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Standard Test Method for Determining the Effective X-Ray Elastic Parameter for X-Ray Diffraction Measurements—Constants for Use in the Measurement of Residual Stress Using X-Ray Diffraction Techniques¹

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^{ε1} NOTE—9.7 was editorially revised in September 2009.

INTRODUCTION

When a crystalline material is strained, the spacing between parallel planes of atoms, ions, or molecules in the lattice change. X-Ray diffraction techniques can measure these changes and, therefore, they constitute a powerful means for studying the residual stress state in a body. The calculation of macroscopic stresses from using lattice strains requires a material constant, the use of X-ray elastic constants (XEC-effective elastic parameter, that) which must be empirically determined by X-ray diffraction techniques as described in this test method.

1. Scope

1.1 This test method covers a procedure for experimentally determining the effective X-ray elastic parameter constants $E(XEC)_{eff}$ for the evaluation of residual and applied stresses by X-ray diffraction techniques. The effective XEC elastic parameter relates macroscopic stress to the strain measured in a particular crystallographic direction in polycrystalline samples. The $E(XEC)_{eff}$ should not be confused with a function of the E , elastic modulus, Poisson's ratio of the material and the hkl the modulus of elasticity. Rather, it is nominally equivalent to plane selected for the measurement. There are two $E(XEC)(1 + \nu)$ for the particular crystallographic direction, where that are referred to as $1/2 \nu S_2^{hkl}$ is Poisson's ratio. The effective elastic parameter is influenced by elastic anisotropy and preferred S_1^{hkl} orientation of the sample material.

1.2 This test method is applicable to all X-ray diffraction instruments intended for measurements of macroscopic residual stress that use measurements of the positions of the diffraction peaks in the high back-reflection region to determine changes in lattice spacing.

1.3 This test method is applicable to all X-ray diffraction techniques for residual stress measurement, including single, double, and multiple exposure techniques.

1.4 The values stated in inch-pound units are to be regarded as standard. The values given in parentheses are mathematical conversions to SI units that are provided for information only and are not considered standard.

1.5 This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.

2. Referenced Documents

2.1 ASTM Standards:²

E4 Practices for Force Verification of Testing Machines

¹ This test method is under the jurisdiction of ASTM Committee E28 on Mechanical Testing and is the direct responsibility of Subcommittee E28.13 on Residual Stress Measurement.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For Annual Book of ASTM Standards volume information, refer to the standard's Document Summary page on the ASTM website.

E6 Terminology Relating to Methods of Mechanical Testing

E7 Terminology Relating to Metallography

E1237 Guide for Installing Bonded Resistance Strain Gages

3. Terminology

3.1 Definitions:

3.1.1 Many of the terms used in this test method are defined in Terminology E6 and Terminology E7.

3.2 Definitions of Terms Specific to This Standard:

3.2.1 *interplanar spacing*—the perpendicular distance between adjacent parallel lattice planes.

3.2.2 *macrostress*—an average stress acting over a region of the test specimen containing many crystals.

3.3 Symbols:

3.3.1 α_x = ~~dummy~~ = dummy parameter for $\text{Sum}(\alpha)\text{Sum}(x)$ and $\text{SD}(\alpha)\text{SD}(x)$.

3.3.2 c = ~~ordinate~~ = ordinate intercept of a graph of Δd versus stress.

3.3.3 d = ~~interplanar~~ = interplanar spacing between crystallographic planes; also called *d-spacing*, *d-spacing*.

3.3.4 d_0 = ~~interplanar~~ = interplanar spacing for unstressed material.

3.3.5 Δd = ~~change~~ = change in interplanar spacing caused by stress.

3.3.6 E = ~~modulus~~ = modulus of elasticity.

3.3.7 ν = Poisson's ratio.

3.3.8 EXEC_{eff} = ~~effective~~ = x-ray elastic parameter for X-ray measurements constants for residual stress measurements using x-ray diffraction.

3.3.9 hkl = Miller indices.

3.3.10 $1/2 S_2^{hkl} = (1+\nu)/E$ for an elastically isotropic body.

3.3.11 $S_1^{hkl} = -\nu/E$ for an elastically isotropic body.

3.3.12 i = ~~measurement~~ = measurement index, $1 \leq i \leq n$.

3.3.13 m = ~~slope~~ = slope of a graphplot of Δd versus stress.

3.3.14 n = ~~number~~ = number of measurements used to determine slope m .

3.3.15 $\text{SD}(\alpha)\text{SD}(x)$ = ~~standard~~ = standard deviation of a set of quantities "a", "x".

3.3.16 $\text{Sum}(\alpha)\text{Sum}(x)$ = ~~sum~~ = sum of a set of quantities "a", "x".

3.3.17 $T_i = \bar{X} = X_i$ minus mean of all X_i values.

3.3.18 X_i = ~~i-th~~ = i -th value of applied stress.

3.3.19 Y_i = ~~measurement~~ = measurement of Δd corresponding to X_i .

3.3.16 ν = Poisson's ratio.

3.3.20 ψ = ~~angle~~ = angle between the specimen surface normal and the normal to the diffracting crystallographic planes.

3.3.21 ϕ = the in-plane direction of stress measurement.

3.3.22 ij = in-plane directions of the sample reference frame.

3.3.23 σ_{ij} = calculated stress tensor terms.

3.3.24 $\varepsilon_{\phi\psi}^{hkl}$ = measured lattice strain tensor terms at a given $\phi\psi$ tilt angle.

3.3.25 σ^A = applied stress.

3.3.26 ε_{max} = maximum strain.

3.3.27 δ_{max} = maximum deflection.

3.3.28 h = specimen thickness.

3.3.29 b = width of specimen.

3.3.30 A_x = cross sectional area of specimen.

3.3.31 L = distance between outer rollers on four-point bend fixture.

3.3.32 a = distance between inner and outer rollers on four-point bend fixture.

3.3.33 F = known force applied to specimen.

3.3.34 $\varepsilon_{\phi\psi 0}$ = the intercept value for each applied force necessary for S_j calculation.

4. Theory

4.1 The $\sin^2\psi$ method is widely used to measure stresses in materials using x-ray diffraction techniques. The governing equation can be written as follows:^{3,4}

³ Evenschor P.D., Hauk V. Z., *Metallkunde*, 1975, 66 pp. 167–168.

⁴ Dölle H., *J. Appl. Cryst.*, 1979, 12, pp. 489–501.

$$\varepsilon_{\phi\psi}^{hkl} = \frac{1}{2} S_2^{hkl} (\sigma_{11} \cos^2 \phi + \sigma_{12} \sin 2\phi + \sigma_{22} \sin^2 \phi - \sigma_{33}) \sin^2 \psi + \quad (1)$$

$$\frac{1}{2} S_2^{hkl} \sigma_{33} + S_1^{hkl} (\sigma_{11} + \sigma_{22} + \sigma_{33}) + \frac{1}{2} S_2^{hkl} (\sigma_{13} \cos \phi + \sigma_{23} \sin \phi) \sin 2\psi$$

where:

$\frac{1}{2} S_2^{hkl}$ and S_1^{hkl} = are the XEC.

For a body that is elastically isotropic on the microscopic scale, $\frac{1}{2} S_2^{hkl} = (1 + \nu)/E$ and $S_1^{hkl} = -(\nu/E)$ where E and ν are the modulus of elasticity and Poisson's ratio respectively for the material for all hkl .

4.2 When a uniaxial force is applied along e.g. $\phi = 0$, Eq 1 becomes:

$$\varepsilon_{\phi\psi}^{hkl} = \frac{1}{2} S_2^{hkl} \sigma^A \sin^2 \psi + S_1^{hkl} \sigma^A \quad (2)$$

where:

σ^A = the applied stress due to the uniaxial force.

Therefore:

$$\frac{1}{2} S_2^{hkl} = \frac{\partial^2 \varepsilon_{\phi\psi}^{hkl}}{\partial (\sin^2 \psi) \cdot \partial \sigma^A} \quad (3)$$

S_1^{hkl} is embedded in the intersection term for each applied force increment and is necessary when performing triaxial measurements.

5. Summary of Test Method

5.1 A test specimen is prepared from a material that is representative of that of the object in which residual stress measurements are to be made-performed.

NOTE 1—If a sample of the same material is available it should be used.

5.2 The test specimen is instrumented with an electrical resistance strain gage-gauge, mounted in a location that experiences the same stress as the region that will be subsequently irradiated with X-rays-x-rays.

5.3 The test specimen is calibrated by loading it in such a manner that the stress, where the strain gage-gauge is mounted, is directly calculable, and a calibration curve relating the strain gage-gauge reading to the applied stress is developed.

5.4 The test specimen is mounted in a loading fixture in an X-ray-x-ray diffraction apparatus-instrument and sequentially loaded to several load-force levels.

5.4.1 The change in interplanar spacing is measured for each load-force level and related to the corresponding stress that is determined from the strain gage-gauge reading and the calibration curve.

5.5 The effective XEC elastic parameter and its standard deviation-deviations are calculated from the test results.

6. Significance and Use

6.1 This test method provides standard procedures for experimentally determining the effective XEC elastic parameter for X-ray diffraction-for use in the measurement of residual and applied stresses-stresses using x-ray diffraction techniques. It also provides a standard means of reporting the precision of the parameter-XEC.

6.2 This test method is applicable to any crystalline material which-that exhibits a linear relationship between stress and strain in the elastic range-range, that is, only applicable to elastic loading.

6.3 This test method should be used whenever residual stresses are to be evaluated by an X-ray-x-ray diffraction technique-techniques and the effective XEC elastic parameter-of the material is-are unknown.

7. Apparatus

7.1 Any X-ray-x-ray diffraction instrument intended for measurements-the measurement of residual macrostress that employs measurements of the diffraction peaks that are, ideally and for best accuracy, in the high back-reflection region may be used, including film camera types, diffractometers, and portable systems.

7.2 A loading fixture is required to apply loads-a force to the test specimen while it is being irradiated in the X-ray-x-ray diffraction instrument.

7.2.1 The fixture shall be designed such that the surface stress applied by the fixture shall be uniform over the irradiated area of the specimen.

7.2.2 The fixture shall maintain the irradiated surface of the specimen at the exact center of rotation of the X-ray-x-ray diffraction instrument throughout the test with sufficient precision to provide the desired levels of precision and bias in the measurements to be made-performed.

7.2.3 The fixture may be designed to apply tensile or bending loads.⁵ A four-point bending technique such as that described by Prevey⁵ is most commonly used.

7.3 Electrical resistance strain gages are mounted upon the test specimen to enable it to be accurately stressed to known levels.

8. Test Specimens

8.1 Test specimens should be fabricated from material with microstructure as nearly the same as possible as that in the material in which residual stresses are to be evaluated. It is preferred for superior results to use the same material with a fine grain structure and minimum cold work on the surface to minimize measurement errors.

8.2 For use in tensile or four-point bending fixtures, specimens should be rectangular in shape.

8.2.1 The length of tensile specimens, between grips, shall be not less than four times the width, and the width-to-thickness ratio shall not exceed eight.

8.2.2 For use in four-point bending fixtures, specimens should have a length-to-width ratio of at least four. The specimen width should be sufficient to accommodate strain gages (see 7.58.5) and the width-to-thickness ratio should be greater than one and consistent with the method used to calculate the applied stresses in 8.19.1.

NOTE 2—Nominal dimensions often used for specimens for four-point bending fixtures are 4.0 × 0.75 × 0.06 in. (10.2 × 1.9 × 0.15 cm); 10.2 × 1.9 × 0.15 cm (4.0 × 0.75 × 0.06 in.).

8.3 Tapered specimens for use in cantilever bending fixtures, and split-ring samples, are also acceptable.

8.4 Specimen surfaces may be electropolished or as-rolled sheet or plate.

8.5 One or more electrical resistance strain gages are affixed to the test specimen in accordance with Guide E1237. The gage(s) shall be aligned parallel to the longitudinal axis of the specimen, and should be mounted on a region of the specimen that experiences the same strain as the region that is to be irradiated. The gage(s) should be applied to the irradiated surface of the beam either adjacent to, or on either side of, the irradiated area in order to minimize errors due to the absence of a pure tensile or bending load.

NOTE 3—In the case of four-point bending fixtures the gage(s) should be placed well inside the inner span of the specimen in order to minimize the stress concentration effects associated with the inner knife edges of the fixture.

9. Calibration

9.1 Calibrate the instrumented specimen using loads applied by dead weights or by a testing machine that has been verified according to Practices E4. The Use a loading configuration is such that the applied stresses, that produces statistically determinate applied stresses in the region where the strain gages are mounted and where X-ray diffraction measurements will be made, are statically determinate (that is, performed (that is, such that stresses may be calculated from the applied loads and the dimensions of the specimen and the fixture). In the case of pure bending using a four-point bending apparatus, the strain gauge may be calibrated by measurement of applied strains via deflection of the specimen and calculated using the following equation:

$$\epsilon_{\max} = \frac{\delta_{\max} 12h}{3L^2 - 4a^2} \quad (4)$$

where:

ϵ_{\max} = maximum applied strain to the strain gauge

δ_{\max} = maximum applied deflection

h = specimen thickness

L = distance between outer rollers on four-point bend fixture

a = distance between inner and outer rollers on each side of the four-point bend fixture

If the modulus of elasticity E for the material being tested is known, the applied stress on the specimen may then be calculated using Hooke's law.

$$\sigma^A = E\epsilon_{\max} \quad (5)$$

If the modulus of elasticity E for the material being tested is not known, the applied stress on the specimen may be calculated using known applied forces in the case where bending is being used:

$$\sigma^A = \frac{3Fa}{bh^2} \quad (6)$$

where:

⁵ Prevey, P. S., "A Method of Determining the Elastic Properties of Alloys in Selected Crystallographic Directions for X-Ray Diffraction Residual Stress Measurement," *Advances in X-Ray Analysis* 20, 1977, pp. 345–354.