



Standard Terminology Relating to Quality and Statistics¹

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1. Scope

1.1 This standard is the general terminology standard for terms defined in the standards of Committee E11 on Quality and Statistics.

1.2 A term in this standard which lists an attribution to an E11 technical standard indicates that the standard is normative for that term. Any changes in the term definition in the normative standard will be editorially changed in this standard. Any terms added to an E11 standard will be editorially added to this standard with an attribution to that standard.

1.3 Term definitions that are similar to ISO 3534 will be noted in this standard, but ISO 3534 will not be considered normative for any E11 terms.

2. Referenced Documents

2.1 *ASTM E11 Standards with Terms in This Standard:*²

E29 Practice for Using Significant Digits in Test Data to Determine Conformance with Specifications

E105 Practice for Probability Sampling of Materials

E141 Practice for Acceptance of Evidence Based on the Results of Probability Sampling

E177 Practice for Use of the Terms Precision and Bias in ASTM Test Methods

E178 Practice for Dealing With Outlying Observations

E691 Practice for Conducting an Interlaboratory Study to Determine the Precision of a Test Method

E1169 Practice for Conducting Ruggedness Tests

E1325 Terminology Relating to Design of Experiments

E1402 Guide for Sampling Design

E1488 Guide for Statistical Procedures to Use in Developing and Applying Test Methods

E1994 Practice for Use of Process Oriented AOQL and LTPD Sampling Plans

E2234 Practice for Sampling a Stream of Product by Attributes Indexed by AQL

E2281 Practice for Process and Measurement Capability Indices

E2282 Guide for Defining the Test Result of a Test Method

E2334 Practice for Setting an Upper Confidence Bound For a Fraction or Number of Non-Conforming items, or a Rate of Occurrence for Non-conformities, Using Attribute Data, When There is a Zero Response in the Sample

E2489 Practice for Statistical Analysis of One-Sample and Two-Sample Interlaboratory Proficiency Testing Programs

E2554 Practice for Estimating and Monitoring the Uncertainty of Test Results of a Test Method Using Control Chart Techniques

E2555 Practice for Factors and Procedures for Applying the MIL-STD-105 Plans in Life and Reliability Inspection

E2586 Practice for Calculating and Using Basic Statistics

E2587 Practice for Use of Control Charts in Statistical Process Control

E2655 Guide for Reporting Uncertainty of Test Results and Use of the Term Measurement Uncertainty in ASTM Test Methods

E2696 Practice for Life and Reliability Testing Based on the Exponential Distribution

E2709 Practice for Demonstrating Capability to Comply with an Acceptance Procedure

E2782 Guide for Measurement Systems Analysis (MSA)

E2819 Practice for Single- and Multi-Level Continuous Sampling of a Stream of Product by Attributes Indexed by AQL

¹ This terminology is under the jurisdiction of ASTM Committee E11 on Quality and Statistics and is the direct responsibility of Subcommittee E11.70 on Editorial/Terminology.

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² For referenced ASTM standards, visit the ASTM website, www.astm.org, or contact ASTM Customer Service at service@astm.org. For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

E2935 Practice for Conducting Equivalence Testing in Laboratory Applications

2.2 *ISO Standards*.³

ISO 3534 Statistics-Vocabulary and Symbols Part 2 Applied Statistics

3. Terminology

acceptance quality limit (AQL), n —quality limit that is the worst tolerable process average when a continuing series of lots is submitted for acceptance sampling. **E2234**

accepted reference value, n —a value that serves as an agreed-upon reference for comparison, and which is derived as: (1) a theoretical or established value, based on scientific principles, (2) an assigned or certified value, based on experimental work of some national or international organization, or (3) a consensus or certified value, based on collaborative experimental work under the auspices of a scientific or engineering group. **E177**

accuracy, n —the closeness of agreement between a test result and an accepted reference value. **E177**

aliases, n —in a fractional factorial design, two or more effects which are estimated by the same contrast and which, therefore, cannot be estimated separately. **E1325**

area sampling, n —probability sampling in which a map, rather than a tabulation of sampling units, serves as the sampling frame. **E1402**

assignable cause, n —factor that contributes to variation in a process or product output that is feasible to detect and identify (see **special cause**). **E2587**

attributes data, n —observed values or test results that indicate the presence or absence of specific characteristics or counts of occurrences of events in time or space. **E2587**

attributes, method of, n —measurement of quality by the method of attributes consists of noting the presence (or absence) of some characteristic or attribute in each of the units in the group under consideration, and counting how many units do (or do not) possess the quality attribute, or how many such events occur in the unit, group, or area. **E2334**

audit subsample, n —a small subsample of a sample selected for review of all sample selection and data collection procedures. **E141**

average outgoing quality (AOQ), n —the average percent defective of outgoing product including all accepted lots or batches, after any defective units found in them are replaced by acceptable units, plus all lots or batches which are not accepted after such lots or batches have been effectively 100 % inspected and all defective units replaced by acceptable units. **E1994**

average outgoing quality limit (AOQL), n —the maximum of the AOQs for all possible incoming percentages defective for the process, for a given acceptance sampling plan. **E1994**

average quality protection, n —a type of protection in which there is prescribed some chosen value of average percent defective in the product after inspection (average outgoing quality limit (AOQL), that shall not be exceeded in the long run no matter what may be the level of percent defective in the product submitted to the inspector. **E1994**

average run length (ARL), n —the average number of times that a process will have been sampled and evaluated before a shift in process level is signaled. **E2587**

average standard deviation, \bar{s} , n —arithmetic average of sample standard deviations. **E2281**

balanced incomplete block design (BIB), n —an incomplete block design in which each block contains the same number k of different versions from the t versions of a single principal factor arranged so that every pair of versions occurs together in the same number, λ , of blocks from the b blocks. **E1325**

bias, n —the difference between the expectation of the test results and an accepted reference value. **E177**

binary scale, n —nominal scale with only two possible categories. **E2282**

bulk sampling, n —sampling to prepare a portion of a mass of material that is representative of the whole. **E1402**

c chart, n —control chart that monitors the count of occurrences of an event in a defined increment of time or space. **E2587**

calibration, n —process of establishing a relationship between a measurement device and a known standard value(s). **E2782**

center line, n —line on a control chart depicting the average level of the statistic being monitored. **E2587**

chance cause, n —source of inherent random variation in a process which is predictable within statistical limits (see **common cause**). **E2587**

characteristic, n —a property of items in a sample or population which, when measured, counted or otherwise observed, helps to distinguish among the items. **E2282**

check sample, n —see **control sample**. **E2554**

classification of defects, n —the enumeration of possible defects of the unit of product arranged according to their seriousness, that is, critical, major, or minor defect. **E2234**

cluster sampling, n —sampling in which the sampling unit consists of a group of subunits, all of which are measured for sampled clusters. **E1402**

coefficient of determination, n —square of the correlation coefficient, r . **E2586**

³ Available from International Organization for Standardization (ISO), 1, ch. de la Voie-Creuse, CP 56, CH-1211 Geneva 20, Switzerland, <http://www.iso.org>.

coefficient of variation (CV), *n*—for a nonnegative characteristic, the ratio of the standard deviation to the mean for a population or sample. **E2586**

collaborative study, *n*—interlaboratory study in which each laboratory uses the defined method of analysis to analyze identical portions of homogeneous materials to assess the performance characteristics obtained for that method of analysis. **E2489**

collaborative trial, *n*—see **collaborative study**. **E2489**

common cause, *n*—see **chance cause**. **E2587**

component of variance, *n*—a part of a total variance identified with a specified source of variability. **E1488**

completely randomized design, *n*—a design in which the treatments are assigned at random to the full set of experimental units. **E1325**

completely randomized factorial design, *n*—a factorial experiment (including all replications) run in a completely randomized design. **E1325**

composite design, *n*—a design developed specifically for fitting second order response surfaces to study curvature, constructed by adding further selected treatments to those obtained from a 2ⁿ factorial (or its fraction). **E1325**

confidence bound, *n*—see **confidence limit**. **E2586**

confidence coefficient, *n*—see **confidence level**. **E2586**

confidence interval, *n*—an interval estimate [L, U] with the statistics L and U as limits for the parameter θ and with confidence level 1- α , where $\Pr(L \leq \theta \leq U) \geq 1 - \alpha$. **E2586**

confidence level, *n*—the value, 1- α , of the probability associated with a confidence interval, often expressed as a percentage. **E2586**

confidence limit, *n*—each of the limits, L and U, of a confidence interval, or the limit of a one-sided confidence interval. **E2586**

confounded factorial design, *n*—a factorial experiment in which only a fraction of the treatment combinations are run in each block and where the selection of the treatment combinations assigned to each block is arranged so that one or more prescribed effects is (are) confounded with the block effect(s), while the other effects remain free from confounding. **E1325**

confounding, *n*—combining indistinguishably the main effect of a factor or a differential effect between factors (interactions) with the effect of other factor(s), block factor(s) or interactions(s). **E1325**

consumer's risk, *n*—probability that a lot having specified rejectable quality level will be accepted under a defined sampling plan. **E2555**

continuous sampling inspection, *n*—a method of sampling a stream of product in order of production where the sampling

frequency is adjusted based on ongoing inspection results. **E2819**

contrast, *n*—a linear function of the observations for which the sum of the coefficients is zero. **E1325**

contrast analysis, *n*—a technique for estimating the parameters of a model and making hypothesis tests on preselected linear combinations of the treatments (contrasts). **E1325**

control chart, *n*—chart on which are plotted a statistical measure of a subgroup versus time of sampling along with limits based on the statistical distribution of that measure so as to indicate how much common, or chance, cause variation is inherent in the process or product. **E2587**

control chart factor, *n*—a tabulated constant, depending on sample size, used to convert specified statistics or parameters into a central line value or control limit appropriate to the control chart. **E2587**

control limits, *n*—limits on a control chart that are used as criteria for signaling the need for action or judging whether a set of data does or does not indicate a state of statistical control based on a prescribed degree of risk. **E2587**

control sample, *n*—sample taken from a stable, homogeneous material for the purposes of monitoring the performance of a test method in a laboratory. **E2554**

correlation coefficient, *n*—for a population, ρ , a dimensionless measure of association between two variables X and Y, equal to the covariance divided by the product of σ_X and σ_Y . **E2586**

correlation coefficient, *n*—for a sample, *r*, the quantity: **E2586**

$$\frac{\sum(x - \bar{x})(y - \bar{y})}{(n - 1)s_x s_y} \quad (1)$$

covariance, *n*—of a population, $\text{cov}(X, Y)$, for two variables, X and Y, the expected value of $(X - \mu_X)(Y - \mu_Y)$. **E2586**

covariance, *n*—of a sample, the quantity: **E2586**

$$\frac{\sum(x - \bar{x})(y - \bar{y})}{(n - 1)} \quad (2)$$

critical defect, *n*—a defect that judgment and experience indicate would result in hazardous or unsafe conditions for individuals using, maintaining, or depending upon the product, or a defect that judgment and experience indicate is likely to prevent performance of the function of a major end item. **E2234**

defect, *n*—any nonconformance of the unit of product with specified requirements. **E2234**

degrees of freedom, *n*—the number of independent data points minus the number of parameters that have to be estimated before calculating the variance. **E2586**

dependent variable, *n*—a variable to be predicted using an equation. **E2586**

- design of experiments, *n***—the arrangement in which an experimental program is to be conducted, and the selection of the levels (versions) of one or more factors or factor combinations to be included in the experiment. Synonyms include *experiment design* and **experimental design**. **E1325**
- double sampling plan, *n***—a multiple sampling plan in which up to two samplings can be taken and evaluated to accept or reject a lot. **E2234**
- empirical percentile, *n***—estimate of a population percentile using the sample data. This is a sample value such that a percentage *p* of the sample is less than that value. **E2586**
- equal complete coverage result, *n***—the numerical characteristic of interest calculated from observations made by drawing randomly from the frame, all of the sampling units covered by the frame. **E141**
- equivalence, *n***—similarity between two population parameters within predetermined limits. **E2935**
- error of result, *n***—a test result minus the accepted reference value of the characteristic. **E2655**
- estimate, *n***—sample statistic used to approximate a population parameter. **E2586**
- evolutionary operation (EVOP), *n***—a sequential form of experimentation conducted in production facilities during regular production. **E1325**
- EWMA chart, *n***—control chart that monitors the exponentially weighted moving averages of consecutive subgroups. **E2587**
- EWMV chart, *n***—control chart that monitors the exponentially weighted moving variance. **E2587**
- expanded uncertainty, *U, n***—uncertainty reported as a multiple of the standard uncertainty. **E2655**
- experimental design, *n***—see **design of experiments**. **E1325**
- experimental unit, *n***—a portion of the experiment space to which a treatment is applied or assigned in the experiment. **E1325**
- experiment space, *n***—the materials, equipment, environmental conditions and so forth that are available for conducting an experiment. **E1325**
- exponentially weighted moving average (EWMA), *n***—weighted average of time-ordered data where the weights of past observations decrease geometrically with age. **E2587**
- exponentially weighted moving variance (EWMV), *n***—weighted average of squared deviations of observations from their current estimate of the process average for time ordered observations, where the weights of past squared deviations decrease geometrically with age. **E2587**
- DISCUSSION—The estimate of the process average used for the current deviation comes from a coupled EWMA chart monitoring the same process characteristic. This estimate is the EWMA from the previous time period, which is the forecast of the process average for the current time period.
- factorial experiment (general), *n***—in general, an experiment in which all possible treatments formed from two or more factors, each being studied at two or more levels (versions) are examined so that interactions (differential effects) as well as main effects can be estimated. **E1325**
- 2ⁿ factorial experiment, *n***—a factorial experiment in which *n* factors are studied, each of them in two levels (versions). **E1325**
- fractional factorial design, *n***—a factorial experiment in which only an adequately chosen fraction of the treatments required for the complete factorial experiment is selected to be run. **E1325**
- frame, *n***—a list, compiled for sampling purposes, which designates all of the sampling units (items or groups) of a population or universe to be considered in a specific study. **E1402**
- fully nested experiment, *n***—a nested experiment in which the second factor is nested within levels (versions) of the first factor and each succeeding factor is nested within versions of the previous factor. **E1325**
- gage, *n***—device used as part of the measurement process to obtain a measurement result. **E2782**
- hierarchical experiment, *n***—see **nested experiment**. **E1325**
- histogram, *n***—graphical representation of the frequency distribution of a characteristic consisting of a set of rectangles with area proportional to the frequency. **ISO 3534-1, E2586**
- I chart, *n***—control chart that monitors the individual subgroup observations. **E2587**
- incomplete block design, *n***—a design in which the experiment space is subdivided into blocks in which there are insufficient experimental units available to run a complete set of treatments or replicate of the experiment. **E1325**
- independent variable, *n***—a variable used to predict another using an equation. **E2586**
- inspection, *n***—the process of measuring, examining, testing, or otherwise comparing the unit of product with the requirements. **E2234**
- inspection by attributes, *n***—inspection whereby either the unit of product is classified simply as defective or non-defective, or the number of defects in the unit of product is counted, with respect to a given requirement or set of requirements. **E2234**
- inspection lot, *n***—a collection of units of product produced under conditions that are considered uniform and from which a sample is drawn and inspected. **E2234**
- interlaboratory comparison, *n***—organization, performance, and evaluation of tests on the same or similar test items by two or more laboratories in accordance with predetermined conditions. **E2489**
- interlaboratory study (ILS), *n***—a designed procedure for obtaining a precision statement for a test method, involving

- multiple laboratories, each generating replicate test results on one or more materials. **E691**
- intermediate precision**, n —the closeness of agreement between test results obtained under specified intermediate precision conditions. **E177**
- intermediate precision conditions**, n —conditions under which test results are obtained with the same test method using test units or test specimens (see Practice **E691**, 10.3) taken at random from a single quantity of material that is as nearly homogeneous as possible, and with changing conditions such as operator, measuring equipment, location within the laboratory, and time. **E177**
- interquartile range (IQR)**, n —the 75th percentile (0.75 quantile) minus the 25th percentile (0.25 quantile), for a data set. **E2586**
- interval scale**, n —continuous scale or discrete scale with equal sized scale values and an arbitrary zero. **ISO 3534-2**, **E2282**
- judgment sampling**, n —a procedure whereby enumerators select a few items of the population, based on visual, positional or other cues that are believed to be related to the variable of interest, so that the selected items appear to match the population. **E105**
- kurtosis**, γ_2 , g_2 , n —for a population or a sample, a measure of the weight of the tails of a distribution relative to the center, calculated as the ratio of the fourth central moment (empirical if a sample, theoretical if a population applies) to the standard deviation (sample, s , or population, σ) raised to the fourth power, minus 3 (also referred to as excess kurtosis). **E2586**
- level (of a factor)**, n —a given value, a specification of procedure or a specific setting of a factor. **E1325**
- life test**, n —process of placing one or more units of product under a specified set of test conditions and measuring the time until failure for each unit. **E2696**
- limiting quality level (LQL)**, n —quality level having a specified consumer's risk for a given sampling plan. **E2555**
- long term standard deviation**, σ_{LT} , n —sample standard deviation of all individual (observed) values taken over a long period of time. **E2281**
- lot**, n —a definite quantity of a product or material accumulated under conditions that are considered uniform for sampling purposes. **E2555**
- lot quality protection**, n —a type of protection in which there is prescribed some chosen value of limiting percent defective in a lot (lot tolerance percent defective (LTPD)) and also some chosen value for the probability (called the consumer's risk) of accepting a submitted lot that has a percent defective equal to the lot tolerance percent defective. **E1994**
- lot tolerance percent defective (LTPD)**, n —for purposes of acceptance sampling, the percentage of defective units in a lot for which the consumer has a stated low probability of acceptance of the lot. **E1994**
- lower control limit (LCL)**, n —minimum value of the control chart statistic that indicates statistical control. **E2587**
- lower process capability index**, C_{pkl} , n —index describing process capability in relation to the lower specification limit. **E2281**
- lower process performance index**, P_{pkl} , n —index describing process performance in relation to the lower specification limit. **E2281**
- main effect, average effect**, n —a term describing a measure for the comparison of the responses at each level (version) of a factor averaged over all levels (versions) of other factors in the experiment. **E1325**
- major defect**, n —a defect, other than critical, that is likely to result in failure, or to reduce materially the usability of the unit of product for its intended purpose. **E2234**
- mean**, n —of a population, μ , average or expected value of a characteristic in a population – of a sample, \bar{x} , sum of the observed values in the sample divided by the sample size. **E2586**
- mean time to failure, θ** , n —in life testing, the average length of life of items in a lot. **E2696**
- measurement process**, n —process used to assign a number to a property of an object or other physical entity. **E2782**
- measurement result**, n —number assigned to a property of an object or other physical entity being measured. **E2782**
- measurement system**, n —the collection of hardware, software, procedures and methods, human effort, environmental conditions, associated devices, and the objects that are measured for the purpose of producing a measurement. **E2782**
- measurement systems analysis (MSA)**, n —any of a number of specialized methods useful for studying a measurement system and its properties. **E2782**
- median**, \tilde{x} , n —the 50th percentile in a population or sample. **E2586**
- method of least squares**, n —a technique of estimation of a parameter which minimizes $\sum e^2$, where e is the difference between the observed value and the predicted value derived from the assumed model. **E1325**
- midrange**, n —average of the minimum and maximum values in a sample. **E2586**
- minimum process capability index**, C_{pk} , n —smaller of the upper process capability index and the lower process capability index. **E2281**
- minimum process performance index**, P_{pk} , n —smaller of the upper process performance index and the lower process performance index. **E2281**
- minor defect**, n —a defect that is not likely to reduce materially the usability of the unit of product for its intended purpose,

- or is a departure from established standards having little bearing on the effective use or operation of the unit. **E2234**
- mixture design**, *n*—a design in which two or more ingredients or components shall be mixed and the response is a property of the resulting mixture that does not depend upon the amount of the mixture. **E1325**
- MR chart**, *n*—control chart that monitors the moving range of consecutive individual subgroup observations. **E2586**
- multiple sampling plan**, *n*—a sampling plan in which successive samples from a lot are drawn and after each sample is inspected a decision is made to accept the lot, reject the lot, or to take another sample, based on quality level of the combined samples. **E2234**
- multiple stage acceptance procedure**, *n*—a procedure that involves more than one stage of sampling and testing a given quality characteristic and one or more acceptance criteria per stage. **E2709**
- multi-stage sampling**, *n*—sampling in which the sample is selected by stages, the sampling units at each stage being selected from subunits of the larger sampling units chosen at the previous stage. **E1402**
- nested experiment**, *n*—an experiment to examine the effect of two or more factors in which the same level (version) of a factor cannot be used with all levels (versions) of other factors. Synonym **hierarchical experiment**. **E1325**
- nested sampling**, *n*—same as **multi-stage sampling**. **E1402**
- nominal scale**, *n*—scale with unordered labeled categories or ordered by convention. **ISO 3534-2, E2282**
- non-conforming item**, *n*—an item containing at least one non-conformity. **E2334**
- number of failures**, *n*—number of failures that have occurred at the time the decision as to lot acceptability is reached. **E2696**
- observation**, *n*—the process of obtaining information regarding the presence or absence of an attribute of a test specimen, or of making a reading on a characteristic or dimension of a test specimen. **E2282**
- observed value**, *n*—the value obtained by making an observation. **E2282**
- operating characteristic**, *n*—probability of acceptance using a specified acceptance sampling plan, as a function of parameters describing quality of the lot. **E2234**
- order statistic** $x_{(k)}$, *n*—value of the k^{th} observed value in a sample after sorting by order of magnitude. **E2586**
- ordinal scale**, *n*—scale with ordered labeled categories. **ISO 3534-2, E2282**
- orthogonal array**, *n*—a table of coefficients identifying the levels, or some weight associated with the levels, for each factor to be used in the analysis of specified effects, which are arranged in such a manner that each effect will be independent of the other effects. **E1325**
- orthogonal contrasts**, *n*—two contrasts are orthogonal if the contrast coefficients of the two sets satisfy the condition that, when multiplied in corresponding pairs, the sum of the products is equal to zero. See **contrast** and **contrast analysis**. **E1325**
- outlier**—see **outlying observation**. **E178**
- outlying observation**, *n*—an observation that appears to deviate markedly in value from other members of the sample in which it appears. **E178**
- p chart**, *n*—control chart that monitors the fraction of occurrences of an event. **E2587**
- parameter**, *n*—see **population parameter**. **E2586**
- partially balanced incomplete block design (PBIB)**, *n*—an incomplete block design in which each block contains the same number *k*, of different versions from the *t* versions of the principal factor. **E1325**
- partially nested experiment**, *n*—a nested experiment in which several factors may be crossed as in factorial experiments and other factors nested within the crossed combinations. **E1325**
- percentile**, *n*—quantile of a sample or a population, for which the fraction less than or equal to the value is expressed as a percentage. **E2586**
- Plackett-Burman designs**, *n*—a set of screening designs using orthogonal arrays that permit evaluation of the linear effects of up to $n = t - 1$ factors in a study of *t*, treatment combinations. **E1325**
- population**, *n*—the totality of items or units of material under consideration. **E2586**
- population parameter**, *n*—summary measure of the values of some characteristic of a population. **ISO 3534 Part 2, E2586**
- precision**, *n*—the closeness of agreement between independent test results obtained under stipulated conditions. **E177**
- prediction interval**, *n*—an interval for a future value or set of values, constructed from a current set of data, in a way that has a specified probability for the inclusion of the future value. **E2586**
- primary sampling unit (psu)**, *n*—the item, element, increment, segment or cluster selected at the first stage of the selection procedure from a population or universe. **E1402**
- probability proportional to size sampling (pps)**, *n*—probability sampling in which the probabilities of selection of sampling units are proportional, or nearly proportional, to a quantity (the “size”) that is known for all sampling units. **E1402**
- probability sample**, *n*—a sample in which the sampling units are selected by a chance process such that a specified