# INTERNATIONAL STANDARD

# ISO/IEC 20008-2

First edition 2013-11-15

**AMENDMENT 2** 

## Information technology — Security techniques — Anonymous digital signatures —

Part 2: Mechanisms using a group public key

## iTeh STAAMENDMENT 2 EVIEW

ST Technologies de l'information — Techniques de sécurité — Signatures numériques anonymes —

Partie 2: Mécanismes utilisant une clé publique de groupe

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# **PROOF/ÉPREUVE**



Reference number ISO/IEC 20008-2/Amd. 2:2023(E)

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ISO/IEC 20008-2:2013/PRF Amd 2

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Published in Switzerland

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## Information technology — Security techniques — Anonymous digital signatures —

## Part 2: Mechanisms using a group public key

## **AMENDMENT 2**

Clause 4

Add the following symbol:

F(p)the finite field containing exactly *p* elements.

6.1

# Replace the first sentence with the following:

This clause specifies five digital signature mechanisms with linking capability.

Replace the text of NOTE 1 with the following:

In the literature, the mechanism of 6.2 is called a list signature scheme, the mechanism of 6.6 is called a pre-DAA scheme and the mechanisms of 6.3, 6.4 and 6.5 are called DAA schemes. The mechanisms given in 6.2, 6.4, 6.5 and 6.6 are based on schemes originally specified in References [9], [6], [11] and [22] respectively, in which security proofs can also be found. The mechanism in 6.3 is based on a scheme in Reference [3] which is a minor modification of the scheme in Reference [4]; the associated security analysis is given in the full version of Reference [4].

6.6

Add new subclause 6.6 as follows:

#### 6.6 Mechanism 8

#### 6.6.1 Symbols

The following symbols apply in the specification of this mechanism.

- $\tau$ : a security parameter.
- $P_1, Q_1, X_1, Y_1, X_1', \tilde{X}_1, C_1, D, D', T_1, T_2, K_1, K_2, K, K_1', K_2', K', J, T_1', T_2', R, R', T, T', R'', T'': elements of$ *G*<sub>1</sub>.
- $P_2$ ,  $X_2$ ,  $Y_2$ ,  $X'_2$ ,  $\tilde{X}_2$ : elements of  $G_2$ .
- $-x, y, z, x', z', c_k, s_x, s_z, c'_k, s_1, u, v, w, v', r, s_2, k_r, k_x, k_z, c, z_r, z_x, z_z, c', s, l, k_s, c_m, \rho, c'_m$ : integers in  $Z_n$

- $n_l$ : an integer of size  $\tau$  -bit.
- $H_1$ : a hash function that outputs elements in  $G_1$ .
- $H_2$ ,  $H_3$ : hash functions that output elements in  $Z_p$ .

#### 6.6.2 Key generation process

The key generation process has two parts: setup process and group membership issuing process. The setup process is executed by the group membership issuer to create the group public parameter, group public key, and group membership issuing key. The group membership issuing process is an interactive protocol running between the group membership issuer and a group member to create a unique group member signature key for the group member.

The setup process takes the following steps by the group membership issuer:

- a) Choose  $\tau$  as a security parameter.
- b) Choose a bilinear group pair  $(G_1, G_2)$  of large prime order p, such that no efficiently computable homomorphism is known between  $G_1$  and  $G_2$ , in either direction, and an associated pairing function  $e: G_1 \times G_2 \to G_T$ .
- c) Choose two random independent generators  $P_1$  and  $Q_1$  of  $G_1$  and provide additional information, denoted by  $\pi_{\text{Gen}}$ , that serve to demonstrate that these two generators were indeed chosen independently, that is without a potentially exploitable relationship between them (such as  $Q_1 = [s]P_1$  for an integer s chosen by the group membership issuer). An example of how to verifiably select independent generators and to verify, using  $\pi_{\text{Gen}}$ , the correct generation of these generators, is given in Annex G.
- d) Choose a random generator  $P_2$  of  $G_2$ . Inc. 20008-2-2013-prf-amd-2
- e) Choose three hash functions  $H_1: \{0,1\}^* \to G_1$ ,  $H_2: \{0,1\}^* \to Z_p$  and  $H_3: \{0,1\}^* \to Z_p$ . An example of how to construct such hash functions is provided in Annex B.
- f) Choose three random integers x, y and z in  $Z_p$ .
- g) Compute  $X_1 = [z]P_1 + [x]Q_1$ ,  $Y_1 = [y]P_1$ ,  $X_2 = [x]P_2$  and  $Y_2 = [y]P_2$ .
- h) Choose two random integers x' and z' in  $Z_p$ .
- i) Compute  $X'_1 = [z']P_1 + [x']Q_1$  and  $X'_2 = [x']P_2$ .
- j) Compute  $c_k = H_2(P_1 || Q_1 || P_2 || X_1 || Y_1 || X_2 || Y_2 || X'_1 || X'_2).$
- k) Compute  $s_x = (x' + c_k \times x) \mod p$  and  $s_z = (z' + c_k \times z) \mod p$ .
- l) Set  $\pi_{Val} = (c_k, s_x, s_z)$  as a proof that the second component of the representation of  $X_1$  in the base  $P_1$  and  $Q_1$  is equal to the discrete logarithm of  $X_2$  in the base  $P_2$ .
- m) Output the following:
  - group public parameter = ( $G_1$ ,  $G_2$ ,  $G_T$ , e,  $P_1$ ,  $Q_1$ ,  $P_2$ , p,  $H_1$ ,  $H_2$ ,  $H_3$ ),
  - group public key = ( $X_1$ ,  $Y_1$ ,  $X_2$ ,  $Y_2$ ,  $\pi_{Gen}$ ,  $\pi_{Val}$ ),
  - group membership issuing key = (x, y, z).
- NOTE 1 Examples of recommended parameters are provided in C.2.

Each entity involved in this anonymous signature mechanism should verify the validity of the group public key before using it. The group public key validity verification process includes the following steps:

- a) Verify that  $P_1$  and  $Q_1$  were generated independently using  $\pi_{\text{Gen}}$ .
- b) Verify the validity of the proof  $\pi_{Val}$ :
  - 1) Compute  $\tilde{X}_1 = [s_z]P_1 + [s_x]Q_1 [c_k]X_1$  and  $\tilde{X}_2 = [s_x]P_2 [c_k]X_2$ .
  - 2) Compute  $c'_{k} = H_{2}(P_{1} \parallel Q_{1} \parallel P_{2} \parallel X_{1} \parallel Y_{1} \parallel X_{2} \parallel Y_{2} \parallel \tilde{X}_{1} \parallel \tilde{X}_{2}).$
  - 3) Verify that  $c_k = c_k$ .
- c) Verify that  $e(Y_1, P_2) = e(P_1, Y_2)$ .
- d) If any of the above verifications fails, output 0 (invalid), otherwise output 1 (valid).

The group membership issuing process requires a secure and authentic channel between the group member and the group membership issuer. How to establish such a channel is out scope of this mechanism. The group membership issuing process includes the following steps:

- a) The group membership issuer chooses a nonce  $n_I \in \{0, 1\}^{\tau}$ .
- b) The group membership issuer sends  $n_I$  to the member.
- c) The member chooses a random integer  $s_1$  from  $Z_p$ .
- d) The member computes  $C_1 = [s_1]Y_1$ . **and s.iteh.ai**)
- e) The member chooses a random integer u from  $Z_p$ .

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- f) the member computes  $D = [u]Y_{1:rds/sist/cfd84dbf-ced8-4363-a0e0-269b5873e0b1/iso-$
- g) The member computes  $v = H_2(P_1 || Q_1 || P_2 || X_1 || Y_1 || X_2 || Y_2 || C_1 || D || n_1).$
- h) The member computes  $w = (u + v \times s_1) \mod p$ .
- i) The member sends ( $C_1$ , v, w) to the group membership issuer.
- j) The group membership issuer computes  $D' = [w]Y_1 [v]C_1$ .
- k) The group membership issuer computes  $v' = H_2(P_1 || Q_1 || P_2 || X_1 || Y_1 || X_2 || Y_2 || C_1 || D' || n_1)$ .
- l) The group membership issuer verifies v = v'. If the verification fails, abort the group membership issuing process.
- m) The group membership issuer selects five random integers r,  $s_2$ ,  $k_r$ ,  $k_x$  and  $k_z$  from  $Z_p$ .
- n) The group membership issuer computes  $T_1 = [r]P_1$  and  $T_2 = [x]T_1 + [r]C_1 + [r \times s_2]Y_1$ .
- o) The group membership issuer computes  $K_1 = [k_r]P_1$ ,  $K_2 = [k_x]T_1 + [k_r](C_1 + [s_2]Y_1)$  and  $K = [k_z]P_1 + [k_x]Q_1$ .
- p) The group membership issuer computes  $c = H_2(P_1 || Q_1 || P_2 || X_1 || Y_1 || X_2 || Y_2 || C_1 || s_2 || K_1 || K_2 || K$ ).
- q) The group membership issuer computes  $z_r = (k_r + c \times r) \mod p$ ,  $z_x = (k_x + c \times x) \mod p$ and  $z_z = (k_z + c \times z) \mod p$ .
- r) The group membership issuer sets  $(T_1, T_2)$  as the member's group membership credential and sends  $(T_1, T_2, s_2, c, z_r, z_x, z_z)$  to the member.

- The member computes  $K_1' = [z_r]P_1 [c]T_1$ ,  $K_2' = [z_x]T_1 + [z_r](C_1 + [s_2]Y_1) [c]T_2$  and  $K' = [z_1]P_1 [c]T_2$ s)  $[z_{z}]P_{1} + [z_{x}]Q_{1} - [c]X_{1}.$
- The member computes  $c' = H_2(P_1 || Q_1 || P_2 || X_1 || Y_1 || X_2 || Y_2 || C_1 || s_2 || K'_1 || K'_2 || K)$ . t)
- The member verifies c = c'. If the verification fails, the member aborts. u)
- The member computes  $s = (s_1 + s_2) \mod p$ . V)
- The group member signature key for the member is (s,  $T_1$ ,  $T_2$ ). w)

The group membership issuer can use the same value  $s_2$  (for example  $s_2 = 0 \mod p$ ) for several NOTE 2 executions of the group membership issuing process. In this case, the security of Mechanism 8 relies on the Pointcheval-Sanders (PS) assumption<sup>[24]</sup>, instead of the q-MSDH assumption<sup>[25]</sup> if the group membership issuer uses a fresh random value  $s_2$  for each new session of the group membership issuing process.

#### 6.6.3 Signature process

On input of a group member signature key (s,  $T_1$ ,  $T_2$ ), a linking base bsn and a message  $m \in \{0,1\}^*$  to be signed, the signature process takes the following steps. The linking base, denoted by bsn, is either a special symbol  $\perp$  or an arbitrary string used for the linking capability.

- If  $bsn = \bot$ , the signer chooses a random J from  $G_1$ , otherwise, computes  $J = H_1(bsn)$ . a)
- The signer selects two random integers l and  $k_s$  in  $Z_p$ . b)
- The signer computes  $T_1 = [l]T_1$  and  $T_2 = [l]T_2$ . c)
- d)
- The signer computes  $R = [s]T_1$  and  $R' = [k_s]T_1$ . https://standards.iteh.ai/catalog/standards/sist/cfd84dbf-ced8-4363-a0e0-269b5873e0b1/iso-
- The signer computes T = [s]J and  $T' = [k_s]J$ . e)
- The signer computes  $c_m = H_3(T_1' || T_2' || J || T || R || T' || R' || m)$ . f)
- The signer computes  $\rho = (k_s + c_m \times s) \mod p$ . g)
- The signer outputs the anonymous signature  $\sigma = (T_1, T_2, J, R, T, c_m, \rho)$ . h)

#### 6.6.4 Verification process

On input of a message m, a linking base bsn, a signature  $(T_1, T_2, J, R, T, c_m, \rho)$  and a group public key (  $X_1$ ,  $Y_1$ ,  $X_2$ ,  $Y_2$ ), the verification process takes the following steps:

- a) If  $bsn \neq \bot$ , verify that  $J = H_1(bsn)$ .
- b) Verify that  $T_1 \neq O_F$ .
- If any of the above verifications fails, output 0 (invalid). c)
- Compute  $R'' = [\rho]T_1 [c_m]R$ . d)
- Compute  $T'' = [\rho]J [c_m]T$ . e)
- Compute  $c'_m = H_3(T'_1 || T'_2 || J || T || R || T'' || R'' || m)$ . f)

- g) Verify that  $c'_m = c_m$ .
- h) Verify that  $e(T'_1, X_2) \times e(R, Y_2) = e(T'_2, P_2)$ .
- i) Optionally, call the revocation checking process.
- j) If any of the above verifications (steps g and h) fails, output 0 (invalid). Otherwise, output 1 (valid).

#### 6.6.5 Linking process

Given two valid signatures  $\sigma = (T_1', T_2', J, R, T, c_m, \rho)$  and  $\hat{\sigma} = (\hat{T}_1', \hat{T}_2', \hat{J}, \hat{R}, \hat{T}, \hat{c}_m, \hat{\rho})$ , the linking process takes the following steps:

a) If  $J = \hat{J}$  and  $T = \hat{T}$ , output 1 (linked), otherwise, output 0 (not linked).

NOTE If the linking process outputs 0 because of  $J \neq \hat{J}$ , it means that the linking process cannot determine whether two signatures were created by the same group member.

#### 6.6.6 Revocation process

Details of the revocation process in this mechanism are surveyed in Reference [10]. There are two types of revocation (private key revocation and verifier blacklist revocation) supported in this mechanism. Private key revocation can be either global revocation or local revocation. Verifier blacklist revocation is a local revocation.

Private key revocation:

- If a group member signature key (s, T<sub>1</sub>, T<sub>2</sub>) is compromised, the group membership issuer puts s into a revocation list RL of this type.
- Given a valid signature  $\sigma = (T_1', T_2', J, R, T, c_m, \rho)$  computed using a linking base *bsn* and a revocation list RL of this type, a verifier can check revocation of this signature as follows: for each  $s' \in RL$ , verify  $T \neq [s']J$ . If any of these verifications fails, output 0 (revoked), otherwise, output 1 (valid).

NOTE The private key revocation works only if the group membership issuer or the verifier has learned the group member signature keys of the compromised group members. This revocation process allows to identify every group signature generated using this private key. If this key can be associated with a group member (e.g. by using contextual information), then no anonymity can be retained for this group member as their signatures can therefore be traced. This is a property inherent to DAA schemes. Thus, a careful assessment of the need for revocation and the consequences for the corresponding group member will be carried out before deployment.

Verifier blacklist revocation:

- If signatures were computed using a linking base *bsn*, a verifier can build its own revocation list RL corresponding to *bsn*. If the verifier wants to blacklist the signer of a valid signature  $\sigma = (T_1, T_2, J, R, T, c_m, \rho)$ , they put *T* into a revocation list RL of this type.
- Given a signature  $\sigma = (T_1, T_2, J, R, T, c_m \rho)$  computed using a linking base *bsn* and a revocation list RL of this type, a verifier can check revocation of this signature as follows: for each  $\hat{T} \in RL$ , verify  $T \neq \hat{T}$ . If any of these verifications fails, output 0 (revoked), otherwise, output 1 (valid).

In order to use verifier blacklist revocation in this mechanism, a signer must use a specific linking base for each verifier. The value of the linking base can, for example, be chosen by the verifier or agreed in advance by the signer and verifier.

#### 7.1

Replace the first sentence with the following:

This clause specifies three digital signature mechanisms with opening capability.

Replace the text of NOTE with the following:

The mechanisms and associated security proofs in 7.2, 7.3 and 7.4 are based on References [17], [14] and [23] (an extended version of Reference [24]), respectively.

#### 7.4

Add new subclause 7.4 as follows:

#### 7.4 Mechanism 9

#### 7.4.1 Symbols

The following symbols apply in the specification of this mechanism.

- $P_1$ ,  $S_i$ ,  $T_1$ ,  $T_2$ , K, K',  $T_1'$ ,  $T_2'$ : elements of  $G_1$ .
- $P_2, X, Y, A, B, Y_i, C_1, C_2, C_3, C_4, K_1, K_2, K_3, K_4, K_1, K_2, K_3, K_4': elements of G_2.$
- $W, W', R, R_i$ : elements of  $G_T$ . (standards.iteh.ai)
- $x, y, a, b, s_i, u, v, k_s, k_u, k_v, c, z_s, z_u, z_v, c', r, t, w, c_m, z, c'_m: elements of Z_p.$
- H: a hash function that outputs elements in  $Z_p$ ; st/cfd84dbf-ced8-4363-a0e0-269b5873e0b1/isoiec-20008-2-2013-prf-amd-2

#### 7.4.2 Key generation process

The group membership issuer key generation process takes the following steps:

- a) Choose a bilinear group pair  $(G_1, G_2)$  of large prime order p, such that no efficiently computable homomorphism is known between  $G_1$  and  $G_2$ , in either direction, and an associated pairing function  $e: G_1 \times G_2 \to G_T$ .
- b) Choose a random generator  $P_1$  of  $G_1$  and a random generator  $P_2$  of  $G_2$ .
- c) Choose two random integers x and y in  $Z_p$ .
- d) Compute  $X = [x]P_2$  and  $Y = [y]P_2$ .
- e) Choose a hash function  $H: \{0,1\}^* \to Z_p$ . Such a hash function shall be constructed as described in Annex B.
- f) Output the following:
  - group public parameters:  $(G_1, G_2, G_T, e, p, H, P_1, P_2)$ ,
  - group public key: (X, Y),
  - group membership issuing key: ( *x* , *y* ).

The group membership opener key generation process takes the following steps:

- a) Choose two random integers a and b in  $Z_p$ .
- b) Compute  $A = [a]P_2$  and  $B = [b]P_2$ .
- c) Output the following:
  - group membership opener public key (*A*, *B*),
  - group membership opening key (*a*, *b*).

The group membership issuer manages a member-list **LIST** = (LIST[1],..., LIST[n]) where n is the number of group members who are registered so far. Each entry of the list contains information associated with each registered user. This member-list **LIST** can be published but it will only be useful to the group membership opener.

The group membership issuing process is an interactive protocol running between the group membership issuer and a user  $U_i$  to create a group member signature key for the user. It consists of the following steps:

- a)  $U_i$  selects six random integers  $s_i$ , u, v,  $k_s$ ,  $k_u$  and  $k_v$  in  $Z_p$ .
- b)  $U_i$  computes  $S_i = [s_i]P_1$  and  $Y_i = [s_i]Y$ .
- c)  $U_i$  computes  $C_1 = [u]P_2$ ,  $C_2 = Y_i + [u]A$ ,  $C_3 = [v]P_2$ ,  $C_4 = Y_i + [v]B$ .
- d)  $U_i$  computes  $K = [k_s]P_1$ ,  $K_1 = [k_u]P_2$ ,  $K_2 = [k_s]Y + [k_u]A$ ,  $K_3 = [k_v]P_2$ ,  $K_4 = [k_s]Y + [k_v]B$ .
- e)  $U_i$  computes  $c = H(P_1 || P_2 || X || Y || A || B || S_i || Y_i || C_1 || C_2 || C_3 || C_4 || K || K_1 || K_2 || K_3 || K_4)$ .
- f)  $U_i$  computes  $z_s = (k_s + c \times s_i) \mod p$ ,  $z_u = (k_u + c \times u) \mod p$  and  $z_v = (k_v + c \times v) \mod p$ .
- https://standards.iteh.al/catalog/standards/sist/cid84dbi-ced8-4363-a0e0-269b58/3e0b1/iso-
- g)  $U_i$  sends  $S_i$ ,  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_4$ , c,  $z_s$ ,  $z_u$  and  $z_v$ . 3-prf-and-
- h) The group membership issuer computes  $K' = [z_s]P_1 [c]S_i$ ,  $K'_1 = [z_u]P_2 [c]C_1$ ,  $K'_2 = [z_s]Y + [z_u]A [c]C_2$ ,  $K'_3 = [z_v]P_2 [c]C_3$  and  $K'_4 = [z_s]Y + [z_v]B [c]C_4$ .
- i) The group membership issuer computes  $c' = H(P_1 || P_2 || X || Y || A || B || S_i || Y_i || C_1 || C_2 || C_3 || C_4 || K' || K'_1 || K'_2 || K'_3 || K'_4).$
- j) The group membership issuer checks if c = c' and aborts if these two values are different.
- k) The group membership issuer stores  $(i, S_i, C_1, C_2, C_3, C_4, c, z_s, z_u, z_v)$  in LIST[i].
- 1) The group membership issuer selects a random integer r in  $Z_n$ .
- m) The group membership issuer computes  $T_1 = [r]P_1$  and  $T_2 = [r \times x]P_1 + [r \times y]S_i$ .
- n) The group membership issuer sends  $T_1$  and  $T_2$  to the user  $U_i$ .
- o) The signature key of the group member  $U_i$  is then  $(s_i, T_1, T_2)$ .

#### 7.4.3 Signature process

On input of a group public key (*X*, *Y*), a group member signature key ( $s_i$ ,  $T_1$ ,  $T_2$ ) owned by the signer and a message  $m \in \{0,1\}^*$  to be signed, the signature process takes the following steps.

- a) The signer selects two random integers t and w in  $Z_p$ .
- b) The signer computes  $T_1' = [t]T_1$  and  $T_2' = [t]T_2$ .
- c) The signer computes  $W = e([w]T_1, Y)$ .
- d) The signer computes  $c_m = H(T_1 || T_2 || W || m)$ .
- e) The signer computes  $z = (w + c_m \times s_i) \mod p$ .
- f) The signer outputs the group signature  $\sigma = (T_1', T_2', c_m, z)$ .

#### 7.4.4 Verification process

On input of a message  $m \in \{0,1\}^*$ , a group signature  $\sigma = (T_1, T_2, c_m, z)$  and a group public key (*X*, *Y*), the verification process takes the following steps:

- a) Verify that  $T'_1 \neq O_E$ . If this verification fails, output 0 (invalid).
- b) Compute  $W' = e([z]T_1, Y) \times e([-c_m]T_2, P_2) \times e([c_m]T_1, X).$
- c) Compute  $\dot{c_m} = H(T_1 || T_2 || W' || m)$ . **10** and **31** iteh.ai)
- d) Verify that  $c'_m = c_m$  holds.

ISO/IEC 20008-2:2013/PRF Amd 2

e) If the above verification fails, output 0 (invalid), otherwise, output 1 (valid). 26955873e061/iso

#### 7.4.5 Opening process

Given a group signature  $\sigma = (T_1, T_2, c_m, z)$ , the member-list **LIST**=(LIST[1],...,LIST[*n*]) and a group opening key (*a*, *b*), the opening process takes the following steps:

- a) Compute  $R = e(T_2, P_2) \times e([-1]T_1, X)$ .
- b) For each  $i \in [1, n]$ ,
  - 1) Recover  $(i, S_i, C_1, C_2, C_3, C_4, c, z_s, z_u, z_v)$  from LIST[i].
  - 2) Compute  $Y_i = C_2 + [-a]C_1$ .
  - 3) Verify if  $e(T_1, Y_i) = R$ .
  - 4) If the above equation holds, output *i*.

#### 7.4.6 Revocation process

The revocation process is a membership credential revocation. The group membership opener revokes a user  $U_i$  by adding some element  $R_i$  (defined below) specific to this user in a revocation list RL. Revocation can thus be global but also local as any verifier is able to manage its own revocation list by