}}{(\sigma_{0})_{V}}\right)^{m_{V}}\right]$$
(5)

6.2.2.1 Here k is a dimensionless factor and has been identified as a "load factor" (e.g., Johnson and Tucker (6)). σ_{max} is the maximum stress in the test specimen at failure. Thus, in general:

$$\left(\sigma_{0}\right)_{V} = \left(\sigma_{\theta}\right)_{V} \left(kV\right)^{1/m_{V}} = \left(\sigma_{\theta}\right)_{V} V_{E}^{-1/m_{V}}$$

$$(6)$$

when the strength controlling flaws are spatially distributed through the volume. Inclusions are an example of such flaws. For all loading geometries except uniaxial tension (see 7.1), k is a function of the Weibull modulus m and the test geometry. The load factor is evaluated numerically and is always positive and usually less than unity. Notice that the Weibull modulus in this instance, m_{V_2} is associated with volume flaws.

6.2.3 The product k times V is often termed an "effective volume, V_E ," in the ceramic literature. The effective volume is the size of a hypothetical tension test specimen that, when stressed to the same level as the test specimen in question, has the same probability of fracture. Expressions for the effective volume of specific test specimen geometries are given Sections 7 and 8. Noting that $(\sigma_0)_V$ is a material parameter (that is in principle independent of the test specimen type), then:

$$(\sigma_0)_V = (\sigma_{\theta,1})_V (k_1 V_1)^{1/m_V} = (\sigma_{\theta,2})_V (k_2 V_2)^{1/m_V}$$
(7)

where the subscripts 1 and 2 denote two different geometries of test specimens fabricated from the same material. This leads to the following relationship:

$$\frac{(\sigma_{\theta,1})_{V}}{(\sigma_{\theta,2})_{V}} = \frac{(k_{2}V_{2})^{1/m_{V}}}{(k_{1}V_{1})^{1/m_{V}}} = \left(\frac{k_{2}V_{2}}{k_{1}V_{1}}\right)^{1/m_{V}} = \left(\frac{V_{E,2}}{V_{E,1}}\right)^{1/m_{V}}$$
(8)

6.2.3.1 It is implied that the same type of volumedistributed flaws control strength in each geometry. Eq 8 means that knowledge of the effective volume of both specimen types allows the computation of one characteristic strength value based on the characteristic strength value of the other specimen geometry. Test specimens with stress gradients have effective volumes less than the size of the test piece. In other words, k < 1. For example, flexural strength specimens expose only a small amount of material to the maximum stress and k << 1. The flexure specimen is "equivalent" to a much smaller test piece that is pulled in uniaxial direct tension. The k factors depend upon the geometry and loading configuration and they usually are very sensitive to the Weibull modulus.

6.3 Surface Distribution:

6.3.1 If the strength controlling flaws are distributed along the surface of the test specimens, then the following expression:

$$P_{f} = 1 - \exp\left[\int_{A} \left(\frac{\sigma}{(\sigma_{0})_{A}}\right)^{m_{A}} dA\right]$$
(9)

$$P_f = 0 \quad \sigma \le 0 \tag{10}$$

shall be utilized for the probability of failure. The integration within the exponential is performed over all tensile regions of the test specimen surface. The integration is sometimes carried out over the area of an effective gage section instead of over the total area of the test specimen. In Eq 9, m_A is the Weibull modulus associated with surface flaws. $(\sigma_0)_A$ is the Weibull material scale parameter and can be described as the Weibull characteristic strength of a test specimen with unit surface area loaded in uniform uniaxial tension. Here the Weibull material scale parameter should be reported using units of MPa·(m)^{2/m_A} or GPa·(m)^{2/m_A}. For a given test specimen geometry, Eq 1 and Eq 9 can be equated, which yields an expression relating $(\sigma_0)_A$ and $(\sigma_0)_A$. Expressions for specific test specimen geometries are presented in Sections 7 and 8.

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6.3.2 For the general case where stress varies within a test specimen and the flaws are surface distributed, the integration given by Eq 3 can be carried out for the surface areas of the specimens that are stressed in tension. This yields the following expression:

$$P_{f} = 1 - \exp\left[-kA\left(\frac{\sigma_{max}}{(\sigma_{0})_{A}}\right)^{m_{A}}\right]$$
(11)

6.3.2.1 Again, k is a dimensionless factor and has been identified as a "load factor" (e.g., Johnson and Tucker (6)). For all loading geometries except uniaxial tension (see 7.1), k is a function of the Weibull modulus m and the test geometry. Notice that the Weibull modulus in this instance, m_A , is associated with surface flaws. σ_{max} is the maximum stress in the test specimen at failure. Thus, in general:

$$\left(\sigma_{0}\right)_{A} = \left(\sigma_{\theta}\right)_{A} \left(kA\right)^{1/m_{A}} = \left(\sigma_{\theta}\right)_{A} S_{E}^{-1/m_{A}}$$
(12)

when the strength controlling flaws are spatially distributed along the surfaces of the test specimens. Surface grinding cracks are an example of such.

Note 1—The conventional nomenclature in the literature is used here. *Areas* are denoted by symbols with the letter *A*. The effective area or effective *surface* is commonly denoted by the letter *S*.

6.3.3 For all loading geometries except for uniaxial tension (see 7.2), k is a function of the Weibull modulus m. The load factor, k, is evaluated numerically and is always positive and usually less than unity. In the ceramics literature, the product k times A is often termed an "effective area" or "effective surface, S_E ." The effective surface is the size of a hypothetical uniaxial tensile test specimen that, when stressed to the same level as the test specimen in question, has the same probability of fracture. Expressions for the effective area of specific test specimen geometries are given in Sections 7 and 8. Noting that $(\sigma_0)_A$ is a material parameter (that is in principle independent of the test specimen type), then:

$$\frac{\left(\sigma_{\theta,1}\right)_{A}}{\left(\sigma_{\theta,2}\right)_{A}} = \frac{\left(k_{2}A_{2}\right)^{1/m_{A}}}{\left(k_{1}A_{1}\right)^{1/m_{A}}} = \left(\frac{k_{2}A_{2}}{k_{1}A_{1}}\right)^{1/m_{A}} = \left(\frac{S_{E,2}}{S_{E,1}}\right)^{1/m_{A}}$$
(13)

where the subscripts 1 and 2 denote two different geometries for test specimens fabricated from the same material. It is implied that the same type of surface-distributed flaws control strength in each geometry. Eq 13 means that knowledge of the effective surfaces of both specimen types allows the computation of one characteristic strength value based on the characteristic strength value of the other specimen geometry. Test specimens with stress gradients have effective surface areas that are less than the size of the test piece and k < 1. The flexure specimen is "equivalent" to a smaller test piece that is pulled in uniaxial direct tension. The *k* factors depend upon the geometry and loading configuration and they usually are very sensitive to the Weibull modulus.

6.4 Mixed Distributions:

6.4.1 Strength scaling relations such as Eq 8 and Eq 13 shall not be used to scale strengths where the flaw type in one test specimen type is surface-distributed (e.g., machining cracks) and the flaw type in the second specimen type is volumedistributed (e.g. inclusions), or vice versa. The scaling equations are only suited for cases where the *same* flaw type is active in the two specimen types. For example, if inclusions control strength in specimen type 1, then the scaling may be suitable if inclusions control strength in specimen type 2. If inclusions control strength in specimen type 1, but pores control strength in specimen type 2, then the correlation will probably not be accurate.

6.5 What May be Scaled:

6.5.1 Eq 8 and Eq 13 are for scaling the Weibull characteristic strengths, σ_0 , of two different type specimens. The characteristic strengths correspond to a probability of failure, P_f , of 63.2 % for each test specimen set. The equations may also be used to scale strengths at other probabilities of failure, P_f . For example, the median strength ($P_f = 50$ %) of one specimen type can be compared to the median strength of another size or type specimen. Similarly, the strengths at a 1 % probability of failure may be scaled.

NOTE 2—These equations may also be used to scale mean strengths, since they closely approximate the median strengths.

NOTE 3—Scaling predictions or correlations at the 1 % probabilities of failure will be subject to considerable uncertainty, since the confidence intervals for such estimates are much broader than those for the characteristic, median, or mean strengths. It is beyond the scope of this Practice to quantify the confidence intervals for the scaled strengths.

6.6 *Edge-Distributed*:

6.6.1 Weibull edge or length scaling is not covered in this practice. In principle, the same concepts and similar mathematics could be used to scale strengths for edge-distributed flaws, however edge-distributed flaws are often very specific to a particular test specimen type. Edge-distributed flaws are those which form as a result of some process such as chipping, cutting, or grinding and are only found at an edge. Volume or

surface type flaws such as pores, inclusions, or normal grinding cracks, which by chance are *located* at a test specimen edge, are not considered edge-distributed flaws. If test specimens have origins that are by nature edge-distributed flaws, the data should be censored as discussed in Practice C1322 in order to properly analyze the surface- and volume distribution parameters.

7. Test Specimens with Uniaxial Stress States—Effective Volume and Area Relationships

7.1 Uniaxial Tensile Test Specimens:

7.1.1 For ambient test temperatures uniaxial tensile test specimens such as shown in Fig. 3 should be tested in accordance with Practice C1273. For elevated test temperatures tensile test specimens shall be tested in accordance with Test Method C1366. Various accepted test specimen geometries are presented within these standards. In general, the volume of material subjected to a uniform tensile stress for a single uniaxially-loaded tensile test specimen may be many times that of a single flexural test specimen. Strength values obtained using the different recommended tensile test specimens (Practice C1273 or Test Method C1366) with different volumes (areas) of material will be different due to these volume (area) differences. Characteristic or mean strength values can be scaled to any gage section and to other test configurations using the volume and area relationships presented in this section, which are applicable to the test specimen geometries presented in Practice C1273 and Test Method C1366.

7.1.2 Volume Distribution—The relationship between the characteristic strength $(\sigma_{0T})_V$ and the Weibull material scale parameter $(\sigma_0)_V$ for a tension test specimen with volume flaws is:

$$\left(\sigma_{0}\right)_{V} = \left(\sigma_{\theta T}\right)_{V} V_{T}^{1/m_{V}}$$
(14)

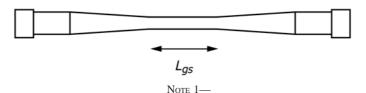
7.1.2.1 This expression is obtained by setting Eq 1 equal to Eq 3, after the integration in Eq 3 has been performed over the gage section volume of the uniaxial tensile test specimen. Thus V_T is the volume of the gage section. Comparison of Eq 14 with Eq 6 yields the following formulation for the effective volume:

$$V_E = kV = V_T \tag{15}$$

7.1.2.2 Thus, for uniaxial tension, k is equal to unity. An expression (7) similar to Eq 14 can be derived relating the material scale parameter to the average uniaxial tensile strength, that is:

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$$\left[\sigma_{0}\right]_{V} = \frac{\left(\overline{\sigma}_{T}\right)_{V} V_{T}^{1/m_{V}}}{\Gamma\left[\frac{1}{m_{V}}+1\right]}$$
(16)



 L_{gs} is the length of the gage section.

FIG. 3 Example of a Round Tension Strength Specimen