



Designation: C1043 – 16

# Standard Practice for Guarded-Hot-Plate Design Using Circular Line-Heat Sources<sup>1</sup>

This standard is issued under the fixed designation C1043; the number immediately following the designation indicates the year of original adoption or, in the case of revision, the year of last revision. A number in parentheses indicates the year of last reapproval. A superscript epsilon ( $\epsilon$ ) indicates an editorial change since the last revision or reapproval.

## 1. Scope

1.1 This practice covers the design of a circular line-heat-source guarded hot plate for use in accordance with Test Method C177.

NOTE 1—Test Method C177 describes the guarded-hot-plate apparatus and the application of such equipment for determining thermal transmission properties of flat-slab specimens. In principle, the test method includes apparatus designed with guarded hot plates having either distributed- or line-heat sources.

1.2 The guarded hot plate with circular line-heat sources is a design in which the meter and guard plates are circular plates having a relatively small number of heaters, each embedded along a circular path at a fixed radius. In operation, the heat from each line-heat source flows radially into the plate and is transmitted axially through the test specimens.

1.3 The meter and guard plates are fabricated from a continuous piece of thermally conductive material. The plates are made sufficiently thick that, for typical specimen thermal conductances, the radial and axial temperature variations in the guarded hot plate are quite small. By proper location of the line-heat source(s), the temperature at the edge of the meter plate is made equal to the mean temperature of the meter plate, thus facilitating temperature measurements and thermal guarding.

1.4 The line-heat-source guarded hot plate has been used successfully over a mean temperature range from  $-10$  to  $+65^{\circ}\text{C}$ , with circular metal plates and a single line-heat source in the meter plate. The chronological development of the design of circular line-heat-source guarded hot plates is given in Refs (1-9).<sup>2</sup>

1.5 This practice does not preclude (1) lower or higher temperatures; (2) plate geometries other than circular; (3) line-heat-source geometries other than circular; (4) the use of

plates fabricated from ceramics, composites, or other materials; or (5) the use of multiple line-heat sources in both the meter and guard plates.

1.6 The values stated in SI units are to be regarded as standard. No other units of measurement are included in this standard.

1.7 *This standard does not purport to address all of the safety concerns, if any, associated with its use. It is the responsibility of the user of this standard to establish appropriate safety and health practices and determine the applicability of regulatory limitations prior to use.*

## 2. Referenced Documents

2.1 *ASTM Standards:*<sup>3</sup>

- C168 Terminology Relating to Thermal Insulation
- C177 Test Method for Steady-State Heat Flux Measurements and Thermal Transmission Properties by Means of the Guarded-Hot-Plate Apparatus
- C1044 Practice for Using a Guarded-Hot-Plate Apparatus or Thin-Heater Apparatus in the Single-Sided Mode
- E230 Specification and Temperature-Electromotive Force (EMF) Tables for Standardized Thermocouples<sup>6</sup>

2.2 *ASTM Adjuncts:*

- Line-Heat-Source Guarded-Hot-Plate Apparatus<sup>4</sup>

## 3. Terminology

3.1 *Definitions*—For definitions of terms and symbols used in this practice, refer to Terminology C168. For definitions of terms relating to the guarded-hot-plate apparatus refer to Test Method C177.

3.2 *Definitions of Terms Specific to This Standard:*

3.2.1 *gap, n*—a separation between the meter plate and guard plate, usually filled with a gas or thermal insulation.

3.2.2 *guard plate, n*—the outer ring of the guarded hot plate that encompasses the meter plate and promotes one-dimensional heat flow normal to the meter plate.

<sup>1</sup> This practice is under the jurisdiction of ASTM Committee C16 on Thermal Insulation and is the direct responsibility of Subcommittee C16.30 on Thermal Measurement.

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<sup>2</sup> The boldface numbers in parentheses refer to a list of references at the end of this practice.

<sup>3</sup> For referenced ASTM standards, visit the ASTM website, [www.astm.org](http://www.astm.org), or contact ASTM Customer Service at [service@astm.org](mailto:service@astm.org). For *Annual Book of ASTM Standards* volume information, refer to the standard's Document Summary page on the ASTM website.

<sup>4</sup> Available from ASTM Headquarters. Order Adjunct: ADJC1043.

3.2.3 *guarded hot plate, n*—an assembly, consisting of a meter plate and a co-planar, concentric guard plate that provides the heat input to the specimens.

3.2.4 *line-heat-source, n*—a thin or fine electrical heating element that provides uniform heat generation per unit length.

3.2.5 *meter area, n*—the mathematical area through which the heat input to the meter plate flows normally under ideal guarding conditions into the meter section of the specimen.

3.2.6 *meter plate, n*—the inner disk of the guarded hot plate that contains one or more line-heat sources embedded in a circular profile and provides the heat input to the meter section of the specimens.

3.2.7 *meter section, n*—the portion of the test specimen through which the heat input to the meter plate flows under ideal guarding conditions.

#### 4. Significance and Use

4.1 This practice describes the design of a guarded hot plate with circular line-heat sources and provides guidance in determining the mean temperature of the meter plate. It provides information and calculation procedures for: (1) control of edge heat loss or gain (Annex A1); (2) location and installation of line-heat sources (Annex A2); (3) design of the gap between the meter and guard plates (Appendix X1); and (4) location of heater leads for the meter plate (Appendix X2).

4.2 A circular guarded hot plate with one or more line-heat sources is amenable to mathematical analysis so that the mean surface temperature is calculated from the measured power input and the measured temperature(s) at one or more known locations. Further, a circular plate geometry simplifies the mathematical analysis of errors resulting from heat gains or losses at the edges of the specimens (see Refs (10, 11)).

4.3 The line-heat source(s) is (are) placed in the meter plate at a prescribed radius such that the temperature at the outer edge of the meter plate is equal to the mean surface tempera-

ture over the meter area. Thus, the determination of the mean temperature of the meter plate is accomplished with a small number of temperature sensors placed near the gap.

4.4 A guarded hot plate with one or more line-heat sources will have a radial temperature variation, with the maximum temperature differences being quite small compared to the average temperature drop across the specimens. Provided guarding is adequate, only the mean surface temperature of the meter plate enters into calculations of thermal transmission properties.

4.5 Care shall be taken to design a circular line-heat-source guarded hot plate so that the electric-current leads to each heater either do not significantly alter the temperature distributions in the meter and guard plates or else affect these temperature distributions in a known way so that appropriate corrections are applied.

4.6 The use of one or a few circular line-heat sources in a guarded hot plate simplifies construction and repair. For room-temperature operation, the plates are typically of one-piece metal construction and thus are easily fabricated to the required thickness and flatness. The design of the gap is also simplified, relative to gap designs for distributed-heat-source hot plates.

4.7 In the single-sided mode of operation (see Practice C1044), the symmetry of the line-heat-source design in the axial direction minimizes errors due to undesired heat flow across the gap.

#### 5. Design of a Guarded Hot Plate with Circular Line-Heat Source(s)

5.1 *General*—The general features of a circular guarded-hot-plate apparatus with line-heat sources are illustrated in Fig. 1. For the double-sided mode of operation, there are two specimens, two cold plates, and a guarded hot plate with a gap

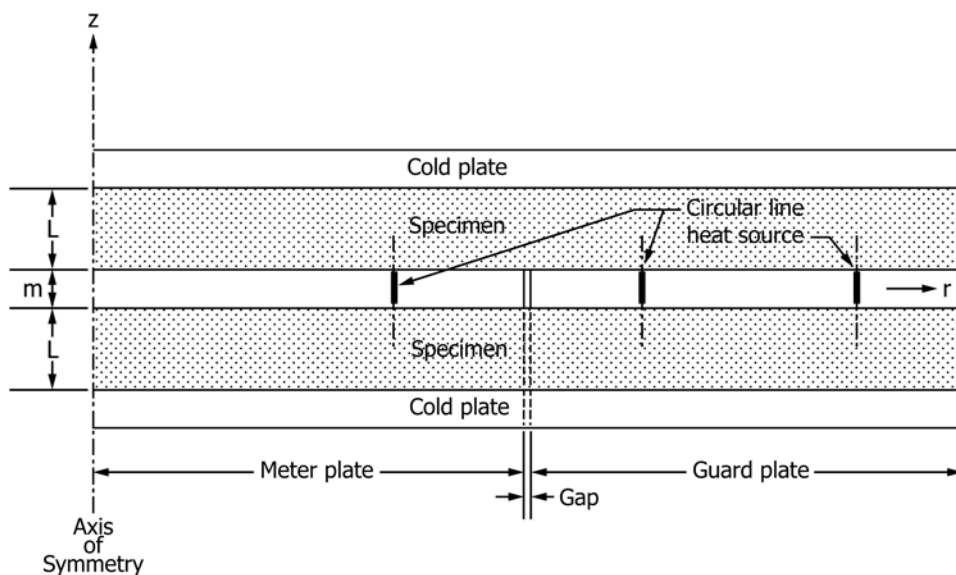


FIG. 1 Schematic of a Line-Heat-Source Guarded-Hot-Plate Apparatus

between the meter and guard plates. The meter and guard plates are each provided with one (or a few) circular line-heat sources.

**5.2 Summary**—To design the meter and guard plates, use the following suggested procedure: (1) establish the specifications and priorities for the design criteria; (2) select an appropriate material for the plates; (3) determine the dimensions of the plates; (4) determine the type, number, and location of the line-heat source(s); (5) design the support system for the plates; and (6) determine the type, number, and location of the temperature sensors.

**5.3 Design Criteria**—Establish specifications for the following parameters of the guarded hot-plate apparatus: (1) specimen diameter; (2) range of specimen thicknesses; (3) range of specimen thermal conductances; (4) characteristics of specimen materials (for example, stiffness, mechanical compliance, density, hardness); (5) range of hot-side and cold-side test temperatures; (6) orientation of apparatus (vertical or horizontal heat flow); and (7) required measurement precision.

**NOTE 2**—The priority assigned to the design parameters depends on the application. For example, an apparatus for high-temperature will necessitate a different precision specification than that for a room-temperature apparatus. Technical data and design drawings for two line-heat-source guarded-hot-plate apparatus are available in the adjunct.<sup>4</sup>

**5.4 Material**—Select the material for the guarded hot plate by considering the following criteria:

**5.4.1 Ease of Fabrication**—Fabricate the guarded hot plate from a material that has suitable thermal and mechanical properties and which is readily fabricated to the desired shapes and tolerances, as well as facilitate assembly.

**5.4.2 Thermal Stability**—For the intended range of temperature, select a material for the guarded hot plate that is dimensionally stable, resistant to oxidation, and capable of supporting its own weight, the test specimens, and accommodating the applied clamping forces without significant distortion. The coefficient of thermal expansion shall be known in order to calculate the meter area at different temperatures.

**5.4.3 Thermal Conductivity**—To reduce the (small) radial temperature variations across the guarded hot plate, select a material having a high thermal conductivity. For cryogenic or modest temperatures, select a metal such as copper, aluminum, silver, gold or nickel. For high-temperature (up to 600 or 700°C) use in air, select nickel or a single-compound ceramic, such as aluminum oxide, aluminum nitride, or cubic boron nitride.

**5.4.4 Heat Capacity**—To achieve thermal equilibrium quickly, select a material having a low volumetric heat capacity (product of density and specific heat). Although aluminum, silver, and gold, for example, have volumetric heat capacities lower than copper, as a practical matter, either copper or aluminum is satisfactory.

**5.4.5 Emittance**—To achieve a uniform, high emittance, select a plate material that will accept a suitable surface treatment. The treatment shall also provide good oxidation resistance. For modest temperatures, various high emittance paints are used for copper, silver, gold, or nickel. For aluminum, a black anodized treatment provides a uniformly high emittance. For high-temperature, most ceramics have an

inherently high emittance. Nickel and its alloys form a fairly stable oxide coating at high temperatures.

**5.5 Guarded-Hot-Plate Dimensions**—Select the geometrical dimensions of the guarded hot plate to provide an accurate determination of the thermal transmission properties.

**NOTE 3**—The accurate determination of thermal transmission properties requires that the heat input to the meter plate flows normally through the specimens to the cold plates. One-dimensional heat flow is attained by proper selection of the diameter of the meter plate relative to the diameter of the guard plate while also considering (1) the specimen thermal conductivities; (2) specimen thicknesses; (3) edge insulation; and, (4) secondary guarding, if any.

**5.5.1 Meter Plate and Guard Plate Diameters**—Use **Annex A1** to determine either the diameter of the guard plate for a given meter plate diameter, or the diameter of the meter plate for a given guard plate diameter. Specifically, determine the combinations of diameters of the meter plate and guard plate that will be required so that the edge-heat-loss error will not be excessive for the thickest specimens, with the highest lateral thermal conductances. If necessary, calculate the edge heat loss for different edge insulation and secondary-guarding conditions.

**NOTE 4**—For example, when testing relatively thin specimens of insulation, maintain the ambient temperature at essentially the mean temperature of the specimens and to use minimal edge insulation without secondary guarding. However, for thicker conductive specimens, edge insulation and secondary guarding are necessary to achieve the desired test accuracy.

**5.5.2 Guarded-Hot-Plate Thickness**—The plate thickness shall provide proper structural rigidity, and have a large lateral thermal conductance, thus minimizing radial temperature variations in the plate. A large thickness, however, will increase the heat capacitance of the plate and thus adversely affect the (rapid) achievement of thermal equilibrium, and reduce the thermal isolation between the meter plate and the guard plate.

**5.5.3 Gap Width**—The gap shall have a uniform width such that the gap area, in the plane of the surface of the guarded hot plate, shall be less than 3 % of the meter area. In any case, the width of the gap shall not exceed the limitations given in Test Method **C177**. The width of the gap is a compromise between increasing the separation in order to reduce lateral heat flow and distorting the heat flow into the specimen and increasing the uncertainty in the determination of the meter area.

**NOTE 5**—The gap provides a significant thermal resistance between the meter and guard plates. The temperature difference across the gap shall be maintained at a very small value, thereby minimizing the heat transfer between the meter and guard plates, both directly across the gap and also through adjacent portions of the specimens.

**5.5.4 Gap Configuration**—Refer to **Fig. 2** in selecting an appropriate design for the gap cross-section. Designs (b) and (c) permit a narrow gap at the surfaces, in the plane of the plate, while maintaining a fairly high thermal resistance between the meter and guard plates. For a small temperature difference across the gap, calculate the corresponding heat flow using guidelines in **Appendix X1**.

**5.5.5 Plate Flatness:**

**5.5.5.1** When assembled, the guarded hot plate shall have the surfaces of both the meter and guard plates flat to within 0.025 % of the outer diameter of the guard plate.

## Gap Configurations

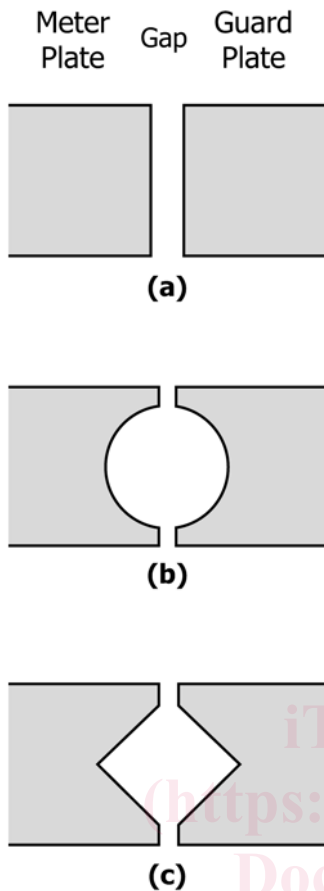


FIG. 2 Designs for the Cross-section of the Gap Between the Meter and Guard Plates

heaters at more than one radius, select these radii by using the criteria given in [Annex A2](#).

5.6.1.2 *Guard Plate*—For a guarded hot plate with the outer radius of the guard plate equal to 2.5 times the radius to the center of the gap, locate the line-heat source at a radius equal to 1.29 times the radius to the center of the gap. If another line-heat source is required in the guard plate, locate the heat source at a radius of 1.97 times the radius to the center of the gap. Use the criteria given in [Annex A2](#) for determining other radii of line-heat sources in the guard plate.

NOTE 7—The location(s) of the line-heat sources in the guard plate is (are) less critical than is the case for the meter plate.

5.6.2 *Type of Heater*—Select the line-heat source from one of the following types of heater elements: (1) thin ribbon; (2) sheathed; or (3) any other stable type that provides a uniform heat output per unit length, for example, fine resistance wire with dielectric insulation.

5.6.2.1 *Ribbon Heater*—A thin ribbon heater consists of an etched foil or wire-wound heating element sandwiched between two layers of electrical insulation. Select the type of electrical insulation based on the temperatures of interest.

5.6.2.2 *Sheathed Heater*—A sheathed heater, sometimes known as a cable heater or a swaged heater, consists of a straight or coiled heater element insulated from its surrounding metal sheath by compacted ceramic powder. This type of heater is suitable for high temperatures, depending upon the type of resistance wire and sheath that are selected.

### 5.6.3 Installation of Heaters:

5.6.3.1 Install the ribbon heater(s) by fabricating the plate (meter or guard) in two concentric sections and placing the heater between the sections by either an interference fit or a tapered fit. Prepare the interference fit by applying a moderate temperature difference to the two concentric sections as described in the adjunct.<sup>4</sup>

5.6.3.2 Install the sheathed heater(s) by pressing the heater into circular grooves that have been cut into one (or more) surface(s) of the plate (meter or guard). The grooves shall be sufficiently deep that the heater will be below the surface of the plate. Fill the remainder of the groove with either conductive epoxy, solder, or braze.

5.6.4 *Lead Wires for Heater*—In order to minimize undesired heat generation from the heater leads, select lead wires that have a lower electrical resistance per unit length than the heater element(s). The heater elements shall have either integral electrical lead wires, or individual insulated lead wires attached to the heater elements with the junctions electrically insulated (with, for example, epoxy or ceramic cement). Secure the electrical connections so they are reliable and insulated electrically from the guarded hot plate.

NOTE 8—Since some heat will be generated by the wire leads, thereby perturbing the temperature profile, consideration shall be given to where the leads are located and how they are installed. Refer to [Appendix X2](#) for guidance on locating the wire heater leads.

### 5.7 Support Structures:

5.7.1 *Support for Meter Plate*—Design the support system for the meter plate to:

NOTE 6—For example, a guarded hot plate with a 600-mm diameter guard plate will be flat over its entire surface to within 0.15 mm.

5.5.5.2 During fabrication, assembly, and installation of the guarded hot plate, care shall be taken to achieve this flatness tolerance. For a metal plate, it will be necessary to anneal the plate to relieve stresses introduced during machining and then grind the plate(s) to final tolerances. Continued checking is necessary to ensure the flatness tolerance is maintained after temperature cycling.

### 5.5.6 Surface Emittances:

5.5.6.1 *Guarded Hot Plate*—Treat the surfaces of the guarded hot plate to maintain a total hemispherical emittance greater than 0.8. In any case, the hot plate surface emittance shall meet the requirements of Test Method [C177](#).

5.5.6.2 *Gap*—To minimize the heat flow across the gap, either treat the surfaces of the gap (by polishing or electroplating) to reduce their emittance, or fill the gap with thermal insulation.

5.6 *Heater Design*—Select the radius of each circular line-heat source for the meter plate and the guard plate as follows.

### 5.6.1 Location of Heaters:

5.6.1.1 *Meter Plate*—If the meter plate has a single line-heat source, locate the heat source at a radius equal to  $\sqrt{2}/2$  times the radius to the center of the gap. If it is desired to have

5.7.1.1 Facilitate assembly of the meter and guard plates so that the two plates are co-planar (per 5.5.5) and concentric with a uniform gap width (per 5.5.3),

5.7.1.2 Support the mass of the meter plate as well as the forces from clamping the test specimens,

5.7.1.3 Account for the effects of thermal expansion of the meter and guard plates,

5.7.1.4 Minimize heat conduction between the meter and guard plates, and

5.7.1.5 Facilitate installation and repair of the line-heat sources, lead wires, and sensors.

NOTE 9—Extraneous heat flows caused by the support system will disturb the desired temperature distribution in the meter plate. One successful technique consists of a system of three small pins with both ends tapered that are installed in radially drilled holes in the guard plate. A tapered-end screw pushed against the outer end of each pin presses the other end of the pin into a circumferential groove in the outer edge of the meter plate. This system will center the meter plate accurately so that the gap width is uniform (per 5.5.3).

5.7.2 *Support for Guard Plate*—Design the support system for the guard plate to maintain the guarded hot plate in the desired orientation (usually the plane of the hot plate will be either horizontal or vertical), and, minimize conductive heat losses from the guard plate.

NOTE 10—Extraneous heat flows caused by the support structure will disturb the desired temperature distribution in the guard plate. One successful technique for supporting the guard plate is wire cables (at three or four locations) at the periphery of the guard plate. A second technique is to rigidly support the underside of the guard plate at the periphery either from above or below.

## 5.8 Temperature Sensors:

5.8.1 *Type*—Select temperature sensors for the guarded hot plate that provide adequate sensitivity and do not significantly change the temperatures that are to be measured. At modest temperatures, select sensors from the following types: (1) thermocouples (either Type T or Type E wire being the most commonly used); (2) small, accurate (platinum) resistance thermometers; or (3) stable thermistors. At extreme temperatures (high or cryogenic), consult Specification E230 or Ref (12) for the use of thermocouples for temperature measurement.

5.8.2 *Calibration*—Temperature sensors shall be calibrated with standards traceable to a national standards laboratory.

NOTE 11—The overall uncertainty depends not only on the type of sensor and its calibration, but also on the measurement system. Normal precautions require minimizing spurious voltages by locating junctions of dissimilar metals in regions of low thermal gradients and using high quality low-thermal emf switches. For further guidelines, consult Test Method C177.

5.8.3 *Location in Meter Plate*—If the line-heat source is located per 5.6.1 in the meter plate, then locate the temperature sensor at the outer radius of the meter plate. Consult Appendix X2 for the angular location of the temperature sensor. For other cases with multiple radii, locate the temperature sensor at the center plane of the meter plate.

5.8.4 *Location in Gap*—Use a thermopile to detect directly the temperature difference across the gap, rather than separate measurements of the absolute temperature of the meter and guard-sides. In order to reduce heat conduction through the

thermopile wires, select (1) wires of small diameter and low thermal conductivity; (2) the minimum number of thermocouple junction pairs necessary for adequate sensitivity; and (3) an oblique (rather than radial) path for the wires to cross the gap.

5.8.4.1 *Thermoelements*—Select thermoelements that have a high thermopower ( $\mu\text{V/K}$ ) and relatively low thermal conductivity of both alloys, such as Type E thermocouple wire, having a diameter no greater than 0.3 mm. Thermopiles constructed from copper thermoelements shall not be used.

5.8.4.2 *Sensitivity*—If the line-heat source is located per 5.6.1 in the meter plate, locate the minimum number of thermocouple junctions relative the heater leads as described in Appendix X2.

NOTE 12—Different designs for guarded hot plates have used anywhere from a few pairs of thermocouple junctions to several dozen pairs to achieve both adequate sensitivity and adequate sampling of the temperature on either side of the gap. The number of thermocouple junctions needs to provide the desired resolution of the temperature difference across the gap. For example, if thermocouple wire with a nominal thermopower of  $60 \mu\text{V/K}$  is used, a thermopile with 16 pairs of junctions will have a thermopower of  $960 \mu\text{V/K}$ . For such a thermopile, measurement of the thermopile output to a resolution of  $1 \mu\text{V}$  will correspond to a resolution in the temperature difference across the gap of approximately 1 mK.

5.8.4.3 *Installation*—Place all thermocouple junctions in good thermal contact with the meter plate or guard plate and secure, when necessary, by mechanical fasteners. Insulate electrically all thermocouple junctions from the meter plate and guard plate.

5.8.5 *Location in Guard Plate*—Measure the temperatures of the primary guard using thermocouples, (platinum) resistance thermometers, or thermistors, or indirectly using differential thermocouples.

NOTE 13—Temperatures in the guard plate do not enter directly into the calculation of thermal transmission properties. However, it is important to measure temperatures at selected locations in the guard plate to verify correct operation of the guarded hot plate.

## 6. Design Precautions

6.1 Error in the measurement of the temperature of the guarded hot plate is introduced from several sources, including: (1) improper design of the guarded hot plate; (2) location of the temperature sensor; and (3) calibration of the temperature sensor as well as the measurement system (see 5.8.2).

6.2 A basic premise in the design of the guarded hot plate is the location of the line-heat source at a prescribed radius as described in Annex A2. This ensures that the mean temperature of the surface of the meter plate is equal to the temperature at the edge of the meter plate. The radial temperature profile is affected by the thermal conductivity of the plate. Consequently, the thermal conductivity of the plate shall be high relative to the specimen (see Annex A2).

6.3 Experimental checks to verify the radial temperature distribution include independent temperature measurements of the guarded hot plate with thermocouples, for example, as described in Refs (5), (8).

6.4 Angular perturbations in the temperature profile are due to heating from the heater leads crossing the gap. In this case,

additional temperature sensors will be necessary to determine adequately the mean temperature of the surface of the meter plate.

7. Keywords

7.1 guarded hot plate apparatus; heat flow; line source heater; steady state; thermal conductivity ; thermal insulation; thermal resistance

ANNEXES

(Mandatory Information)

A1. CONTROL OF EDGE HEAT LOSS OR GAIN

A1.1 Scope

A1.1.1 This annex provides a procedure for determining the diameter of the guard plate and ambient temperature conditions required to reduce the edge effects to negligible proportions. Alternative procedures are allowed, but it is the responsibility of the user to determine that those procedures yield equivalent results.

A1.2 Theoretical Analysis

A1.2.1 For an apparatus with an isothermal guarded hot plate and cold plate(s), the error due to edge heat loss or gain has been derived for both circular and square plates by Peavy and Rennex (10), for the case of the specimen being anisotropic, and by Bode (11), for the isotropic case. The error due to edge heat transfer in a guarded hot plate apparatus is given by:

$$\varepsilon = A + BX \tag{A1.1}$$

where:

$$X = \frac{2(T_m - T_a)}{T_h - T_c} \tag{A1.2}$$

Here,  $T_h$  is the guarded hot plate temperature, and  $T_c$ , the cold plate temperature. The mean temperature of the specimen is  $T_m = (T_h + T_c)/2$ , and  $T_a$  is the ambient temperature at the edge of the specimen.

A1.2.2 For a circular plate geometry, the coefficients  $A$  and  $B$  are given by:

$$A = \sum_{n=1}^{\infty} W_{2n} \tag{A1.3}$$

$$B = \sum_{n=1}^{\infty} W_{2n-1} \tag{A1.4}$$

The terms in the summations are given by:

$$W_n = \frac{4}{\pi^2} \left( \frac{hL}{\lambda} \right) \left( \frac{\gamma L}{b} \right) \frac{I_1(n\pi b/\gamma L)}{n^2 [I_1(n\pi d/\gamma L) + (hL/n\pi\lambda)I_0(n\pi d/\gamma L)]} \tag{A1.5}$$

where  $I_0$  and  $I_1$  are modified Bessel functions of the first kind of order 0 and 1, respectively,  $b$  is the radius to the center of the

gap,  $d$  is the outer radius of the guard plate,  $L$  is the thickness of the specimen, and  $h$  is the heat transfer coefficient at the circumference of the specimen. The anisotropy ratio for the specimen is  $\gamma^2 = \lambda_r/\lambda_z$  where  $\lambda_r$  and  $\lambda_z$  are the thermal conductivities in the radial and axial directions, respectively. The geometrical mean of the thermal conductivities is  $\lambda = (\lambda_r\lambda_z)^{1/2}$ .

A1.2.3 For the range of parameters that provide appropriate guarding, Eq A1.3 and Eq A1.4 are convergent and require only a few terms to obtain accurate results. Peavy and Rennex (10) provide plots of  $A$  and  $B$  as functions of geometry and of the ratio of heat transfer coefficient,  $h$ , to specimen conductivity.

A1.2.4 For relatively small values of  $A$  and  $B$ , approximate universal curves are obtained by writing:

$$A = \frac{\frac{hL}{\lambda}}{1 + \left(1 + \frac{\gamma L}{4\pi d}\right) \frac{hL}{2\pi\lambda}} A' \tag{A1.6}$$

$$B = \frac{\frac{hL}{\lambda}}{1 + \left(1 + \frac{\gamma L}{2\pi d}\right) \frac{hL}{\pi\lambda}} B' \tag{A1.7}$$

where  $A$  and  $B$  are computed from Eq A1.3 and Eq A1.4 and  $A'$  and  $B'$  are then computed using Eq A1.6 and Eq A1.7. Fig. A1.1 and Fig. A1.2 present parametric curves of  $A'$  and  $B'$ , respectively, as functions of  $\gamma L/d$ . The values computed for  $A'$  and  $B'$  are also weak functions of  $hd/\lambda$ . The widths of the lines shown in Fig. A1.1 and Fig. A1.2 correspond to the variations due to  $hd/\lambda$  being varied from 0.1 to infinity. Fig. A1.1 and Fig. A1.2 are used to obtain values of  $A'$  and  $B'$ , from which  $A$  and  $B$  are computed using Eq A1.6 and Eq A1.7.

A1.2.5 For values of  $d/b$  not shown, or for values of  $\gamma L/d$  larger than unity,  $A$  and  $B$  are obtained from Peavy and Rennex (10) or computed directly from Eq A1.3 and Eq A1.4. Alternatively, upper limits on  $A'$  and  $B'$  are computed simply from the expressions:

$$A' < \frac{1}{\pi^2} \left( \frac{\gamma L}{b} \right) \left( \frac{d}{b} \right)^{1/2} \exp\left( \frac{-2\pi(d-b)}{\gamma L} \right) \tag{A1.8}$$