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Standard

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Cylindrical involute gears and gear pairs —

Part 2:

Calculation and measurement of tooth thickness and backlash

Roues dentées et engrenages cylindriques en développante de cercle —

Partie 2: Calcul et mesurage de l'épaisseur de dent et du jeu de battement

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Foreword

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