
**Information technology — Language
independent arithmetic —**

**Part 1:
Integer and floating point arithmetic**

*Technologies de l'information — Arithmétique indépendante de
langage —*

Partie 1: Arithmétique de nombres entiers et en virgule flottante

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ISO copyright office
Case postale 56 • CH-1211 Geneva 20
Tel. + 41 22 749 01 11
Fax + 41 22 749 09 47
E-mail copyright@iso.org
Web www.iso.org

Published in Switzerland

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Foreword

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The main task of the joint technical committee is to prepare International Standards. Draft International Standards adopted by the joint technical committee are circulated to national bodies for voting. Publication as an International Standard requires approval by at least 75 % of the national bodies casting a vote.

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ISO/IEC 10967-1 was prepared by Joint Technical Committee ISO/IEC JTC 1, *Information technology*, Subcommittee SC 22, *Programming languages, their environments and system software interfaces*.

This second edition cancels and replaces the first edition (ISO/IEC 10967-1:1994), which has been technically revised.

ISO/IEC 10967-1 consists of the following parts, under the general title *Information technology — Language independent arithmetic*:

— *Part 1: Integer and floating point arithmetic* [10967-1:2012](https://standards.iteh.ai/catalog/standards/iso/13295cc0-9e67-4f42-a48d-cb19c894fa8e/iso-iec-10967-1-2012)

— *Part 2: Elementary numerical functions*

— *Part 3: Complex integer and floating point arithmetic and complex elementary numerical functions*